

# FFT Normalisation

$$\sum_{i=0}^{N-1} V_i^2 = \frac{1}{N} \sum_{i=0}^{N-1} |H_i|^2 \quad \text{Parseval}$$

$$y_i = \frac{\Delta t}{N \Delta f} |H_i|^2 \quad \text{Chosen power estimator}$$

$$\Delta t \sum_{i=0}^{N-1} V_i^2 = \Delta f \sum_{i=0}^{N-1} y_i = \frac{\Delta t}{N} \sum_{i=0}^{N-1} |H_i|^2$$

$Y_i$  is the power per frequency in a frequency bin

$$A_i = \frac{|H_i|}{\Delta f}$$

Chosen Amplitude estimator (per frequency bin)

$$A_i = \frac{2|H_i|}{\Delta f}$$

Actually use twice this as FFTW will return  $2N+1$  frequency bins

$$P_i = 2 \left( \frac{\Delta f A_i}{2} \right)^2 \frac{\Delta t}{N \Delta f} = \frac{\Delta t}{N \Delta f} 2 |H_i|^2$$

$A_i$  is what is returned by

`AraJpdWaveformTools::getFFTAplitude()`

$P_i$  is what is used by

`AraJpdFilter::addEventToAveragePower()`