The Standard model Day 2

Jon Butterworth





Neutrinos

- Neutrino = Italian for neutral ['neu'] small ['ino'] one
- First the *electron neutrino* was conceived in the mind of Wolfgang Pauli in 1930 as a 'desperate remedy' to explain electron energy spectrum in β decay, thought to be
 - To conserve lepton flavour number, v_e has $L_e(v_e) = +1$
 - Electron neutrinos were subsequently discovered by Reines and Cowan in 1956 [!]
 - Muon neutrino 'discovered' in 1962
 - Tau neutrino existence implied by previous experiments, but finally 'discovered' only in 2000. (The last matter particle of the SM.)



KATRIN





Tritinium decays, releasing an electron and an antielectron-neutrino. While the neutrino escapes undetected, the eletron starts ist journey to the detector. Electrons are guided towards the sprectrometer by magnetic fields. Tritium has to be pumped out to provide tritium free spectrometers. The electron energy is analyzed by applying an electrostatic retarding potential. Electrons are only transmitted if their kinetic energy is sufficiently high. At the end of their journey, the electrons are counted at the detector. Their rate varies with the spectrometer potential and hence gives an integrated β-spectrum.

- Neutrinos have mass
 - New unitary mixing matrix, potential new source of CP violation

$$egin{bmatrix}
u_e \
u_\mu \
u_ au \end{bmatrix} = egin{bmatrix} U_{e1} & U_{e2} & U_{e3} \ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \ U_{ au 1} & U_{ au 2} & U_{ au 3} \end{bmatrix} egin{bmatrix}
u_1 \
u_2 \
u_2 \
u_3 \end{bmatrix}.$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{\rm CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{\rm CP}} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
$$= \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{\rm CP}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{\rm CP}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{\rm CP}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{\rm CP}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{\rm CP}} & c_{23}c_{13} \end{bmatrix}.$$

Pontecorvo–Maki–Nakagawa–Sakata (PMNS) matrix



- Neutrinos have mass
 - New unitary mixing matrix, potential new source of CP violation $\begin{vmatrix} \nu_e \\ \nu_\mu \\ \nu_e \end{vmatrix} = \begin{vmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \end{vmatrix} \begin{vmatrix} \nu_1 \\ \nu_2 \\ \nu_2 \end{vmatrix}.$
 - Maybe new (Majorana?) mass terms

$$\begin{split} U &= \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix} \\ &= \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{bmatrix} \\ &= \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{bmatrix} \begin{bmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{bmatrix} \end{split}$$





Neutrinoless double beta decay(?)



Three lepton generations

Generation	Particle	Mass (MeV)	Q/e	Le	L_{μ}	L_{τ}
1	$ u_{ m e}$	$< 2 \times 10^{-6}$	0	1	0	0
	e ⁻	0.511	-1	1	0	0
2	$ u_{\mu} $	< 0.19	0	0	1	0
	μ^-	105.658	-1	0	1	0
3	$ u_{ au}$	< 18.2	0	0	0	1
	$ au^-$	1777	-1	0	0	1

QUIZ