Title

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Declaration

I, Hamzah Hussain confirm that the work presented in this thesis is my own. Where information has been derived from other sources, I confirm that this has been indicated in the thesis.

Abstract

Acknowledgements

Contents

Li	st of	Figures	8
Li	st of	Tables	10
1	Intr	roduction	11
	1.1	Author's Contributions	13
2	Neu	trino Phenomenology and Double Beta Decay	14
	2.1	The Standard Model Neutrino	14
	2.2	Origins of Neutrino Mass	15
		2.2.1 Neutrino Mixing and Oscillation Phenomenology	16
		2.2.2 Oscillation in a Vacuum	17
		2.2.3 Oscillations in Matter	18
		2.2.4 Oscillations Parameters	19
	2.3	Mass Hierarchy	20
		2.3.1 CP Violation	21
	2.4	Beyond Standard Model Neutrino Mass	21
		2.4.1 Dirac Mass	21
		2.4.2 Majorana Mass	22
		2.4.3 See-Saw Mechanism	23
	2.5	Neutrino Mass Constraints	24
		2.5.1 Beta Decay	24
		2.5.2 Cosmological Constraints	26
		2.5.3 Neutrinoless Double Beta Decay	27
	2.6	Beta Decay	28
	2.7	Two Neutrino Double Beta Decay $(2\nu\beta\beta)$	30
	2.8	Neutrinoless Double Beta Decay $(0\nu\beta\beta)$	31
		2.8.1 Light Neutrino Exchange	33
		2.8.2 Majoron Emission	34
		2.8.3 Right Handed Current	36
	2.9	Nuclear Matrix Elements	38
	2.10	Open Questions on the Nature of Neutrinos	39
		2.10.1 Single and Higher State Dominance	39
3	The	e SuperNEMO Demonstrator	40
	3.1	The SuperNEMO Demonstrator Design	41
		3.1.1 Source Foil	43

		3.1.2 Tracker	44
		3.1.3 Calorimeter	46
			47
		3.1.5 Calibration	47
	3.2	Commissioning Progress	49
		3.2.1 Expected Sensitivity	49
	3.3	Backgrounds Sources	50
		3.3.1 Background Locations	50
		3.3.2 Other DBD Experiments	53
		3.3.3 Magnetic Coil and Shielding	54
	3.4	Motivation for Magnetic Field Studies	55
			56
		3.4.2 Magnetic Shield Testing	58
4	Ana	dysis Techniques	59
	4.1	Falaise	59
			60
			61
			61
		v	62
			63
	4.2	1 0	64
			64
			65
		1	66
	4.3		68
	4.4	1	71
	4.5		72
	1.0	11	73
	4.6	8	75
	4 7	4.6.1 Feldman-Cousins	75
	4.7	Minimum Detectable Activity	75
5		U U	77
	5.1		77
	5.2		78
		5.2.1 2e Channel Selection	78
		1	79
	5.0	1	81
	5.3		82 85
	54		85
	5.4	Summary of Double Beta Decays	86

6 Conclusion

 $\mathbf{7}$

List of Figures

2.1	Hierarchy [7]
2.1 2.2	DiracCoupling [9]
$\frac{2.2}{2.3}$	Bitaccoupling [9] 22 BetaSpectrum [11] 25
2.3 2.4	$msquared [12] \dots \dots$
$2.4 \\ 2.5$	HierarchyLimit
$2.0 \\ 2.6$	SEMF [16] 30
2.0 2.7	2vFeynman [16]
2.1	$\begin{array}{c} 2 \text{VFeynman} [16] \\ 0 \text{vFeynman} [16] \\ \dots \\ $
2.8 2.9	$BlackBox [22] \dots $
2.9	MajoronEmission [24] 35
2.10	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
	0vRH [23]
2.12 2.12	WRII [25]
	NMEValues [34] 39
3.14	$Demons Detector \qquad \qquad$
3.2	FullDetector [37] 43
3.3	Isotope Properties
3.4	TrackerCells
3.4	
$3.5 \\ 3.7$	0
3.1 3.8	1
3.9	
	$BiPoDetector [40] \dots \dots$
	Bi214DecayScheme
	Tl208DecayScheme
	A
	A
	A
	A
4.1	Visualization of the Falaise pipeline structure, beginning with simulation and ending
	with the stored data banks for reconstructed data
4.2	User interface of the Flvisualize tool used for visually displaying simulated and re-
	constructed events. The left hand side displays a 2D top view of the detector whereas
	the right hand side displays a 3D projection of the detector parallel to the foil 62

4.3	Representation of a reconstructed event with two charged particle tracks, the first	
	belonging to an electron (blue track) and the second to a positron (green track), with	
	an initial decay vertex on the source foil	65
4.4	Representation of a reconstructed event with one electron (blue track) as well as a	
	photon (yellow calorimeter hit with an unassociated/dashed track), with an initial	
	decay vertex on the source foil.	66
4.5	Representation of a reconstructed event with one electron (blue track) as well as an	
	alpha (short red track), with an initial decay vertex on the source foil	67
4.6	Internal (a) and external (b) probabilities for $0\nu\beta\beta$, internal, radon and external	
	backgrounds with reconstructed 2e topologies. The probability distributions were	
	calculated using the equations 4.5 and 4.8 respectively	70
4.7	$0\nu\beta\beta$ total energy spectra for the three magnetic field configurations, with the region	
	of interest (2.8 - 3.2 MeV) highlighted in red.	74
4.8	Probability distributions for the two Poisson variables, B and $S+B$. The black curve	
	represents the background distribution and the red curve signal + background, with	
	the shaded areas each corresponding to 1 - CL [16]	76
5.1	0 and $2\nu\beta\beta$ total energy spectra for events with a 2e topology with all three magnetic	
	fields. The $0\nu\beta\beta$ spectra are illustrated by the thick line and $2\nu\beta\beta$ by the dotted line.	83
5.2	0 and $2\nu\beta\beta$ single electron energy spectra for events with a 2e topology with all three	
	magnetic fields. The $0\nu\beta\beta$ spectra are illustrated by the thick line and $2\nu\beta\beta$ by the	.
-	dotted line.	84
5.3	0 and $2\nu\beta\beta \cos\theta$ spectra for events with a 2e topology with all three magnetic fields.	
	The $0\nu\beta\beta$ spectra are illustrated by the thick line and $2\nu\beta\beta$ by the dotted line. All	o 4
	events have a total energy within the 82 Se ROI (2.8 - 3.2 MeV)	84

List of Tables

1	- [6]	19
2	$0\nu\beta\beta$ cut flow for the three magnetic field configurations. Each row lists a short	
	description of the cut as well as the concurrent detection efficiency. \ldots \ldots \ldots	80
3	$2\nu\beta\beta$ cut flow and number of expected events for the three magnetic field configura-	
	tions. Each row lists a short description of the cut as well as the concurrent detection	
	efficiency.	82
4	Best case scenario detector sensitivity estimate for the three magnetic fields. Best	
	case scenario assumes only $2\nu\beta\beta$ as a contributing background to the ⁸² Se $0\nu\beta\beta$ ROI.	85
5	Summary table of the $0/2\nu\beta\beta$ detection efficiency, $2\nu\beta\beta$ number of expected events	
	and the sensitivity estimates for the three magnetic fields	86

Chapter 1

Introduction

Although neutrinos are the most abundant matter particles in the known Universe, their low interaction cross sections have made the neutrino one of the most mysterious particles in the Standard Model (SM) of particle physics. Historically, the Standard Model has been extremely successful at accurately predicting a number of parameters, most recently however, the discovery of neutrino oscillation was beyond any Standard Model prediction for the neutrino. Neutrinos were known to exist in three different flavour eigenstates, ν_e , ν_{μ} and ν_{τ} however the phenomenon of neutrino oscillation allows the neutrinos to mix between the different flavour eigenstates. Most importantly, the observation of neutrino oscillation proved that neutrinos were in fact massive particles, contradictory to the standard model prediction of massless neutrinos. Additionally, this raised the question of whether the non-zero neutrino mass is a Dirac or Majorana mass. If the neutrino has a Dirac mass, like the other Standard Model fermions, then the neutrino and anti-neutrino would be distinctly unique particles, whereas if the neutrino has a Majorana mass, the neutrino would be its' own antiparticle.

One such method for investigating the nature of neutrino mass is to examine the beyond Standard Model (BSM) interaction of neutrinoless double beta decay $(0\nu\beta\beta)$. Neutrinoless double beta decay is a hypothesised nuclear decay and the neutrinoless analogue of two neutrino double beta decay $(2\nu\beta\beta)$, which is an exotic rare nuclear decay resulting in the emission of two beta electrons and two associated neutrinos from the same nucleus. Observing neutrinoless double beta decay would affirm the Majorana nature of the neutrino whilst providing additional insight into the absolute neutrino mass scale and hierarchy.

Many experiments have been developed to probe and measure the hypothetical $0\nu\beta\beta$ decay including the SuperNEMO detector, which is the successor to the previous NEMO-3 experiment that ran and collected data for number of different double beta decaying isotopes between 2003 and 2011. The complete SuperNEMO detector design comprises of 20 smaller demonstrator modules, each holding between 5 and 7 Kg of the double beta decaying isotope ⁸²Se. Currently a single SuperNEMO demonstrator module is undergoing construction and commissioning in the Laboratoire Souterrain de Modane. The demonstrator module combines unique tracking and calorimetry techniques in order to study the 6.25 Kg of ⁸²Se source foil located at the centre of the demonstrator. The tracking capabilities of the SuperNEMO demonstrator allows the trajectory of reconstructed charged particles to be determined with high accuracy in three dimensions and the segmented calorimeters allows for the energies of individual particles to be measured. Also, there is the option to apply a magnetic field to the tracker volume, in order to identify particles via their curvature in response to the applied field. Reconstructed particle kinematics combined with particle identification can be used to efficiently reject multiple backgrounds, however the currently proposed magnetic field may in fact not provide the best performance for the demonstrator module and there is also the possibility of taking data without turning on the magnetic field from the beginning.

A short description of each chapter is provided below:

- i The first chapter includes an introduction to neutrino phenomenology as well as the underlying physics of double beta decay.
- ii Chapter two overviews the SuperNEMO experiment and demonstrator module, including the relevant backgrounds for ⁸²Se double beta decay. Also, the definition of the realistic magnetic field is given ***
- iii Chapter three gives a description of the different analysis techniques used in the thesis, including the internal software package Falaise. Additionally, the reconstructed topologies of different particles of are described and how they come together to measure particles in particular decay channels. Finally, the tools needed to estimate the total signal and background contributions as well as the overall sensitivity of the study are given.
- iv Chapter four provides an in depth description of the double beta decay event selection used to determine if a reconstructed event has a double beta topology. Furthermore, the detection efficiency for $0\nu\beta\beta$ and the contribution from the irreversible background $2\nu\beta\beta$ are discussed.
- v In chapter six, descriptions for the different classifications of backgrounds are provided and the contribution of those backgrounds to the 82 Se sensitivity are shown.
- vi Chapter 7 discusses the optimization process for reducing the prominent backgrounds from the previous chapter and provides estimations for the overall sensitivity using the statistical approximations discussed in the analysis techniques chapter.
- vii The final chapter concludes the magnetic field study, providing suggestions for how to approach the installation of the magnetic field or whether a magnetic field should in fact be used with the SuperNEMO demonstrator module, based on the results of the study.

1.1 Author's Contributions

Chapter 2

Neutrino Phenomenology and Double Beta Decay

The neutrino was first proposed by Wolfgang Pauli in 1930, following observations of continuous energy spectra from β decay electrons. Pauli suggested the existence of a small uncharged particle, emitted alongside the β electron, allowing the decay to conserve energy, momentum and spin. Enrico Fermi coined the name neutrino in reference to the similarly uncharged neutron, following its discovery by James Chadwick in 1932.

Having no electric or colour charge made the neutrino very difficult to identify from low intensity beta decaying isotopes and it wasn't until the 1950s that experimental evidence of the neutrino was first discovered at the Savannah River Nuclear Reactor. ***Ref*** Cowan and Reines erected a nearby detector and successfully used the giant flux of antineutrinos coming from the reactor to illustrate the process of inverse beta decay, winning them the 1995 Nobel Prize. Over the following half century, further breakthroughs were made in the field of neutrino physics, including the discovery of multiple neutrino flavours, $\nu_{electron}$, ν_{muon} and ν_{tau} , corresponding to the three charged leptons. In the late 1960s, the Homestake experiment first measured the incoming solar neutrino flux as roughly 1/3 to 1/2 of the hypothesised flux [1], ultimately resulting in the discovery of neutrino and non-zero neutrino mass.

2.1 The Standard Model Neutrino

The Standard Model of particle physics describes fundamental particles and their interactions through the three underlying forces, the electromagnetic, the strong nuclear and the weak nuclear force. It is a renormalizable quantum field theory with an $SU(3) \ge SU(2) \ge U(1)$ symmetry, representing the strong, weak and electromagnetic interactions respectively.

$$\underbrace{SU(3)}_{Strong} \mathbf{x} \underbrace{SU(2) \times U(1)}_{Electroweak}$$

Predictions made by the Standard Model have been experimentally probed and proven to a high degree of accuracy, although the model falls short in certain aspects, in particular, the nonzero mass of neutrinos. Within the Standard Model neutrinos are massless, but we know, from observing oscillations, this is false. Fermions cannot have an explicit gauge invariant mass term in the Standard Model Lagrangian and only gain their mass via spontaneous symmetry breaking. The absence of the right handed neutrino (or left handed anti-neutrino) does not allow the neutrino to couple to the Higgs and so the neutrino does not gain a Yukawa mass term from the Standard Model spontaneous symmetry breaking. The origin of neutrino mass is still unclear, however we know the Standard Model is wrong and neutrinos do have a non-zero mass.

Mass dirac vs Major ***

2.2 Origins of Neutrino Mass

Neutrino oscillation was first proposed by Bruno Pontecorvo, akin to the oscillation observed with Kaons,

$$K^0 \longleftrightarrow \bar{K^0}$$
 (2.1)

However, this proposal was rejected, as a massless neutrino should not undergo oscillation. Results from the Homestake [1] experiment indicated a deficit in the number of expected solar neutrinos, with only 1/3 of the expected number being measured during the experiment, indicating the solar neutrinos were undergoing some interaction causing the flux to reduce.

Electron neutrinos produced by proton-proton fusion in the centre of the sun were used to induce the radiochemical transmutation of ³⁷Cl into ³⁷Ar via the inverse beta process

$${}^{37}\text{Cl}^+ + \nu_e \text{ (Solar)} \longrightarrow {}^{37}\text{Ar} + e^-$$

$$(2.2)$$

Many tons of a ³⁷Cl containing compound were used to interact with the solar neutrinos and the resulting ³⁷Ar gas was collected and measured to estimate the neutrino interaction rate. The deficit of electron neutrinos found in the Homestake experiment was later dubbed the "Solar neutrino problem" and it wasn't until the end of the 20th century when experiments such as Kamiokande-II and SNO (Sudbury Neutrino Observatory) validated the results of the Homestake experiment and determined the number of solar electron neutrinos was suppressed as a result of neutrino oscillation [2].

Pontecorvos initial proposals made in [3] and [4] were and the neutrino was shown to have a non-zero mass contradictory to the Standard Model expectation. In response to the proposal of neutrino oscillations, theorists have postulated

The implication of this discovery

Oscillation -¿ Higgs coupling...?

Three flavour states from Z invisible width

PMNS

2.2.1 Neutrino Mixing and Oscillation Phenomenology

Neutrinos are produced in weak decays and are emitted in their weak flavour eigenstates ν_e , ν_{μ} and ν_{τ} . The flavour eigenstates propagate as plane waves corresponding to superpositions of the mass eigenstates ν_1 , ν_2 and ν_3 . The mixing between the flavour states and the mass states is described by the unitary PMNS (Pontecorvo-Maki-Nakagawa-Sakata) matrix [5],

$$U_{PMNS} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} = \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}}_{\text{Atmospheric}} \underbrace{\begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix}}_{\text{Cross-mixing}} \underbrace{\begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\text{Solar}}$$
(2.3)

with $c_{ij} = \cos \theta_{ij}$, $s_{ij} = \sin \theta_{ij}$. θ_{ij} are mixing angles that have been experimentally calculated and represent the mixing between the mass stated *i* and *j*. Finally δ represent the neutrino CP violating phase. If the neutrino is a Majorana particle (to be discussed in section 2.4.2), additional CP violating phases α_1 and α_2 can be added to the PMNS matrix in equation 2.3, by post-multiplication with the following,

$$\begin{pmatrix}
e^{\frac{i\alpha_1}{2}} & 0 & 0 \\
0 & e^{\frac{i\alpha_2}{2}} & 0 \\
0 & 0 & 1
\end{pmatrix}$$
(2.4)

 U_{PMNS} relates the flavour and mass eigenstates as,

$$\begin{pmatrix} v_e \\ v_\mu \\ v_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} v_1 \\ v_2 \\ v_3 \end{pmatrix}$$
(2.5)

The mixing of flavour and mass eigenstates can be used to illustrate how neutrino oscillation implicitly infers the non-zero mass of neutrinos, starting with oscillations in a vacuum.

2.2.2 Oscillation in a Vacuum

From equation 2.3, the relationship between a single flavour and mass eigenstate can be written as,

$$|\nu_{\alpha}\rangle = \sum_{i} U_{\alpha i} |\nu_{i}\rangle \tag{2.6}$$

where α represents the flavour states $\nu_{e,\mu,\tau}$ and *i* the mass states $\nu_{1,2,3}$. The mass states ν_i evolve according to the Schrödinger equation and so the time evolution of the mass eigenstate can be written as (in natural units),

$$|\nu_i(t)\rangle = e^{-i(E_i t - p_i L)} |\nu_i(0)\rangle \tag{2.7}$$

where L is the distance travelled and m_i the mass of the eigenstate.

The relativistic energy, as a result of the low neutrino mass, can be approximated as,

$$E_i = \sqrt{p_i^2 + m_i^2} = p_i \left(1 + \frac{m_i^2}{p_i^2}\right)^{1/2} \approx p_i + \frac{m_i^2}{2p_i}$$
(2.8)

and so the time evolution becomes,

$$|\nu_i(t)\rangle = e^{-i\left(m_i^2/2p_i\right)L} |\nu_i(0)\rangle$$
(2.9)

When taking $E \approx p$ for the relativistic neutrino, equation 2.6 can be written as,

$$|\nu_{\alpha}(L)\rangle \approx \sum_{i} U_{\alpha i} e^{-i\left(m_{i}^{2}/2E\right)L} |\nu_{i}\rangle = \sum_{i,\beta} U_{\alpha i} U_{\beta i}^{*} e^{-i\left(m_{i}^{2}/2E\right)L} |\nu_{\beta}\rangle$$
(2.10)

The probability for ν_{α} oscillating to ν_{β} is,

$$P(\alpha \to \beta)(L) = |A(\alpha \to \beta)(L)|^2 = |\langle \nu_\beta \mid \nu_\alpha(L) \rangle|^2$$
(2.11)

where A is the transition amplitude for $\nu_{\alpha} \rightarrow \nu_{\beta}$.

Using equation 2.10, the transition probability is,

$$P_{\nu_{\alpha} \to \nu_{\beta}}(L) = \sum_{i,j} U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^* e^{-i\left(\Delta m_{ij}^2/2E\right)L}$$
(2.12)

with $\Delta m_{ij}^2 = m_i^2 - m_j^2$ the mass difference between the two mass eigenstates.

According to equation 2.12, in order for oscillations to occur, the Δm_{ij}^2 term must be non-zero. Δm_{ij}^2 is a mass squared difference and so the absolute mass of the neutrino eigenstates cannot be determined directly from oscillations in a vacuum. By measuring the oscillation of one neutrino flavour to another, the mass squared difference can be determined by controlling for the distance travelled L and the energy of the neutrino E.

2.2.3 Oscillations in Matter

Neutrino oscillations also occur in matter, however the presence of significantly dense matter alters the behaviour of the neutrino as it passes through. Neutrinos of all flavours are able to interact with matter via neutral current interactions, exchanging an intermediary Z_0 boson. However, the prevalence of electrons in matter, allows for the charged current interaction between the ν_e and electron, with the exchange of a W^- boson, to occur. As a result, the flavour states undergo different interactions when traversing matter, altering the oscillatory behaviour of the neutrinos. The changing oscillatory behaviour of the neutrinos in matter is known as the Mikheyev-Smirnov-Wolfenstein or MSW effect.

One of the most important examples of the MSW effect is the propagation of solar neutrinos through the sun. The MSW effect is sensitive to both the electron density and neutrino energy. When neutrinos are produced in the centre of the sun, during proton-proton fusion, the significant density at the centre of the sun results in the neutrinos being skewed towards the heavier mass eigenstate. However as the density decreases away from the sun and eventually becomes negligible as the neutrino leaves the sun, the neutrino is in the mass eigenstate ν_2 , and so does not mix as it propagates through space until it reaches earth. Measuring these solar neutrinos provides data for the Δm_{21}^2 .

**** Dirac mass and alpha term ***

Parameter	Value
$\sin^2(\theta_{12})$	0.307 ± 0.013
Δm^2_{21}	$(7.53 \pm 0.18) \times 10^{-5} \text{ eV}^2$
$\sin^2(\theta_{23})$ IH	0.539 ± 0.022
$\sin^2(\theta_{23})$ NH	0.546 ± 0.021
Δm^2_{32} IH	$(-2.524 \pm 0.034) \times 10^{-3} \text{ eV}^2$
Δm^2_{32} NH	$(2.453 \pm 0.033) \times 10^{-3} \text{ eV}^2$
$\sin^2(heta_{12})$	$(2.20 \pm 0.07) \times 10^{-2}$
δ CP violating phase	$1.36^{+0.20}_{-0.16} \pi \mathrm{rad}$
$\left< \Delta m^2_{21} - \Delta \bar{m}^2_{21} \right>$	$<1.1 \times 10^{-4} \text{ eV}^2, \text{ CL} = 99.7\%$
$\left< \Delta m_{32}^2 - \Delta \bar{m}_{32}^2 \right>$	$(-0.12 \pm 0.25) \times 10^{-3} \text{ eV}^2$

2.2.4 Oscillations Parameters

Table 1: -[6]

The PMNS matrix shown in equation 2.3 has a number of measurable parameters as shown in table 1. Various neutrino based experiments have been run in the previous few decades in order to improve the constraints set on the PMNS parameters, particularly, the mixing angles and mass squared differences. Reactor and accelerator experiments are the primary detectors used for probing neutrinos and the associated PMNS parameters. Reactor experiments use neutrino fluxes from nearby nuclear reactors in order to measure the neutrino flux whereas accelerator experiments generate a neutron beam that is measured firstly at a near detector and finally at a far detector.

Neutrino oscillation experiments have continued to improve on the previously set constraints for the mixing angles and mass squared differences, however some questions continue to be left unanswered. Currently, only the sign of the Δm_{12}^2 is measurable and so the ordering of the mass constraints is still unknown. Additionally, the CP voilating parameters δ and α_i are still *poorly understood.

2.3 Mass Hierarchy

Neutrino oscillation established the non-zero finite mass of the neutrino, antithetical to the Standard Model picture of the massless neutrino. Currently, the sign of the Δm_{32} term is indistinguishable resulting in the two hypothesised mass eigenstate orderings, the normal hierarchy (NH) and the inverted hierarchy (IH). Observations of the pure ν_2 solar neutrinos described in section 2.2.3 inferred the sign of the Δm_{21} term, confirming $m_{\nu_1} < m_{\nu_2}$. If the Δm_{32} sign is positive ($\Delta m_{32} > \Delta m_{21} > 0$) the neutrino mass ordering follows the normal hierarchy, whereas if the Δm_{32} sign is negative ($\Delta m_{32} < 0 < \Delta m_{21}$), the inverted hierarchy reigns. The NH and IH are illustrated in figure 2.1.

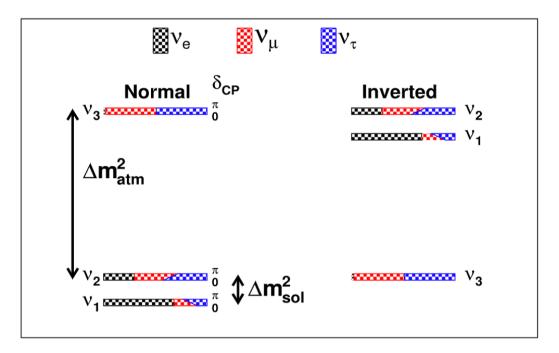


Figure 2.1: Hierarchy [7]

If the normal hierarchy is correct, the lightest mass eigenstate ν_1 would correspond strongly with the electron neutrino, analogous to the to the charged leptons, whereas, if the inverted hierarchy is proven, the lightest mass eigenstate would correspond strongly with the ν_{μ} and ν_{τ} . Ongoing experimental data puts a preference on the normal mass ordering, with a >2.5 σ statistical significance, taking into account double beta decay, cosmological measurements and oscillation data [8], although ***

2.3.1 CP Violation

2.4 Beyond Standard Model Neutrino Mass

As previously highlighted, the standard model prediction of the massless neutrino has been demonstrably disproven by neutrino oscillation. However, there are several SM extensions that allow for a non-zero neutrino mass term, the most common of which are the Dirac and Majorana methods, which add BSM terms for the neutrino mass corresponding to the different neutrino types. The Dirac neutrino is similar to the other standard model leptons, having a distinct particle and anti-particle, whereas the Majorana neutrino is its own antiparticle. Additionally, the See-Saw mechanism proposes a combination of both Dirac and Majorana terms, where each light neutrino has an associated heavy but inert counterpart.

what's in section ***

2.4.1 Dirac Mass

In the Standard Model neutrinos are incorporated as left handed chiral particles, with no right handed equivalent and vice versa for the antineutrino. Charged leptons and quarks gain their mass through the Yukawa coupling of the left and right handed fields to the Higgs,. In order to couple neutrinos to the Higgs field a right handed neutrino field is added for each neutrino flavour, producing a Dirac mass term m_D .

The Dirac term in the Lagrangian manifests as,

$$\mathcal{L}^{\mathcal{D}} = -\frac{1}{2}m_{\nu}^{D}\bar{\nu}\nu = -\frac{1}{2}m_{\nu}^{D}\left(\bar{\nu}_{R}\nu_{L} + \bar{\nu}_{L}\nu_{R}\right)$$
(2.13)

with the chirality operators $P_L = \frac{1}{2} (1 - \gamma_5)$ and $P_R = \frac{1}{2} (1 + \gamma_5)$ decomposing the neutrino into its left and right handed components. The Dirac neutrino mass term can then be defined as,

$$m_i = g_Y \frac{v}{\sqrt{2}} \tag{2.14}$$

The Dirac approach provides a simple lepton number conserving extension to the Standard Model for the purpose of adding the non-zero neutrino mass, although there are a several ramifications of this method. The Lagrangian includes the three right handed neutrino fields which only interact gravitationally (having no electric or weak charge), making them completely sterile to the other Standard Model particles. Additionally, the value of g_Y is inexplicably small, many orders of magnitude lower than the corresponding charged lepton couplings.

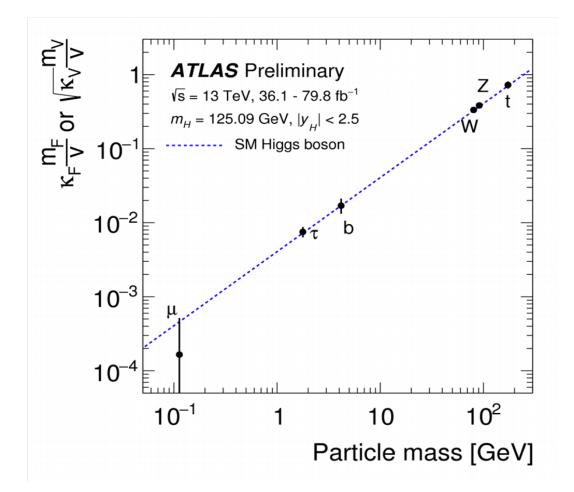


Figure 2.2: DiracCoupling [9]

2.4.2 Majorana Mass

The Dirac mass terms attempts to couple the left and right handed neutrino fields in a lepton conserving manner, with the addition of the sterile right handed neutrinos. However, in 1937, Ettore Majorana contemplated whether the left and right handed neutrinos were not independent particles [10] and were in fact related by a charge conjugation shown in equation 2.15,

$$\nu_R = \xi \mathcal{C} \bar{\nu}_L^T \tag{2.15}$$

with ξ an arbitrary phase factor, C the charge conjugation matrix and ν_R and ν_L the two measured neutrino fields. As shown in equation 2.13, the neutrino can be decomposed into its left and right handed components,

$$\nu = \nu_L + \nu_R \tag{2.16}$$

and using using 2.15 can be rewritten as,

$$\nu = \nu_L + \mathcal{C}\bar{\nu}_L^T = \nu_L + \nu_L^c \tag{2.17}$$

Taking the charge conjugation of the Majorana neutrino and using $\hat{C}|\psi\rangle = C|\bar{\psi}\rangle$,

$$\nu^{c} = (\nu_{L} + \nu_{L}^{c})^{c} = \nu_{L}^{c} + \nu_{L} = \nu$$
(2.18)

inferring the neutrino and its charge conjugate are the same particle. Particles which are their own antiparticles are characterized as Majorana particles. Of all the Standard Model fermions, only the neutrino is capable of being a Majorana particle due to its neutral charge. The Majorana term in the Lagrangian is,

$$\mathcal{L}^M = -\frac{1}{2} m_\nu^M \bar{\nu}_L^c \nu_L \tag{2.19}$$

with m_{ν}^{M} the Majorana mass term. Using the Majorana Lagrangian term, neutrinos are able to acquire mass without a Yukawa coupling, however lepton conservation is violated in the process. Like the Dirac mechanism, the Majorana mass term requires a sterile right handed neutrino, although the Majorana mass provides a better explanation of the difference between the neutrino and charged lepton masses.

2.4.3 See-Saw Mechanism

The See-Saw mechanism combines both the Dirac and Majorana mass terms into a single Lagrangian term,

$$\mathcal{L}^{D+M} = \mathcal{L}^D + \mathcal{L}^M$$

$$= -\frac{1}{2} m_{\nu}^D \left(\bar{\nu}_R \nu_L + \bar{\nu}_L \nu_R \right) - \frac{1}{2} m_{\nu}^M \bar{\nu}_L^c \nu_L + h.c.$$

$$= -\frac{1}{2} \left(\begin{array}{cc} \bar{\nu}_L & \bar{\nu}_L^C \end{array} \right) \begin{pmatrix} m_L & m_D \\ m_D & m_R \end{pmatrix} \begin{pmatrix} \nu_R^C \\ \nu_R \end{pmatrix} + h.c$$
(2.20)

The neutrinos in equation 2.20 are not the mass eigenstates because the mass matrix is not diagonal. To find the mass eigenvalues m_1 and m_2 , the mass matrix is first diagonalised, giving

$$m_{\pm} = \frac{1}{2} \left(m_L + m_R \pm \sqrt{\left(m_L - m_R\right)^2 + 4m_D^2} \right)$$
(2.21)

The See-Saw mechanism $m_L = 0$ and $m_D \ll m_R$, so that the two mass eigenstates become,

$$m_+ \approx m_R \text{ and } m_- \approx \frac{m_D^2}{m_R}$$
 (2.22)

and the mixing angle

$$\tan(2\theta) = \frac{2m_D}{m_R - m_L} \tag{2.23}$$

The See-Saw mechanism predicts the existence of a heavy GUT scale sterile neutrino, which has a mass of m_R and a light neutrino of mass $\frac{m_D^2}{m_R}$. The heavy sterile neutrino is almost entirely composed of the ν_R field explaining why it is unobserved whereas the light neutrino is almost entirely composed of the ν_L field, corresponding to the observed left handed neutrino. The type 1 See-Saw mechanism introduces one heavy sterile neutrino for each of the neutrino flavours, independent of an extremely low Yukawa coupling and could potentially explain the minute mass of the neutrino and its partiality for left handedness at current observable energies. The right handed GUT scale neutrino may also provide further insight into matter-anti matter asymmetries, CP violation and beyond standard model Grand Unification Theories if neutrinos are found to be Majorana particles.

Only looking at type 1

2.5 Neutrino Mass Constraints

The four main types of experiments used for extracting constraints on the neutrino mass are oscillation, Tritium beta decay cosmology models and finally neutrinoless double beta decay $(0\nu\beta\beta)$.

***** complete *** Neutrino experiments have provided constraints on the

KAtrin experiment mass limit for ν_e

Oscillation paramters already discussed and shown in figure 1, get mass squared differences

2.5.1 Beta Decay

Tritium undergoes beta decay into Helium,

$${}^{3}\mathrm{H} \rightarrow {}^{3}\mathrm{He} + \mathrm{e}^{-} + \bar{\nu_{e}}$$

$$(2.24)$$

with a decay energy of 18.6 KeV. The energy of the electron follows a beta decay spectrum as shown in figure *** ref. The ν_e emitted during the decay reduces the energy of the beta electron, lowering the endpoint of the electron energy spectrum.

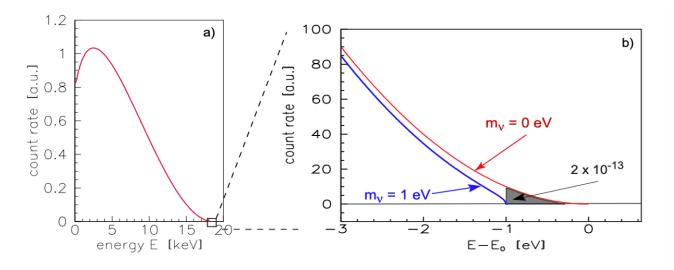


Figure 2.3: BetaSpectrum [11]

By measuring the energy loss of the beta electron with a massive and massless neutrino, the average of the neutrino mass weighted by the mass state coupling to ν_e ,

$$\langle m_{\beta} \rangle = \sqrt{\sum_{i} |U_{ei}|^2 m_i^2} \tag{2.25}$$

As the beta decay energy of tritium is of low energy, the endpoint is more sensitive to $\langle m_\beta \rangle$ shifts in the beta electron spectrum, making it a particularly good decay for probing the electron neutrino mass especially considering the simplicity of the decay. The Karlsruhe Tritium Neutrino (KATRIN) experiment currently holds the best upper limit on the mass of the electron neutrino, at $\langle m_\beta \rangle < 1.1$ eV (at 90% CL)[12], an improvement on the previous upper limit of $\langle m_\beta \rangle < 2$ eV (at 95% CL) [13]. The KATRIN experiment is expected to improve the sensitivity on m_ν by an order of magnitude, to roughly 0.2 eV (at 90% CL), in the next couple of years [12].

*** find way to talk/reference this ***

***advantage of tritium? ***

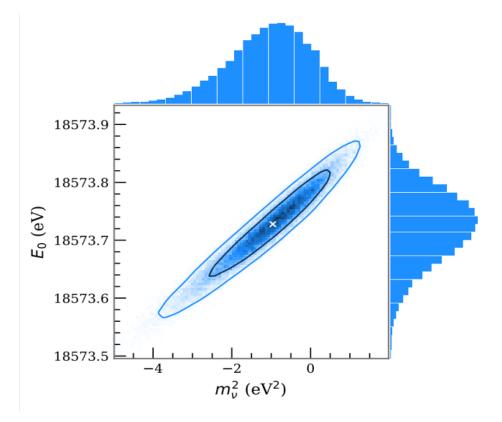


Figure 2.4: msquared [12]

2.5.2 Cosmological Constraints

Cosmological observations can yield limits on the sum of the neutrino masses, by combining a number of cosmological observables. Neutrinos played a significant role in the structure and development of the early universe and the influence of neutrinos can be measured using a number of different tools, including, baryonic acoustic oscillation in the cosmic microwave background (CMB), CMB temperature anisotropy and large scale structure formation. Using the minimal $\Lambda \text{CDM} +$ Σm_{ν} , with the most up to date CMB data, the 95% confidence limit for the Σm_{ν} bounds are $\Sigma m_{\nu} < 0.12 \text{ eV}, \Sigma m_{\nu} < 0.15 \text{ MeV}$ and $\Sigma m_{\nu} < 0.17 \text{ MeV}$ for the degenerate, normal and inverted hierarchies respectively [14]. Additionally, the normal hierarchy is mildly preferred to the inverted hierarchy.

The constraints calculated using cosmological data are very dependent on the model used.

results depend on model ***

*** CMB picture ***

2.5.3 Neutrinoless Double Beta Decay

If neutrinoless double beta decay is observed and the neutrino shown to be a Majorana particle, the decay could be used to determine the absolute mass of the Majorana neutrino. Using the light neutrino exchange mechanism ***discussed ref*** discussed in section***, the effective mass of the Majorana neutrino is,

$$\langle m_{\beta\beta} \rangle = \left| \sum_{i} U_{ei}^2 m_i \right| \tag{2.26}$$

The effective mass of the Majorana neutrino $(\langle m_{\beta\beta} \rangle)$ provides a constraint on the limits for the mass of the lightest mass eigenstate dependant upon the correct mass hierarchy. The current best limit on the effective Majorana neutrino mass comes from the KamLAND-Zen experiment [15]. For neutrinoless double beta decay mediated by light neutrino exchange, the upper limit for $\langle m_{\beta\beta} \rangle$, derived from the decay half-life, was measured as 61 - 165 meV, shown in figure 2.5, alongside the normal and inverted hierarchy regions for $\langle m_{\beta\beta} \rangle$ vs $m_{lightest}$ [15]. The upper limit is given as a range to reflect the uncertainty on the nuclear matrix element calculations.

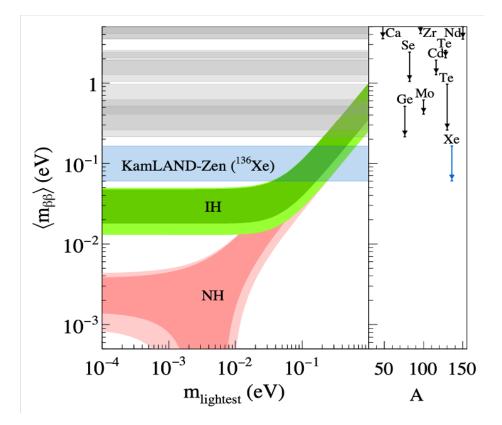


Figure 2.5: HierarchyLimit

An upper limit of 61 - 165 meV almost completely negates the possibility of the effective neutrino mass being found in the quasi-degenerate region, which combines predictions from the normal and inverted hierarchy. Next generation $0\nu\beta\beta$ experiments are expected to reduce this upper limit in order to validate or deny the presence of the effective neutrino mass in the inverted hierarchy region. Limits on the effective Majorana neutrino mass only hold true if the neutrino is in fact a Majorana particle. If no evidence for $0\nu\beta\beta$ is found, the limits for observing the decay and identifying neutrinos as Majorana particles becomes more stringent. Neutrinoless double beta decay experiments aim to answer the ongoing question of whether neutrinos are Dirac or Majorana particles. Observations of neutrino oscillation already proved that neutrinos are not massless as currently described in the Standard Model and so the current role of neutrino experiments are to identify the absolute masses of the different neutrino flavour and mass eigenstates whilst attempting to decipher if neutrinos are Majorana particles that fulfil the requirement of being their own antiparticle.

discussed in section ***red ***,

2.6 Beta Decay

Beta decay is a type of radioactive nuclear decay, in which a atomic nucleus undergoes a transmutation from one element into another with the emission of a beta particle alongside a corresponding neutrino, conserving both Baryon and Lepton numbers. Beta decay is a weak force, charged current interaction, mediated by a W^{\pm} boson. Three different beta decays are commonly observed, β^{-} decay, β^{+} decay and electron capture, resulting in the emission of either a neutrino or antineutrino. β^{-} decay occurs when a neutron decays into a proton, producing an electron and lepton number conserving antineutrino,

$$n \to p + e^- + \overline{\nu_e} \tag{2.27}$$

 β^+ decay occurs with the decay of a proton into a neutron, emitting a positron and neutrino,

$$p \to n + e^+ + \nu_e \tag{2.28}$$

and finally, electron capture occurs when an electron is captured by an atomic proton, which decays into a neutron, similar to β^+ except with the emission of a sole neutrino.

$$p + e^- \to n + \nu_e \tag{2.29}$$

For β^{\pm} decays to occur, the daughter nuclei must have a lower energy than the decaying nuclei, with the energy difference used to create the emitted particles. Moreover, the energy difference must exceed the rest mass energy of the charged lepton and neutrino, with the additional energy providing the particles kinetic energy. Knowing the decay energy of a beta decaying isotope and

measuring the energy of the beta electron provides the energy of the neutrino without directly measuring it. The decay energy is extracted using the mass of the parent and daughter nuclei, which are calculated using the Semi-Empirical Mass Formula (SEMF). The SEMF estimates the mass of an atomic nucleus given the atomic and molecular numbers, in order to determine if the daughter nuclei has a lower energy than the parent, making the decay energetically possible.

The semi-empirical mass formula takes the form,

$$m = Zm_p + (A - Z)m_n - a_V A + a_s A^{2/3} + a_c \frac{Z^2}{A^{1/3}} + a_A \frac{(A - 2Z)^2}{A} + \delta(A, Z)$$
(2.30)

where,

$$\delta(A, Z) = \begin{cases} \frac{a_p}{A^{1/2}} & N \text{ even } (A \text{ even}) \\ 0 & A \text{ odd} \\ \frac{-a_p}{A^{1/2}} & N \text{ odd } (A \text{ even}) \end{cases}$$
(2.31)

and m is the mass of the nucleus, A the mass number and Z the atomic number. From left to right, terms one and two approximate the mass of the individual nucleons inside the atom. The remaining terms describe the corrections to the mass, from volume, surface, Coulombic, neutron/proton asymmetry and nucleus spin coupling. In an attempt to describe the energetically viable beta decays, the atomic number Z is plotted below, for a fixed even mass number A,

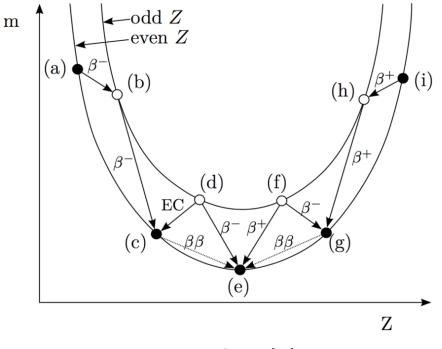


Figure 2.6: SEMF [16]

For an odd value of A, there is only one curve for Z, however, as shown in figure 2.6, for an even value of A, there are two curves, separated by the $\delta(A, Z)$ term described in equation 2.31. The possible β^{\pm} transitions between the even and odd Z curves are shown by the arrows in figure 2.6.

2.7 Two Neutrino Double Beta Decay $(2\nu\beta\beta)$

As shown in section 2.6, equation 2.30 can be used to determine the mass of a nuclei and whether a particular decay is energetically permitted. For an isotope that is unable to decay directly via beta decay, such as isotope (c) in figure 2.6, it is possible for them to decay via double beta decay. During double beta decay, two neutrons simultaneously undergo β^- decay, resulting in the emission of two electrons and two corresponding electron neutrinos for the two neutrino variation of double beta decay,

$$(A, Z) \to (A, Z+2) + 2e^- + 2\bar{\nu_e}$$
 (2.32)

Double beta decay was first proposed by M. Goeppert-Mayer in 1935 [17] and has been observed in a number of isotopes that have their regular beta decay rate suppressed or forbidden. Like single beta decay, the two emitted electrons lead to a continuous energy spectrum that has an end point at the decay energy $Q^{\beta\beta}$. $2\nu\beta\beta$ has been measured for isotopes including ⁸²Se, ¹⁰⁰Mo and ¹³⁶Xe and is currently a possible decay for 35 different isotopes. Of the measured double beta decaying isotopes, the NEMO-3 experiment studied 7 [18], including ⁸²Se which is the isotope of choice for the SuperNEMO experiment. The reasons for which ⁸²Se was chosen as the source for SuperNEMO will be discussed further in chapter 3.

 $2\nu\beta\beta$ is a second order weak interaction that is allowed in the Standard Model, but is extremely rare, with a measured half-life of the order 10^{20} years. The Feynman diagram of the decay is shown in figure 2.7,

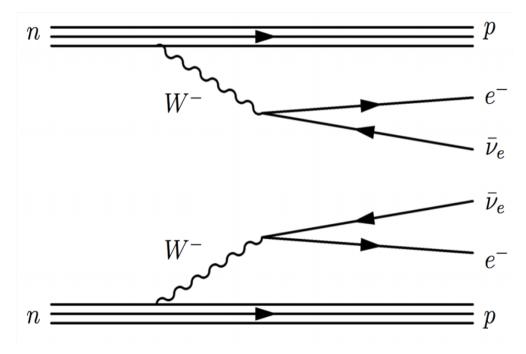


Figure 2.7: 2vFeynman [16]

From [19], the half-life $\left(T_{1/2}^{2\nu}\right)^{-1}$ of the decay is related to the phase space factor $G^{2\nu}\left(Q_{\beta\beta},Z\right)$ and the nuclear matrix element $M^{2\nu}$ as,

$$\left(T_{1/2}^{2\nu}\right)^{-1} = G^{2\nu} \left(Q_{\beta\beta}, Z\right) \left|M^{2\nu}\right|^2 \tag{2.33}$$

 $G^{2\nu}$ is a four body phase space factor that is calculated analytically and $M^{2\nu}$ represents the transition probability from the initial to the final state of the decay. Measuring double beta decaying isotopes reduces the uncertainties on the values of $M^{2\nu}$ improving the precision of the calculated half-life and phase space factors.

2.8 Neutrinoless Double Beta Decay $(0\nu\beta\beta)$

***eegy spectrum 0 vs 2v.

Neutrinoless double beta decay is the neutrinoless analogue of the double beta decay presented in the previous section and is a hypothesised decay which if observed would demonstrate that the neutrino is a Majorana particle [20]. $0\nu\beta\beta$ was first proposed by W.H. Furry in 1939 [21], as an alternative to the two neutrino decay making the decay a possibility for all double beta decaying isotopes. During neutrinoless double beta decay, two beta electrons are simultaneously emitted, however unlike the two neutrino decay, no antineutrinos are emitted and all the decay energy is carried by the two electrons,

$$(A, Z) \to (A, Z+2) + 2e^{-}$$
 (2.34)

Without emitting the two associated antineutrinos, $0\nu\beta\beta$ violates lepton number conservation and is therefore a forbidden standard model interaction. The hypothesised mechanisms through which the neutrinoless decay is thought to occur include light neutrino exchange (neutrino mass mechanism), right handed current, Majoron emission and the more exotic R-parity violating supersymmetry, extra dimensions and squark mixing. If $0\nu\beta\beta$ is observed, light neutrino exchange is the most natural and expected method of decay as it most closely resembles the current Standard Model decay. Figure 2.8 illustrates neutrinoless double beta decay via light neutrino exchange, where a right handed antineutrino emitted from one W boson is absorbed as a left handed neutrino, if neutrinos are Majorana particles. ***not mention exotic decays***

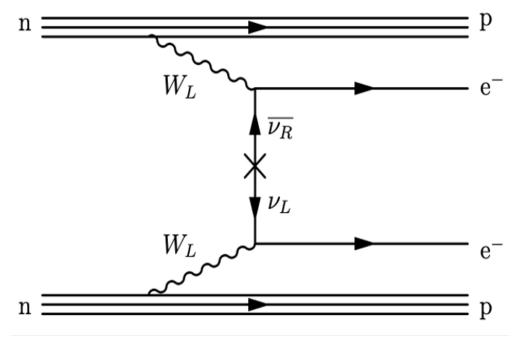


Figure 2.8: 0vFeynman [16]

The light neutrino exchange mechanism in figure 2.8 clearly illustrates the Majorana nature of neutrinos however, amongst the other $0\nu\beta\beta$ mechanisms, neutrinos are often not involved making

conclusions regarding the nature of the neutrino less obvious. In 1980, Schechter and Valle [22] illustrated that for any $0\nu\beta\beta$ decay, regardless of the beyond Standard Model intermediary process, neutrinos are Majorana even though they are not directly involved in the decay. The $0\nu\beta\beta$ mechanism can therefore be replaced with a 'Black Box' that is independent of the decay mechanism as shown in figure 2.9.

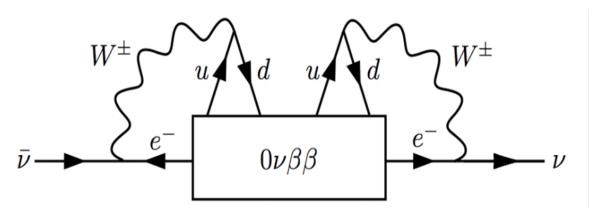


Figure 2.9: BlackBox [22]

For $0\nu\beta\beta$ decay, the decay rate takes the form,

$$\left(T_{1/2}^{0\nu}\right)^{-1} = G^{0\nu} \left(Q_{\beta\beta}, Z\right) \left| M^{0\nu} \right|^2 \eta_{LV}^2$$
(2.35)

where $G^{0\nu}$ is the two particle phase space factor, $M^{0\nu}$ the nuclear matrix element for the neutrinoless decay transmission and η_{LV} the lepton number violating parameter that is unique to each of the decay mechanisms. Light neutrino exchange, right handed current and Majoron emission will be briefly discussed in the following sections, focusing on the relationship between the decay mechanism and the corresponding decay rate.

2.8.1 Light Neutrino Exchange

As mentioned, light neutrino exchange is the proposed interaction that most closely resembles a current Standard Model interaction, shown in figure 2.8. The decay rate for this interaction is,

$$\left(T_{1/2}^{0\nu}\right)^{-1} = G^{0\nu} \left(Q_{\beta\beta}, Z\right) \left| M^{0\nu} \right|^2 \left< m_{\beta\beta} \right>^2$$
(2.36)

where the lepton number violating parameter in equation 2.35, is replaced by the effective Majorana mass $\langle m_{\beta\beta} \rangle$. $\langle m_{\beta\beta} \rangle$ is defines as,

$$\langle m_{\beta\beta} \rangle = \left| \sum_{i} U_{ei}^2 m_i \right| \tag{2.37}$$

and for three light active neutrinos with mass m_i , ***wording***

$$= \left|\cos^{2}\theta_{13}\left(m_{1}\cos^{2}\theta_{12} + m_{2}e^{i\alpha_{1}}\sin^{2}\theta_{12}\right) + m_{3}e^{i(\alpha_{2}-2\delta)}\sin^{2}\theta_{13}\right|$$
(2.38)

using the PMNS matrix shown in equation 2.3 and the Majorana phases in equation 2.4. From equation 2.38, the decay rate of the light neutrino exchange is sensitive to the absolute scale of the neutrino mass eigenstates.

*** add more ***

2.8.2 Majoron Emission

*** talk about B-L *** the difference between the baryon and lepton numbers

Standard Model extensions have the orized the violation of B - L, resulting in the manifestation of a Goldstone Boson or Majoron, which could mediate neutrinoless double beta decay. $0\nu\beta\beta$ mediated by a single Majoron can be expressed as,

$$(A, Z) \to (A, Z+2) + 2e^{-} + \chi^{0}$$
 (2.39)

where χ^0 is the emitted Majoron. The decay rate for the interaction is given by,

$$\left(T_{1/2}^{0\nu\chi^{0}}\right)^{-1} = G^{0\nu\chi^{0}}\left(Q_{\beta\beta}, Z\right) \left| M^{0\nu\chi^{0}} \right|^{2} \left\langle g_{\chi^{0}} \right\rangle^{2}$$
(2.40)

where $G^{0\nu\chi^0} M^{0\nu\chi^0}$ are as previously defined, and the lepton number violating parameter in equation 2.35 is exchanged for $\langle g_{\chi^0} \rangle$ which represents the coupling between the Majoron and the neutrino. The Feynman diagram of the decay is shown below,

The measured total electron energy of the decay can be used to infer the Majoron emitting decay mechanism, however with the addition of emitted particles other than the electron, the energy takes on a continuous spectra similar to that observed with $2\nu\beta\beta$ ***ref plot woth 0/2v energy. The shape of the total electron energy spectra is dependent upon the Majoron model used during the decay, which can include up to two different Majorons as shown in figure ??

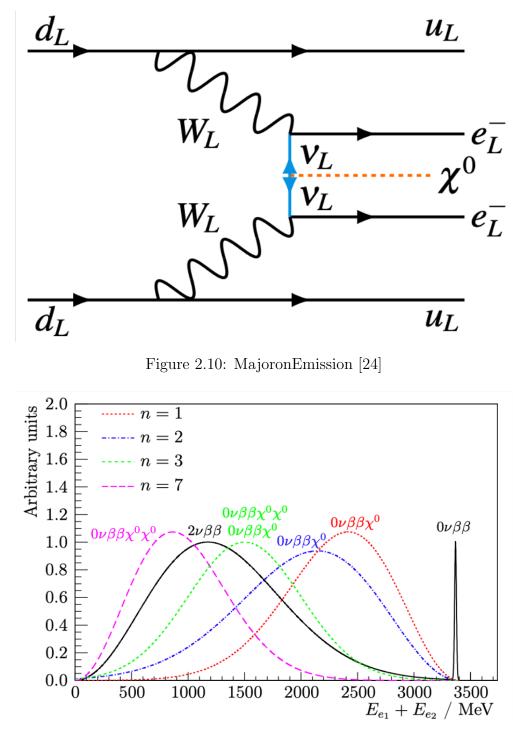


Figure 2.11: MajoronEnergies [25]

2.8.3 Right Handed Current

Currently, the weak interaction is only propagated by a left handed W boson, however by proposing a right handed component of the weak force, a right handed gauge boson, may mediate a neutrinoless double beta decay with only right handed neutrinos. The hypothesized right handed gauge boson may be related to the W or Z bosons as a mixture of multiple boson states or could manifest as an entirely novel gauge boson. A Feynman diagram of $0\nu\beta\beta$ mediated by a right a right handed W boson and right handed neutrino is shown in figure 2.12 below,

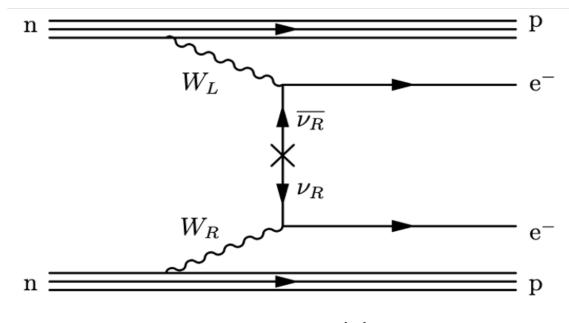


Figure 2.12: 0vRH [23]

In figure 2.12, $0\nu\beta\beta$ is mediated by a right handed W boson and right handed neutrino which is a Majorana particle. The alternative decay kinematics may be probed by investigating opening angle and energy distributions as shown in figure 2.13, which highlights the difference in the distributions with changing decay mechanisms. The

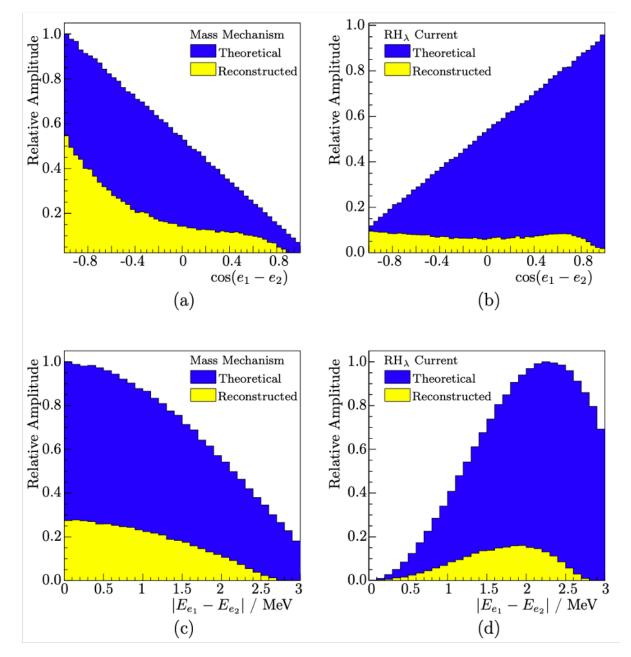


Figure 2.13: RHCurrents [26]

2.9 Nuclear Matrix Elements

Nuclear Matrix Elements (NMEs) are a key components for investigating double beta decay as shown in equation 2.35, where using both the NMEs and the measurable decay rate, the absolute neutrino mass $\langle m_{\beta\beta} \rangle$ can be probed for a particular decay mechanism such as light neutrino exchange shown in equation 2.36. By improving the precision of the NMEs calculations, improved limits can be determined for the absolute neutrino mass during double beta decay searches. In order to calculate the NMEs, nuclear structure theory is necessary, beginning with a many body Hamiltonian, which describes the interactions between nucleons. NME calculations are further complicated as the entire range of energy states for the decaying nuclei must be considered and their respective contributions to the transition rate determined to a high degree of accuracy. 5 different approximations [27] for calculating the NMEs will be discussed in the remainder of the section and the level of uncertainly with each model will be presented as a function of the decaying isotope ***ref figure ***

- Interacting Shell Model (ISM) [28]: The interacting shell model considers a small number of nuclear orbitals that are closest to the Fermi level, but within each of the lower orbitals, the nucleons behave independently in a self imposed mean field. ISM accurately describes the the interactions between the limited number of nucleons and therefore the model predicts smaller nuclei such as ⁸²Se more accurately. Additionally, as only a few of the orbital shells are considered, the approximations made by the ISM are often on the lower end.
- Quasiparticle Random Phase Approximation (QRPA) [29]: Unlike the ISM, QRPA uses a greater number of different orbitals to calculate the NMEs, however the complexity of the nucleon interactions is reduced to compensate for this. Incorporating an increased number of nuclear orbitals increases the precision of QRPA for larger nuclei. For the purpose of calculating the NMEs, QRPA considers the initial and final states via a number of virtual intermediary states. The proton-proton interaction parameter g_{pp} can be constrained experimentally by measuring the decay rate of the two neutrino decay reducing the uncertainty of the model for $2\nu\beta\beta$, although the reduced uncertainty may not translate directly to the neutrinoless decay.
- Interaction Boson Model (IBM) [30]: The IBM is similar to the shell model approximation but denotes pairs of nucleons as single bosons with angular momentum of either 0 or 2. The advantages of the IBM are similar to that of the ISM however, similarly for large nuclei the uncertainty on the calculations increases.
- Projected Hartree-Fock Bogoliubov (PHFB) [31]: PHFB calculates the transition probability using the nuclear wave functions for neutron pairs with even values of angular moment and positive parity such as 0⁺/2⁺/4⁺. PHFB includes only quadrupole interactions with fewer model dependent parameters compared to the previous approximations.
- Energy Density Functional (EDF) [32]: The EDF method improves on the simple PHFB method by including the Gogny interaction for nucleons [33].

The different models are used to compute the NMEs of several double beta decaying isotopes, by firstly calculating the NMEs of β^{\pm} decay as well as the two neutrino DBD and then estimating the values for $0\nu\beta\beta$ based off the previous measurements, taking into account the different intermediate states of the neutrinoless decay. The results for 11 double beta decay isotopes, using the five NME estimation models described above, are shown in figure 2.14. As mentioned, the different models produce different values for the NMEs and because of this there is a large uncertainty, up to an order of magnitude, between the estimated neutrinoless double beta decay half-lifes.

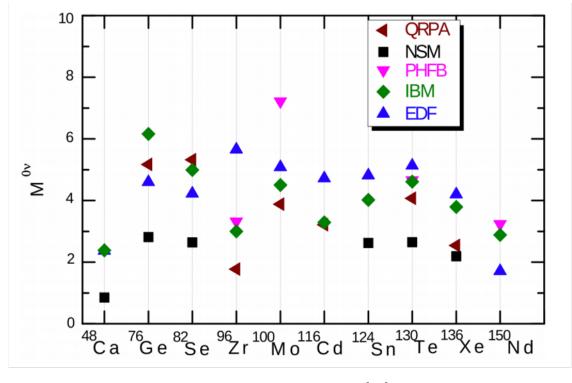


Figure 2.14: NMEValues [34]

2.10 Open Questions on the Nature of Neutrinos

2.10.1 Single and Higher State Dominance

Chapter 3

The SuperNEMO Demonstrator

SuperNEMO is the successor to the NEMO-3 experiment [35] which ran from 2003-2011 collecting data for the following double beta decaying isotopes, ¹⁰⁰Mo, ⁸²Se, ¹³⁰Te, ¹¹⁶Cd, ¹⁵⁰Nd, ⁹⁶Zr and ⁴⁸Ca. Unlike NEMO-3 however, SuperNEMO will focus solely on the isotope ⁸²Se. SuperNEMO is located in the underground laboratory, Laboratoire Souterrain de Modane (LSM), within the Frejuis road tunnel linking Modane to Bardonnecchia. The underground location helps to protect the detector from cosmic radiation and further protection comes in the form of an anti radon tent as well as iron and water shielding, which reduces the impact of the natural radiation found in the surrounding rock.

NEMO-3 used a cylindrical design, divided into 20 equal sections of isotopic source material whereas SuperNEMO demonstrator uses a modular structure, with the thin source foils located at the centre of the detector, surrounded by the tracker and calorimeters as shown in figure 3.1. The source foils consist of over 6 Kg of the double beta decaying ⁸²Se and hopes to achieve a sensitivity of $T_{1/2}^{0\nu} > 6.5 \times 10^{24}$ years, which corresponds to an effective neutrino mass $\langle m_{\nu} \rangle < (260$ - 500) meV, following 6.19 Kg × 2.5 years of exposure [36]. During detector operation, a magnetic field is expected to be applied to the tracker volume for the purpose of identifying the charge of a particle passing through the detector. However, prior to activating the magnetic coil, the influence of different magnetic field configurations will be investigated in this thesis to determine the optimum magnetic field choice for the detectors operational lifetime.

The following chapter will describe the structure of the SuperNEMO detector, the current progress of the detector commissioning, the main backgrounds for the ⁸²Se $0\nu\beta\beta$ search and finally the role of the magnetic field within the detector and the formation of the realistic field, which presents the expected shape and strength of the magnetic field that is expected during detector operation.

3.1 The SuperNEMO Demonstrator Design

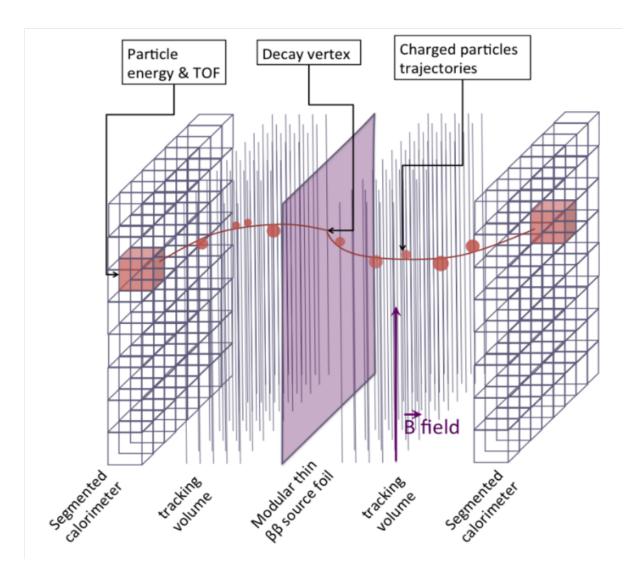


Figure 3.1: DemonsDetector

Unlike other double beta decay experiments, SuperNEMO uses a source-tracker-calorimeter structure allowing both the particle energy and the associated trajectory to be determined. The structure of the detector is shown in figure 3.1 and provides multiple advantages compared to other double beta decay experiments including,

- Record particle trajectories in three spatial dimensions.
- Being able to identify and differentiate particles such as the electron, positron, photon and alpha particle. Furthermore it is possible for SuperNEMO to identify muons that may cross the detector.

- Probing a variety of decay channels, primarily the two electron channel for double beta decay as well as the $1e1\alpha$ channel for BiPo measurements or other background decay channels.
- Measuring the energies of single electrons as well as the opening angles of double beta candidate events.
- Can be easily scaled to increase the exposure of ⁸²Se or perhaps investigate other double beta decaying isotopes.

However there are also a number of disadvantages as a result of the detector design including,

- Low source mass, limited by the thickness of the source foil. If the source foil is too thick it will inhibit the emission of electrons from inside the foil reducing the detection efficiency.
- Lower detection efficiency (section 4.4) and energy resolution compared to germanium and bolometer experiments.

3.1.1 Source Foil

As mentioned, the SuperNEMO detector uses a modular source-tracker-calorimeter with the use of a passive source, that is, a source that is not part of detection, unlike many other double beta decay experiments ***ref**. The modular structure allows for both the particle energy and trajectory through the tracker volume to be reconstructed, providing the ability to identify a particles topology and kinematics. This is particularly important for identifying particular backgrounds that can mimic double beta decays, but also provides information for single electrons which can be used to infer the underlying mechanism of the decay.

The source foil is located at the centre of the detector, surrounded by the tracker volume and finally the calorimeters. The source foil is a thin, mechanically processed foil, that is enriched in ⁸²Se. The narrowness of the foil allows for improved emission of charged particles from the source foil and into the tracker chamber. In total the source foil mass was measured to be approximately 6.19 Kg of enriched ⁸²Se, whilst being approximately 2.7m in length. The SuperNEMO demonstrator structure allows for the source foil to be easily replaced or changed, whilst additionally allowing for easy scaling of the detector size, with the final SuperNEMO detector expected to combine 20 of the unique demonstrator modules, increasing the exposure 20 fold. The figure below provides the physics goals for the current demonstrator as well as the proposed full SuperNEMO detector [37].

	Full SuperNEMO	Demonstrator module	
Source mass	100 kg	7 kg	
Energy resolution	4% at 3 MeV (FWHM)		
²²² Rn in tracker volume	$< 0.15 \text{ mBq/m}^3$		
²⁰⁸ Tl in source foil	$<2 \mu\mathrm{Bq/kg}$		
²¹⁴ Bi in source foil	$< 10 \ \mu Bq/kg$		
Sensitivity to $0\nu\beta\beta$ half life	>10 ²⁶ yr	$> 6.6 \times 10^{25} \text{ yr}$	
Sensitivity to $\langle m_{\beta\beta} \rangle$	<40-100 meV	<200-400 meV	

Figure 3.2: FullDetector [37]

⁸²Se was selected as the isotope of choice for the SuperNEMO demonstrator, amongst the isotopes used in the NEMO-3 detector because of its relatively high decay energy (≈ 3 MeV), reasonable $2\nu\beta\beta$ half-life, high natural abundance, ease of enrichment and reasonable phase space factor $G_{0\nu}$. The low decay energy removes a large amount of the low energy backgrounds whilst the remaining factors ensure the availability of ⁸²Se with a frequent number of decays. The properties of the isotopes used in NEMO-3 are shown in figure 3.3 below,

Isotope	$Q_{\beta\beta}$ (MeV)	$G_{0\nu} (10^{-15} y^{-1})$	$T_{1/2}^{2 u}$ (y)	η (%)
⁴⁸ Ca	4.273	24.81	$6.37^{+0.56}_{-0.69} {}^{+1.21}_{-0.89} 10^{19}$ (NEMO-3)	0.187
⁷⁶ Ge	2.039	2.363	$1.926 \pm 0.094 \ 10^{21}$ (GERDA)	7.8
⁸² Se	2.995	10.16	$9.6 \pm 0.3 \pm 1.0 \ 10^{19}$ (NEMO-3)	9.2
⁹⁶ Zr	3.350	20.58	$2.35 \pm 0.14 \pm 0.16 \ 10^{19}$ (NEMO-3)	2.8
¹⁰⁰ Mo	3.035	15.92	$6.93 \pm 0.04 \ 10^{18}$ (NEMO-3)	9.6
¹¹⁶ Cd	2.809	16.70	$2.8 \pm 0.1 \pm 0.3 \ 10^{19}$ (NEMO-3)	7.6
¹³⁰ Te	2.530	14.22	$6.9 \pm 0.9 \ 10^{20}$ (NEMO-3)	34.5
¹³⁶ Xe	2.458	14.58	$2.165 \pm 0.016 \pm 0.059 \ 10^{21}$ (EXO-200)	8.9
¹⁵⁰ Nd	3.367	63.03	$9.11_{-0.22}^{+0.25} \pm 0.63 \ 10^{18}$ (NEMO-3)	5.6

Figure 3.3: Isotope Properties

The method used to produce the source foil was takes from NEMO-3 and involved mixing ⁸²Se powder with PVA, which acts as a binding agent. The mixture of ⁸²Se and PVA was sandwiched between two layer of 12μ m thick Mylar [38]. In total, 34 ⁸²Se have been produced, with 18 produced using NEMO-3 processing methods. The surface density of the source foils is between 40 and 60 mg/cm² and a thickness of 0.3 mm. Alongside the 34 ⁸²Se source foils, two ultra pure copper foils were produced and mounted either side of the source foils for the purpose of calibration and measuring certain backgrounds.

3.1.2 Tracker

In order to track the trajectories of the charged particles propagating from the source foil, each side of the surrounding tracker chamber comprises of 113 columns of nine drift cells, totalling 2034 cells for both sides of the tracker. Each tracker cell is 3m long with a diameter of roughly 4cm (figure 3.4). Each cell contains a central anode wire which is run at a high voltage, surrounded by eight grounded field shaping wires and two ring shaped copper cathodes at on either end of the cell. Unlike NEMO-3 which had a rounded tracker volume, the SuperNEMO tracker is planar to the source foil increasing the coverage of the calorimeters surrounding the tracker.

The tracker volume is filled with gas, a mixture of He (95%), ethyl alcohol (4%) and Ar (1%). As charged particles enter the tracker chamber they ionize the gas and the time taken for the ionized electron shower to drift towards the anode infers the distance of the charged particle from the centre

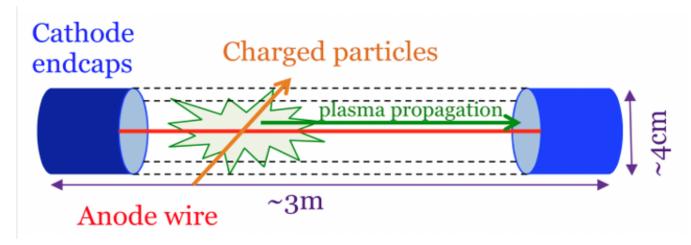


Figure 3.4: TrackerCells

of the cell. Tracker cells are run in Geiger mode, shown in figure 3.5, so that when an ionization occurs from a passing charged particle, the high electric potential in the tracker cell accelerates the freed electrons, further ionizing the gas, producing an avalanche.

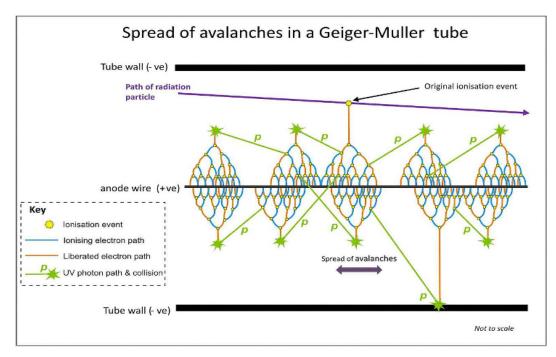


Figure 3.5: GeigerMechanismtrum [39]

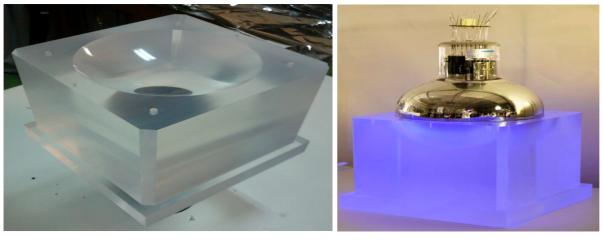
Additionally, the two cathode end caps measure how far along the the tracker cell the charged particle was when generating the electronic shower. The combination of these two mechanisms allows the trajectory of the particle to be determined in three dimensions.

3.1.3 Calorimeter

The final component of the SuperNEMO demonstrator module structure is the calorimeter wall, which surrounds each side of the tracker. There are a total of six calorimeter walls for SuperNEMO, two of each of the following; Main wall, X wall and the Gamma Veto or Veto wall. Each wall is comprised of a different number of optical modules (OM) with the corresponding PMT size,

- Main wall: 220 8" calorimeters and 40 5" calorimeters.
- X wall: 64 5" calorimeters.
- Veto wall: 32 5" calorimeters.

totalling 712 OMs. Each OM comprises of a plastic scintillator, shown in figure 3.6a and a Hammatsu PMT. The plastic scintillator is made of POPOP (1,4-di-(5-phenyl-2-oxazoly)benzene) doped polystyrene, which acts as a wavelength shifter and PTP (para-terphenyl) which increases the light yield during ionization. When an incident particle strikes the plastic scintillator block, it loses energy from multiple scatterings, resulting in a number of photons being emitted proportional to the incident particle energy. Scintillator blocks are wrapped in both aluminised mylar to increase light collection and protect against UV radiation from the tracker or adjacent OMs and teflon to increase photon collection efficiency. Hamamatsu PMTs were recycled from NEMO-3 for use in SuperNEMO and come in two sizes, 8" and 5". The 8" calorimeters provide improved energy resolution and thus are mostly confined to the Main wall. By carving the plastic scintillators, the PMT bulbs can be coupled to them using radiopure glue, combined to form the OM shown in figure 3.6b. Directly coupling the PMT and scintillator allows for the light guides to be removed (as used in NEMO-3), improving the energy resolution of the OM.



(a) ScintCurve

(b) OM

The 8" PMTs coupled directly to the plastic scintillators results in an increases energy resolution compared to NEMO-3, with the energy resolution of the Main wall OMs being roughly 8.3% FWHM

at 1 MeV. The timing resolution at the same energy is close to 400ps, compared to the 25ps resolution for NEMO-3 ***ref ***. Significantly, the absence of the light guide, results in the PMTs being exposed to the magnetic field applied to the tracker volume. Exposure to magnetic flux considerably reduces the performance of the PMTs, so they require magnetic shielding which alters the shape of the applied field. The impact of the shielding will be described in section 3.3.3.

3.1.4 Tracker Construction

3.1.5 Calibration

Multiple calibration methods will be used to determine the energy and time responses of the detector to known sources. To perform energy calibration for SuperNEMO, ²⁰⁷Bi will be deployed within the detector to obtain an absolute energy measurement. ²⁰⁷Bi undergoes a number of internal conversions, resulting in the emission of electron calibration lines with energies of at 482, 976 and 1682 keV, shown in figure 3.7.

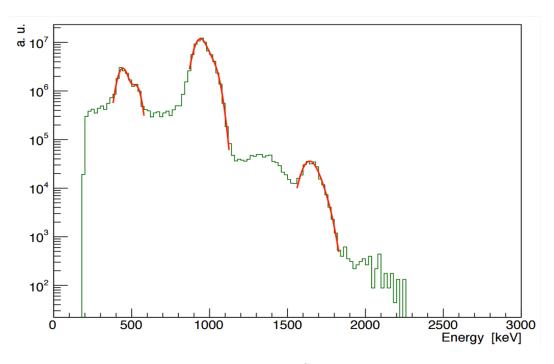


Figure 3.7: 207BiSpectrum

For each source, a droplet of ²⁰⁷Bi in between two layers of mylar will be encapsulated by a radiopure copper frame, following which they will be inserted into the gaps between the source foils via an automatic source deployment system. Calibration is expected to be performed regularly during detector operation to ensure energy measurements are accurate. The ²⁰⁷Bi internal conversions will be reconstructed from the location of the copper frames to the calorimeters for the purpose of

measuring the reconstructed energies and comparing to the true ²⁰⁷Bi internal conversion lines. For neutrinoless double beta decay in the ⁸²Se region of interest (2.8-3.2 MeV), the greatest internal conversion energy of 1682 keV will provide the best degree of calibration at those energies. However, until the tracker has been fully commissioned, the high voltage gain of the PMTs is equalized using the Compton edge of the ²⁰⁸Tl high energy 2.61 MeV photon (section ref^{***}). Doing so reduced the spread of the optical modules gain to less than 10% although this is expected to improve once the ²⁰⁷Bi energy calibration method is online [36].

Alongside the ²⁰⁷Bi deployment close to the source foil, a light injection system (LIS - figure 3.8) will also be deployed to perform both time calibration and measure gain for the optical modules. The light injection system uses pulses of ultraviolet light from light emitting diodes, through optical fibres to illuminate OMs and measure their gain. The length of all fibres will be maintained at 20m to avoid any systematic time differences. ²⁴¹Am is used as a source with a reference OM to monitor and maintain the light level. In total, the LIS will allow any variations in gain from voltage fluctuations be tracked and corrected with a precision of 1% alongside the time calibration.

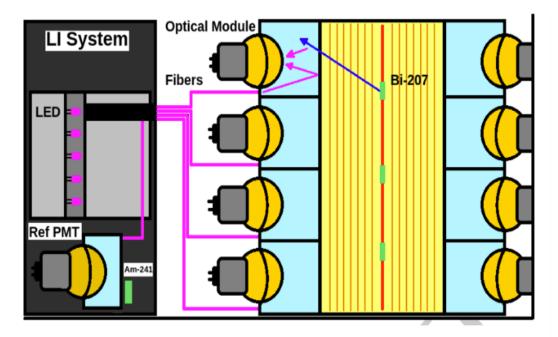


Figure 3.8: LIS

Additional time calibration will be performed using ⁶⁰Co, which produces two photons, the first being of energy 1.17 MeV and the second, 1.33 MeV. The two photons are emitted almost simultaneously ($\Delta t = 0.41$ ps) from the source at a separation much lower than the time resolution of the PMTs. However, by placing the ⁶⁰Co source behind the main wall in one of nine different positions, at known distances from two PMTs, the energies and time separation of the two photons can be measured to determine the offset of the PMTs. The mechanism for measuring the time

resolution using 60 Co is shown in figure 3.9 [36]. Preliminary data has been taken using 60 Co in order to determine the time resolution. Initial results have shown the time resolution to be be <600 ps for photons with energy close to 1 MeV, which is expected to improve once the tracker is fully commissioned and 207 Bi can be used.

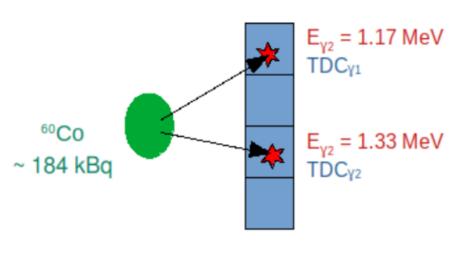


Figure 3.9: Co60 [36]

3.2 Commissioning Progress

3.2.1 Expected Sensitivity

3.3 Backgrounds Sources

The main SuperNEMO background contributions come from natural radioactivity found within the rocks surrounding the LSM, the laboratory itself, detector components and source foil. The majority of the relevant backgrounds come from the decay chains of the long lived radioisotopes ²³²Th and ²³⁸U as shown in figures 3.13 and 3.12 respectively. ²³²Th and ²³⁸U are two naturally occurring backgrounds, found in small amounts within all materials. The decay progeny of ²³²Th and ²³⁸U are high energy electron/photon emitters, which can mimic double beta decays (chapter ??), in the ⁸²Se region of interest (2.8 - 3.2 MeV).

3.3.1 Background Locations

Shielding and the anti radon tnet

The two main SuperNEMO backgrounds are ²⁰⁸Tl and ²¹⁴Bi, which have decay energies of 4.99 and 3.27 MeV respectively. The backgrounds can be discriminated based on their locations within the detector, although backgrounds within the surrounding rocks and outside of the detector are not expected to be problematic as a result of the detector shielding. External neutron backgrounds may also significantly contribute to the neutrinoless double beta decay sensitivity, however they are not considered in this work. The three main background locations are:

- Internal for backgrounds located within the source foil.
- Radon for backgrounds that originate from radon contamination within the tracker volume.
- External for non-radon backgrounds originating outside of the source foil but within the detector components.

To minimize the background levels all materials were screened using the High Purity Germanium (HPGe) detector, which must have a high germanium purity to reduce the backgrounds to the expected levels ***ref. An additional BiPo detector, which has its name derived from the decay of Bismuth to Polonium, was developed in [40], to measure the ²⁰⁸Tl and ²¹⁴Bi levels in thin materials , including the SuperNEMO source foils. The sensitivity of the BIPo detector for measuring the contamination of the SuperNEMO source foils was found to be $<2 \ \mu$ Bq/Kg for ²⁰⁸Tl and $<140 \ \mu$ Bq/Kg for ²¹⁴Bi (90% C.L.) after 6 months of measurements.

mechanisms for HPGe and BiPo

The current BiPo detector BiPo-3, derived from the BiPo prototypes [41], works by detecting the emission of an electron followed by a delayed alpha ($1e1\alpha$ channel), for the BiPo decays of 212 Bi and 214 Bi. 212 Bi is used to determine the 208 Tl contamination as it is the predecessor to 208 Tl and decays into 208 Tl 36% of the time (figure 3.10).

The activity of ²⁰⁸Tl is then calculated by measuring the alpha emission (alpha half-life of 300

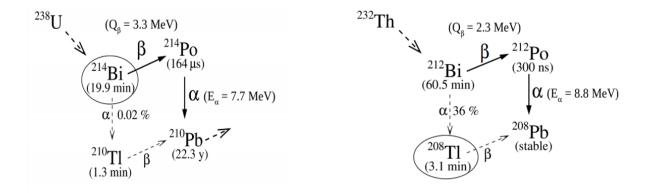


Figure 3.10: CloseDecayScheme [40]

ns) of ²¹²Po which is produced by the remaining 64% of ²¹²Bi decays. ²¹⁴Bi beta decays to ²¹⁴Po, which is also an alpha emitter but with an alpha half-life of 164 μ s. To measure the contamination of the source foils, the foils are placed between two thin ultra radiopure plastic scintillators as shown in figure 3.11, which then detects the beta decays of ²¹²Bi and ²¹⁴Bi as an energy deposition in one scintillator with no coincident signal in the second scintillator. The alphas are then measured as a delayed signal in the second scintillator without a coincident deposition in the first scintillator. The events are labelled as back-to-back events since the beta and alpha particles are detected in the different scintillators on the opposite side of the foil. ₂₁₂Bi and ²¹⁴Bi are differentiated based on the alpha timing and the energy of the alpha is used to determine if the decay originates from the surface or bulk of the source foil.

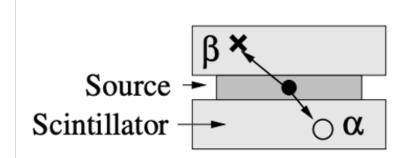


Figure 3.11: BiPoDetector [40]

background activities???*** Targets?

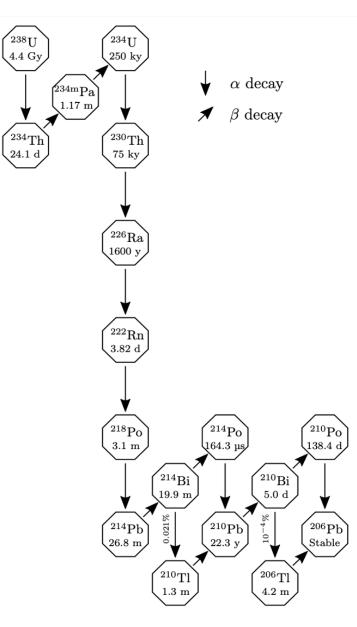


Figure 3.12: Bi214DecayScheme

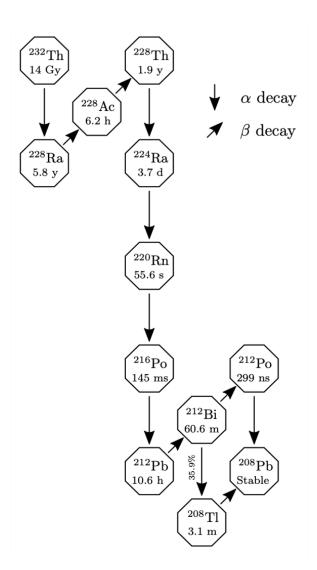


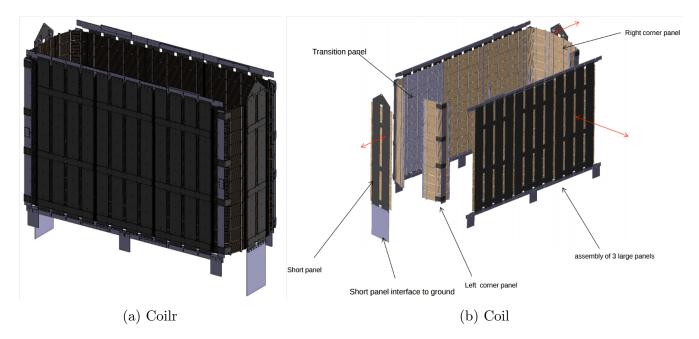
Figure 3.13: Tl208DecayScheme

mention field wire bulk as non radon background but still put with Rn.

3.3.2 Other DBD Experiments

3.3.3 Magnetic Coil and Shielding

The magnetic field for the SuperNEMO detector will be generated by a copper magnetic coil, recycled from old NEMO-3 copper rods. The coil will be built to surround the detector ensuring the magnetic flux is contained within the tracker volume.



The presence of magnetic field inside the glass of a PMT significantly reduces the performance of the PMT even at very low field strengths, figure 3.15

Unlike NEMO-3, SuperNEMO does not use a light guide with the OMs as the PMTs are directly coupled to the plastic scintillators as shown in figure ****ref ***. As a result, the PMTs are exposed to the tracker volume and the potential magnetic flux. To prevent the PMT performance being reduced by the magnetic field, iron shields will be used to protect the PMTs and remove any magnetic field from within their volume.

Furthermore, it is expected that the coil will be used to generate a magnetic field of approximately 25 Gauss. However it is possible for the strength of the magnetic field to be adjusted by altering the current inside of the coil. The purpose of the magnetic field applied to the tracker volume is to help determine the charge of any particle propagating through the tracker by measuring the magnetic field induced curvature of the particle. Electrons from ⁸²Se double beta decay are of relatively low energy and so do not require high magnetic field strengths to curve them, however it may be pertinent to use a different field strength if it results in an increase in the detection efficiency of $0\nu\beta\beta$.

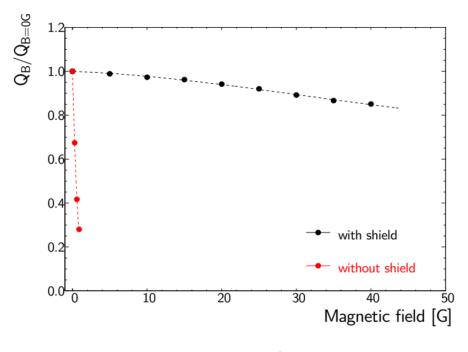


Figure 3.15: A

3.4 Motivation for Magnetic Field Studies

The magnetic field allows electrons and positrons to be differentiated by the directionality of their associated track curvatures. It provides a useful tool for removing significant backgrounds, in particular photons with energy greater or equal to 1.02 MeV, which are capable of pair producing an electron positron pair. Other sources of positrons include rare positron emitting decays however they are seldom observed and not expected to be problematic.

***pair produce/ show electron curvature ***

Photon flux inside the detector is extremely high as illustrated by table *** table of photon flux for different sources*** so positron identification is a priority. However it may be possible to use the detector without a magnetic field. Removing or reducing the strength of the magnetic field may increase the number of expected background events, however it may also increase the signal reconstruction efficiency, resulting in a net gain in sensitivity. By reducing the positron generating backgrounds by other means, it may be possible to increase the signal efficiency without significantly increasing the background that comes with having a reduced or no field.

Initially, three magnetic field configurations were selected, including the uniform field, no field and the realistic field. The uniform field is defined as having a nominal 25 Gauss field, with uniform strength and shape throughout every part of the detector. No field is characterised by having no magnetic field (0 Gauss) throughout the detector and corresponds to having the magnetic field turned off. The realistic field is a mathematically computed field, representing the shape and strength of the field we expect to see during operation with a nominal 25 Gauss applied via a magnetic coil.

By comparing the detection efficiency of the three magnetic field configurations, a decision can be made as to when or if activating the magnetic field will increase our sensitivity to ⁸²Se neutrinoless double beta decay. Maximising our sensitivity increases the probability of observing the decay, whilst simultaneously improving the precision of nuclear matrix elements and setting better limits on the decay itself.

3.4.1 The Realistic Field

Unlike NEMO-3, magnetic shields are required for the SuperNEMO demonstrator module as a consequence of the detector geometry exposing the PMTs to magnetic flux. The removal of a light-guide coupled to the surface of the PMTs exposes the vacuum tube of the PMT to the magnetic field inside the tracker volume. As shown in figure *** the presence of a magnetic field is extremely detrimental to the performance of a PMT and so the shielding should ensure that all magnetic flux is removed from the volume of the PMTs.

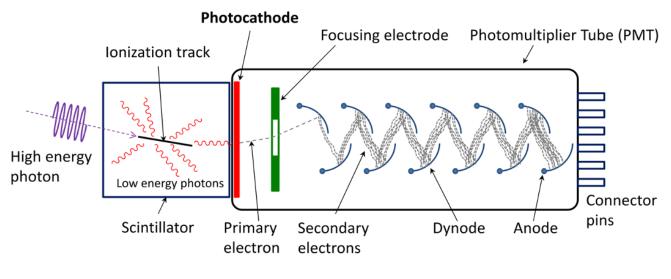


Figure 3.16: A

***from wiki

The working mechanism of a PMT involves incoming photons generating photoelectrons that are focused onto the first dynode. Secondary electron emission from the dynodes carries a charge which is collected by the anode. The collected current provides an output signal to indicate a hit to the calorimeter. With the addition of a magnetic field, the low energy photoelectron trajectories are altered, reducing the collection efficiency of the dynodes. Even at a field strength of 1 Gauss the reduction in collection efficiency results in a complete loss of signal. Furthermore, there is the possibility of PMT components, in particular, the dynode substrate and the electrode, being permanently magnetised following exposure to weak magnetic fields for long periods of time. The residual magnetization can result in a change to the gain of a PMT, ultimately reducing performance. Over the length of time taken for detector operation any changes in the gain of PMTs should be monitored to ensure the precision of energy measurements are maintained.

As a result of using the magnetic shields however, the shape and strength of the field is altered so that is it no longer uniform in shape or strength. As mentioned earlier, the expected magnetic field is labelled the realistic field and represents the magnetic field altered by the magnetic shielding to protect the PMTs against the magnetic flux in the tracker. The shape and strength of the realistic field is shown in the image below

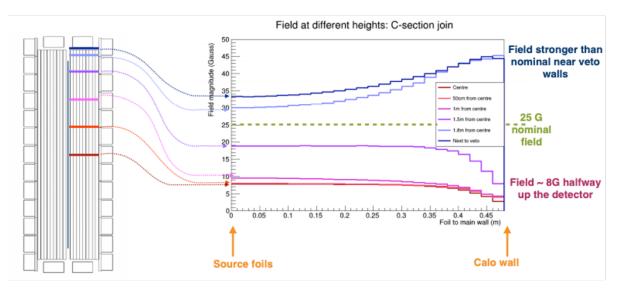


Figure 3.17: A

The main aim of the magnetic field analysis described in this thesis is to compare the performance of the three field configurations to determine which of the three fields is most advantageous for use during and throughout the detectors operational lifetime. Although the uniform field does not correctly depict the non-uniformity of the magnetic field during operation, it provides a nominal representation to compare to the other magnetic fields. Furthermore, by scaling the magnetic field applied by the coil, it is possible to increase the field strength of the realistic field so that it more closely resembles the uniform field and a more direct comparison can be made.

****as shown by scaled field****

No field examines the performance of the detector without an applied magnetic field. If no field displays an increased performance over the realistic and uniform fields it may be advantageous to run the detector without a magnetic field and to remove pair produced backgrounds through other avenues. Additionally, there is the option to run the detector without the magnetic field for a short period of time and to determine at what point, if at all, to turn on the magnetic field during experimentation. Once the magnetic field is turned on, it is impossible to reverse the effects of the applied field on the detector components even if the field is later turned off and so it is important to identify what approach to take and if or when the magnetic field should be applied, as applying the field is irreversible.

***maybe more detail on shields, relative permeability, vs field inside field *** maybe include pic of own magnetic field in 3D

3.4.2 Magnetic Shield Testing

Prior to installation, individual magnetic shields were tested to ascertain whether they were still able to significantly reduce magnetic flux from within the volume inside. To measure the efficiency at which the shields remove magnetic flux from within their own volume, the magnetic field with and without shielding was measured. A copper solenoid was connected to a controlled current source to generate a magnetic field. The solenoid was coiled around an impermeable container to retain the field inside of the container. A magnetometer was used to measure the field strength within the container. The field was calibrated to 25G following each measurement and the magnetometer measured the field strength, with and without shielding to determine the influence of the shield on the magnetic field inside of it.

Over 250 shields were tested, both for 8" and 5" PMTs, with the majority expelling over 95% ($\mathbf{B} < 1.25$ G)of the magnetic field within the shielded volume. Once tested the shields were packed and shipped to the LSM to be installed as part of the detector.



Figure 3.18: A

Chapter 4

Analysis Techniques

4.1 Falaise

Falaise provides the overarching software environment and is used as the primary tool for the simulation, processing and analysis of data for the SuperNEMO collaboration. Falaise uses the DECAY0 event generator in combination with GEANT4 and the C++ Bayeux library to generate and propagate particles throughout the depiction of the detector geometry.

Falaise is comprised of four principal components:

• Flsimulate

The primary tool for simulating data

• Flreconstruct

Pipeline structure used to process the output from fisimulate and produce reconstructed data

• Flvisualize

Event viewer for the visualization of the detector geometry, simulated and reconstructed data

• LibFalaise

The core libraries

Data production follows the route displayed in figure 4.1. Firstly, events are simulated, after which the simulated data is processed via a reconstruction pipeline to generate reconstructed data. Reconstructed data incorporates detector effects such as noise and energy resolution into the simulated data, producing data in the same format as the detector electronics.

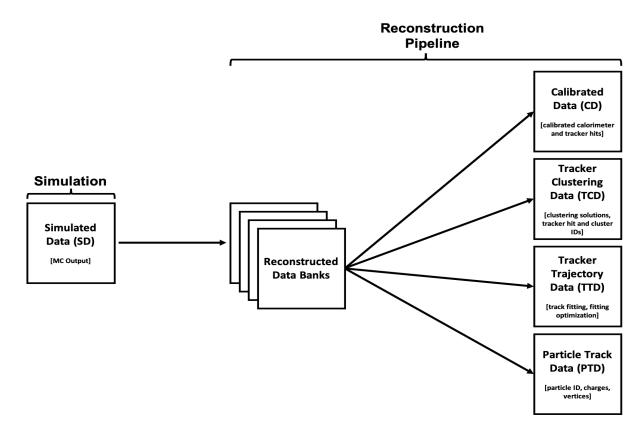


Figure 4.1: Visualization of the Falaise pipeline structure, beginning with simulation and ending with the stored data banks for reconstructed data.

4.1.1 Simulation

Flsimulate is the main simulation tool for SuperNEMO. Flsimulate is a command line program which accepts a configuration file that provides instructions for simulating events. The configuration file allows the user to determine multiple criterion for simulation, including;

- The initial decay particle
- The availability of raw data for secondary particles. Secondary particles are generated as a result of primary particle interactions with the detector (as described by GEANT4).
- Location of the decay vertex
- Number of simulations
- Magnetic field configuration

The DECAY0 event generator [42] is responsible for generating the initial radioactive decay particle with appropriate energies, timing, kinematics and branching ratios. Propagation of decay particles through the detector is determined by the object-oriented toolkit GEANT4 [43], which simulates the interactions of decay particles with the detector geometry and materials. GEANT4 also manages detector hits, tracks and visualisation for each simulated event. Flsimulate provides a default output file type of Boost over Root I/O (.brio) as suitable input for both reconstruction (flreconstruct) and visualization (flvisualize).

4.1.2 Reconstruction

The simulated output is processed with fireconstruct, using a customizable reconstruction pipeline, which runs through the raw data. Modules can be sequentially selected to generate and fill multiple data banks with reconstructed data. The reconstruction pipeline highlighted in figure 4.1 illustrates the data banks and the types of data they include. Calibrated Data (CD) includes data with the addition of detector noise and resolution effects. Tracker Clustering Data (TCD), using pattern recognition software, stores reconstructed tracker hits and clusters. Track fitting and χ^2 optimization of the clusters is stored in the Tracker Trajectory Data (TTD) and finally particle identification is accomplished, using the CD and TTD banks as inputs in order to identify the particle charges and vertices, storing the data in the Particle Track Data (PTD) bank. Combined, the different data banks provide all the reconstructed data for simulated decays, which provides an accurate depiction of the real data that is processed during detector operation.

An additional factor for reconstruction is the fitting type used by the TrackFit pipeline module. Charged particles can either be fitted with a straight track or a helical track, determined by the χ^2 of the proposed track. The track with the lowest χ^2 is selected from amongst the calculated tracks and is fitted to the simulated track. For no field simulations we expect the charged particle tracks to be straight and optimised to straight line fitting, however, for technical reasons, all three magnetic fields had both line and helical fitting active, which were fitted to the tracks solely based on the χ^2 value of the fitted track. Information regarding the curvature of charged particle tracks with no field was consequently discarded. Gammas are reconstructed using the gamma tracking module and are important for distinguishing the different background channels, such as $e\gamma$ or $e2\gamma$.

4.1.3 Visualization

Event display visualization of both raw and reconstructed data is possible using the GUI display, flvisualize. Flvisualize provides an interface for both 2D and expansive 3D visual projections of the detector. Visualised data is shown within the framework of the detector to allow for visual analysis of simulations. The left hand panel of flvisualize provides a 2D display of either the top, side or front of the detector. The second panel displays a 3D projection of the detector including all three spatial dimensions. Flvisualize also provides multiple panels, including a 'Tracks' panel, which displays reconstructed data structures with selective visuals, allowing the user to determine which

Analysis Techniques

visuals they wish to display. The remaining panels, 'Options' and 'Selections', provide additional functions however they are unimportant.

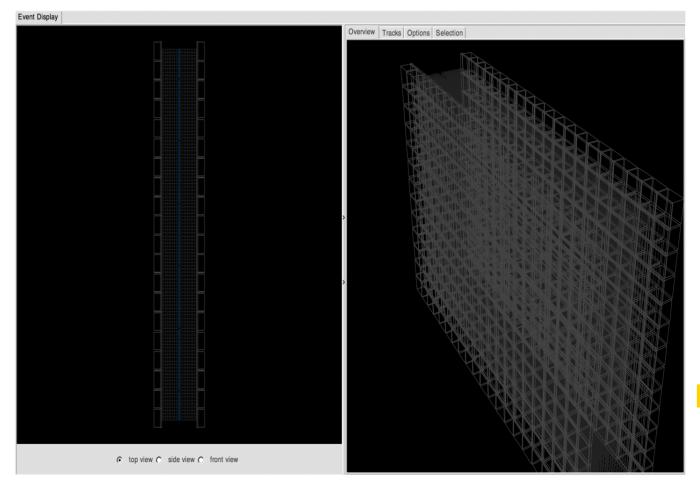


Figure 4.2: User interface of the Flvisualize tool used for visually displaying simulated and reconstructed events. The left hand side displays a 2D top view of the detector whereas the right hand side displays a 3D projection of the detector parallel to the foil.

4.1.4 Secondary Particle Information

Secondary particle information provides increased true/GEANT level information, including additional insight into the properties of simulated particles, both primary and secondary. Secondary particle information provides the following:

- i Particle designation (electron/positron/photon) for all true simulated particle tracks
- ii Particle classification (primary or secondary) contingent on if the particle originated from the initial decay (primary) or from any other source (secondary)

iii Number of true GEANT level hits for each particle track

iv Simulated true track visuals in flvisualize

Additional simulations, with access to secondary particle information, were simulated in order to shed more light on the underlying mechanism behind the considerable number of double beta candidate events from external ²⁰⁸Tl. Understanding the underlying mechanism allowed for the background to be explicitly targeted and removed, in order to reduce the total background contamination, as will be discussed in chapter ??.

4.1.5 Sensitivity Module

Sensitivity Module is a Falaise pipeline module which converts stored data from the Falaise data banks into easily readable ROOT nTuples. Sensitivity Module uses the output from flreconstruct to generate nTuples containing both simulated and reconstructed data. The combination of true and reconstructed data forms can be used to validate an analysis, by ensuring the true data supports inferences made using the reconstructed data.

Sensitivity Module can be uniquely compiled to add supplementary nTuple branches, containing a multitude of variables that may not already be encompassed into the pipeline. This allows additional parameters to be investigated as long as they can be computed from the Falaise data banks. By establishing the parameters necessary for identifying double beta decays, the selected parameters can be used to devise a double beta candidate cut flow.

The cut flow is a sequential application of data cuts, to determine the number of events in a particular decay channel, such as the 2e signal channel or one of the many background channels (e α and e γ). Events that pass all of the selected cuts are labelled as candidate events for the corresponding decay channel. During experimentation, the cut flow will be used on real data to probe various channels. By measuring the efficiency of reconstructing backgrounds in the two electron channel, the contribution of individual backgrounds to the $0\nu\beta\beta$ sensitivity can be determined.

4.2 Reconstructed Topologies

To identify double beta candidate events from reconstructed data, the reconstructed topology of charged particles must first be established so that the corresponding cuts can be identified and applied to the Sensitivity Module root nTuples. A double beta candidate event, in the 2e channel has a two electron topology, so the reconstructed topology of two electrons are combined. For the multitude of different backgrounds channels like $e\alpha$ and $e\gamma$, the reconstructed topologies of the photon and alpha particle are required.

4.2.1 Electrons and Positrons

Electrons are the primary particles for double beta decay so it is vital they are identified and differentiated from other particle topologies. Within the Falaise environment, the light charged particles (electron/positron) are characterized by a curved reconstructed track, with a vertex on the source foil and an associated calorimeter hit, as defined above. The subtle difference between the particle topology of an electron and a positron is the curvature of the track under an applied magnetic field as shown in figure 4.3. As a result of its' positive charge, the positron curves in the opposite direction to the electron; clockwise from a top down perspective. Whereas the negatively charged track curves anti-clockwise from a top down view. The curvature of a charged particle is also dependant upon the direction of travel, so for a positron travelling from the calorimeter to the source, the direction of curvature is identical to an electron travelling from the source to the calorimeters and vice versa. Charged particles travelling from the calorimeters to the foil can still be differentiated from source electrons by using timing and time of flight cuts.

Electrons and positrons are identical under reconstruction until the charge is identified. For no field there is no separation of charge and so electrons and positrons cannot be differentiated. By separating electrons and positrons, double beta candidate events that involve positrons can be identified and removed. The electron topology is most important for probing the 2e channel which is the decay channel used to search for neutrinoless double beta decay. The requirements for double beta candidate events in the two electron channel will be discussed in section ??.

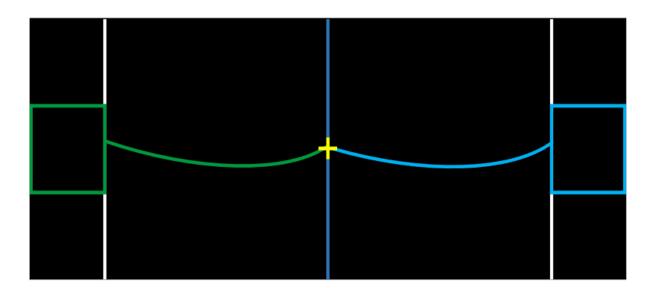


Figure 4.3: Representation of a reconstructed event with two charged particle tracks, the first belonging to an electron (blue track) and the second to a positron (green track), with an initial decay vertex on the source foil.

4.2.2 Gammas

When attempting to identify and measure the activities of selected backgrounds, it is important to establish the reconstructed topology of particles other than the electron and positron. Neutrinos are of course undetectable by the SuperNEMO demonstrator however the detector does allow for both photons and alpha particles to be identified. The beta decay of ²⁰⁸Tl results in the emission of multiple photons alongside the beta electron and ²¹⁴Bi beta decay is followed by the emission of a delayed alpha particle (figures ?? and ??). Establishing the additional particles that constitute these background decays helps to identify and remove them, reducing the total background count.

Unlike electrons and positrons, photons do not leave tracks in the detector and can only be identified by unassociated calorimeter hits, that is, calorimeter hits with no associated track or initial vertex. Furthermore, the time of flight cuts (internal and external probabilities) can be used to determine whether the timing of the unassociated calorimeter hit corresponds to that of a photon or an electron travelling from the source foil to the calorimeter. Calorimeter hits with energies lower than the detector trigger energy of 50 keV are labelled as noise regardless of whether there is an associated track or not. Reconstructed gammas often have noise hits close to the stricken calorimeter, however if the energies of these hits are below 50 keV, again the hits are labelled as noise. In the Falaise environment gammas can be identified by a yellow calorimeter hit with a dashed yellow originating at the particle source, as illustrated in figure 4.4.

The $1e2\gamma$ channel is the main gamma background channel and the primary channel for measuring the contamination of ²⁰⁸Tl. The $1e2\gamma$ channel contains events with a single electron accompanied

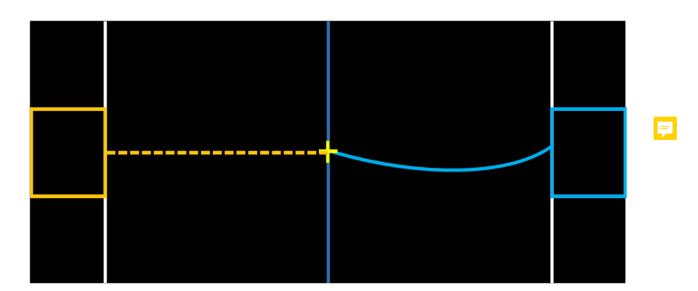


Figure 4.4: Representation of a reconstructed event with one electron (blue track) as well as a photon (yellow calorimeter hit with an unassociated/dashed track), with an initial decay vertex on the source foil.

by two photons. For ²⁰⁸Tl, the majority (99.8%) of decays result in the emission of a high energy 2.6 MeV photon which is often emitted alongside a number of lower energy photons. The decay scheme of ²⁰⁸Tl is complicated (figure ??) and can result in more than two photons being emitted from the decay, however the most populated background channel is the $1e2\gamma$ channel. Measuring $eN\gamma$ channels combines the reconstructed topologies of the electron and gamma, with addition of a shared vertex between the particles. Similarly, ²¹⁴Bi decays can result in the emission of multiple photons although the addition of the delayed alpha in ²¹⁴Bi beta decay allows for it to be measured in the $1e1\alpha$ decay that will be discussed in the following section.

4.2.3 Alphas

Alpha particles have short straight delayed tracks, confined to the tracker volume. The large mass of the alpha particle suppresses it's propagation through the tracker and it rapidly loses its' energy within the tracker in close vicinity to the source foil. The main source of alpha particles for SuperNEMO is the beta decay of ²¹⁴Bi to ²¹⁴Po, from the ²³⁸U decay chain shown in figure 3.12. ²²²Ra diffuses into the tracker volume and undergoes a number of decays, eventually resulting in the presence of ²¹⁴Bi on the surface of the source foil and tracker wires. ²¹⁴Bi undergoes beta decay to ²¹⁴Po which subsequently decays via alpha emission, with a half-life of 164.3 μ . The short red track in figure 4.5 demonstrates a typical reconstructed delayed alpha track alongside an electron. As mentioned earlier in the chapter, the number of tracker hits for a reconstructed alpha can be fewer than the three tracker hits required for a charged particle track. For non delayed tracker hits that are not part of a larger track, the hits are registered as noise, whereas isolated delayed hits are

reconstructed as alphas.

Reconstructed alphas permit the BiPo (²¹⁴Bi-²¹⁴Po) activity to be measured in the 1e1 α channel, throughout the detector. The rate of 1e1 α decays and consequently the BiPo activity within the different parts of the detector can be used to determine the contamination level of ²¹⁴Bi at those locations. For the 1e1 α channel, the reconstructed variables outlined for the electron and alpha, are combined with the following additional constraints:

- There only being one prompt track
- The delayed alpha track occurs at least 4μ s after the prompt electron track
- The two tracks share a vertex

As no other SuperNEMO background produces a delayed alpha, the $1e1\alpha$ channel can be precisely measured to determine the BiPo activity.

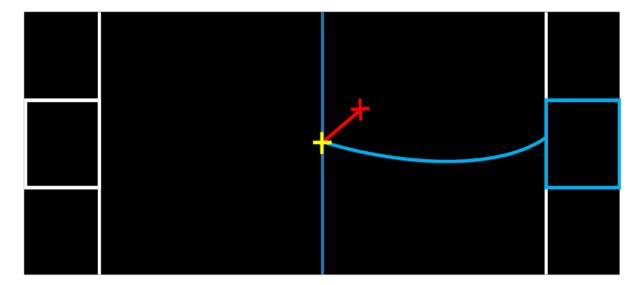


Figure 4.5: Representation of a reconstructed event with one electron (blue track) as well as an alpha (short red track), with an initial decay vertex on the source foil.





4.3 Internal/External Hypothesis

Any internal contribution, whether signal $(0\nu\beta\beta)$ or background, must originate from within the source foil and should not be induced by interactions originating from a source external to the ⁸²Se source foil. Time of flight information is used to establish the origin of the initial decay. The time of flight cuts used are the internal and external probabilities, which estimate the probability that a reconstructed event was induced by a decay interior or exterior to the source foil. The external probability does not differentiate between an event originated from radon in the tracker or one of the many external background sources outlined earlier. For $0\nu\beta\beta$, time of flight information is most useful for identifying and removing double beta like events that may have originated from a source external to the source foil, whilst simultaneously the internal probability is used to ensure that any real double beta decays originated from within the source foil.

The internal hypothesis assumes a measured particles originated from within the source foil and the probability of this hypothesis can be calculated using the calorimeter hit timing of the particles. To calculate the internal probability, given two different calorimeter hit times t_1^{meas} and t_2^{meas} , first the theoretical time of flight t_i^{tof} is calculated using

$$t_i^{\text{tof}} = \frac{l_i}{\beta_i} \tag{4.1}$$

with l_i the length of the particle track which is curved for charged particles and straight line for photons. Additionally, for photons $\beta_i = 1$ and for electrons is calculated using

$$\beta_i = \frac{\sqrt{E_i \left(E_i + 2m_e\right)}}{E_i + m_e} \tag{4.2}$$

with E_i the calibrated energy recorded by the calorimeter and m_e the rest mass of an electron. The emission time of a particle, t_i^{int} , takes into account the measured time in the calorimeter as well as the theoretical time of flight and is given as

$$t_i^{\text{int}} = t_i^{\text{meas}} - t_i^{\text{tof}} = t_i^{\text{meas}} - \frac{l_i}{\beta_i}$$

$$(4.3)$$

A χ^2 test representing the approximately Gaussian timing distribution is used with the corresponding χ^2 variable

$$\chi_{\rm int}^2 = \frac{\left(\left(t_1^{\rm meas} - \frac{l_1}{\beta_1}\right) - \left(t_2^{\rm meas} - \frac{l_2}{\beta_2}\right)\right)^2}{\sigma_{t_1^{\rm int}}^2 + \sigma_{t_2^{\rm 2int}}^2}$$
(4.4)

=

where $\sigma_{t_i^{\text{int}}}^2$ represents the variance of the emission timing t_i^{int} . $\sigma_{t_i^{\text{int}}}^2$ depends on multiple factors including the uncertainties on the measured time, particle speed and distance travelled. For photons, the particle speed is c and so there is no uncertainty on this value, however the uncertainty surrounding the path length is unknown as photons are not tracked in SuperNEMO.

 $\chi^2_{\rm int}$ is converted into a probability by transforming the Gaussian distribution into a flat distribution between 0 and 1. The internal probability is therefore defined as

$$P\left(\chi_{\rm int}^2\right) = 1 - \frac{1}{\sqrt{2\pi}} \int_0^{\chi_{\rm int}^2} x^{-\frac{1}{2}} e^{-\frac{x}{2}} dx \tag{4.5}$$

Unlike the internal hypothesis, the external hypothesis assumes an incident external photon interacts with the detector to produce either a $1e1\gamma$ event or a crossing electron. The external background results in the generation of an event in the 2e channel via a number of mechanisms that will be outlined later on. Calculating the external probability is done in a similar manner to the internal probability, but the time of flight t^{tof} is given as

$$t^{\rm tof} = \frac{l_1}{\beta_1} + \frac{l_2}{\beta_2} \tag{4.6}$$

which sums the timing for both particle tracks.

The χ^2 for the external hypothesis is then

$$\chi_{\text{ext}}^{2} = \frac{\left(\left(t_{2}^{\text{meas}} - t_{1}^{\text{meas}} \right) - \left(\frac{l_{1}}{\beta_{1}} + \frac{l_{2}}{\beta_{2}} \right) \right)^{2}}{\sigma_{t_{1}^{\text{ext}}}^{2} + \sigma_{t_{2}^{\text{ext}}}^{2}}$$
(4.7)

where $\sigma_{t_i^{\text{int}}}^2$ is the equivalent variance of emission for the external hypothesis. Like the internal probability in equation 4.5, the external probability is calculated with

$$P\left(\chi_{\text{ext}}^{2}\right) = 1 - \frac{1}{\sqrt{2\pi}} \int_{0}^{\chi_{\text{ext}}^{2}} x^{-\frac{1}{2}} e^{-\frac{x}{2}} dx$$
(4.8)

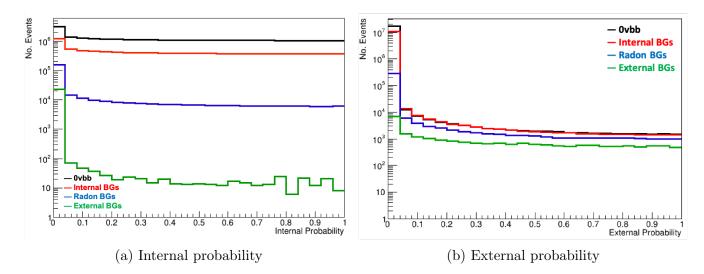


Figure 4.6: Internal (a) and external (b) probabilities for $0\nu\beta\beta$, internal, radon and external backgrounds with reconstructed 2e topologies. The probability distributions were calculated using the equations 4.5 and 4.8 respectively.

4.4 Number of Expected Events

In order to determine the contribution of different backgrounds to a decay channel (for $0\nu\beta\beta$ this is the 2e channel), the number of expected events (N_exp) of the background is first calculated. The number of expected events represents the total number of expected decays of a particular background during the detectors operational lifetime and is calculated differently for backgrounds located in different parts of the detector in order to correctly represent the changing exposure throughout the detector. The ratio of successfully reconstructed events in a given channel, from a known number of Monte Carlo simulations is denoted the detection efficiency and is given as the following,

$$\epsilon = \frac{N_{Survived}}{N_{TOTMC}} \tag{4.9}$$

with $N_{Survived}$ equal to the number of events that pass all the cuts and N_{TOTMC} the total number of simulated events. The number of expected events of ⁸²Se two neutrino double beta decay, in the source foil, is given by,

$$N_{2\nu\beta\beta} = \frac{N_A \times \ln 2 \times \epsilon \times m \times t}{T_{1/2}^{2\nu\beta\beta} \times M(^{82}Se)}$$
(4.10)

where N_A is Avogadro's constant, ϵ is the previously quoted reconstruction efficiency ratio, m is the total mass of the ⁸²Se source foil (6.23 Kg), t is the total run time of the experiment, $T_{1/2}^{2\nu\beta\beta}$ is the half life of ⁸²Se and $M(^{82}Se)$ is the mass number for ⁸²Se. For other internal backgrounds, such as ²⁰⁸Tl and ²¹⁴Bi, the number of expected events is

$$N_i = A_i \times \epsilon_i \times m \times t \tag{4.11}$$

with A_i and ϵ_i designated as the activity and reconstruction efficiency respectively, for background *i*.

Radon induced backgrounds are calculated using the activity of the background within the volume of the tracker chamber. The volume of the tracker replaces the source foil mass in equation 4.11 and so the number of expected events for Radon simulations is given by,

$$N_i = A_i \times \epsilon_i \times V \times t \tag{4.12}$$

with V as the volume of the tracker chamber. External backgrounds were only simulated on the PMT glass bulbs, so the activity is a proportion of the total activity from the entire PMTs. The number of expected events for external backgrounds is given by,

$$N_i = A_{Glassbulb.i,i} \times \epsilon_i \times t \tag{4.13}$$

with $A_{Glassbulb,i,i}$ the activity of the PMT glass bulb for a given background i and PMT location j.

The number of expected events represents the total contribution of a decay to a particular channel. For SuperNEMO, the signal detection efficiency and the contribution of different backgrounds in the 2e channel are used in order to estimate the overall $0\nu\beta\beta$ half-life sensitivity of the demonstrator.

4.5 Half-Life Calculation

The sensitivity of an experiment is often given as a half-life $T_{1/2}$, which incorporates the detection efficiency and N_{exp} from section 4.4. To derivation of the half-life formula is shown below, starting with the exponential decay of a radioactive isotope,

$$N(t) = N(0)e^{-\lambda t} \tag{4.14}$$

with N(t) the number of remaining atoms of the isotope at time t, N(0) the number of atoms at the beginning of the experiment and λ the decay constant. λ is related to the half-life $T_{1/2}$ by the following

$$\lambda = \frac{\ln(2)}{T_{1/2}} \tag{4.15}$$

The half-life of two neutrino ⁸²Se double beta decay is approximately of the order 10^{20} years and even greater for neutrinoless double beta decay so equation 4.14 can be Taylor expanded in λt to give the approximation

$$e^{-\lambda t} \simeq (1 - \lambda t) \tag{4.16}$$

The number of observed events can therefore be written as

$$N_{\rm obs} = \epsilon N(0) \left(1 - e^{-\lambda t}\right) \simeq \epsilon N(0) \lambda t = \epsilon N(0) \frac{\ln(2)}{T_{1/2}} t$$
(4.17)

with the ϵ the detection efficiency of $0\nu\beta\beta$ and t the running time of experimentation. The number of atoms at the beginning of the experiment, N(0) is given by



$$N(0) = \frac{N_A m}{A} \tag{4.18}$$

and by inserting the definition of N(0) into equation 4.17, the half life of $0\nu\beta\beta$ can be calculated using

$$T_{1/2} = \frac{\epsilon}{N_{\rm obs}} \frac{N_A m}{A} \ln(2)t \tag{4.19}$$

4.5.1 Half Life Approximation

There are various methods to approximate the half-life sensitivity established in section 4.5, the most common of which use the entire energy spectrum of both signal and background and separate them to determine their respective contributions. In this thesis, a basic counting approach is utilized, which determines the number of expected events found in a selected energy window to calculate the half-life. For ⁸²Se neutrinoless double beta decay, the initial counting window is established as 2.8 to 3.2 MeV (highlighted in figure 4.7), encompassing the ⁸²Se Q valu, corresponding to the peak of the $0\nu\beta\beta$ energy distribution. Counting methods are less precise than the more thorough complete energy spectrum methods, however as this thesis is a comparative analysis to determine which of the three magnetic field is most suitable for detector operation, a less precise but relative study between the three magnetic fields is beneficial. By attempting to compare the relative performance of the three magnetic fields, the precision of the sensitivity estimation can be compromised in order to increase the speed of the analysis.

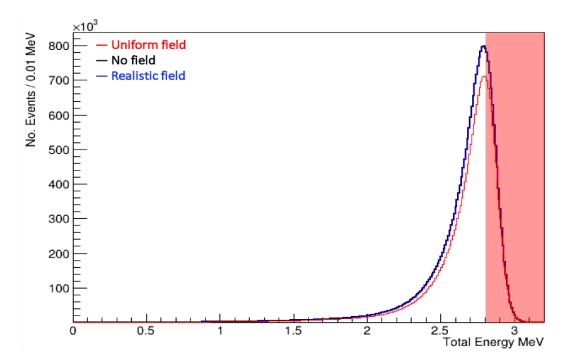


Figure 4.7: $0\nu\beta\beta$ total energy spectra for the three magnetic field configurations, with the region of interest (2.8 - 3.2 MeV) highlighted in red.

4.6 Limit Setting Procedures

As mentioned, for this work, a counting approach is utilized for estimating the half-life sensitivity of the SuperNEMO demonstrator. The first counting method is a Gaussian approximation, which is particularly useful for studies with low numbers of expected backgrounds. For the Gaussian approximation at 90% CL, $T_{1/2}^{0\nu}$ is defined as,

$$T_{1/2}^{0\nu} > 4.16 \times 10^{26} \text{yr} \left(\frac{\epsilon amt}{M(^{82}Se)}\right) \left(\frac{1}{1.64\sqrt{N_B}}\right)$$
(4.20)

with ϵ the efficiency of detecting 0vbb (from equation 4.9), *a* the isotopic abundance (given as 1 for the refined source foil), *mt* the exposure, $M({}^{82}Se)$ the ${}^{82}Se$ mass number and N_B the number of expected background events. The $\sqrt{1.64}$ denominator term represent a 90% confidence level (CL). Although not as precise as the other methods, the Gaussian approximation is a simple and fast approach for comparing the performance of three magnetic field configurations, although as the number of background events increases, the precision of the Gaussian approximation reduces significantly.

An alternative to the Gaussian approximation is the Poissonian approximation which provides greater precision for an analysis with increased statistical data. Poissonian approximations use equation 4.19 with the extraction of N_{obs} dependent upon a selected method. The methods used to calculate the number of observed events include the Feldman-Cousins method described in [45] and the Minimum Detectable Activity (MDA) method [46], both of which are outlined below.

4.6.1 Feldman-Cousins

The Feldman-Cousins approach is often used to quote limits on the size of a signal, given the background contamination. For a known background and confidence limit, for a Poissonian signal such as equation 4.21, Feldman-Cousins provides an estimate for $N_{\rm obs}$ which is then used to calculate equation 4.19.

$$P(s \mid b, N) = \frac{e^{-(s+b)}(s+b)^N}{N!}$$
(4.21)

4.7 Minimum Detectable Activity

In this thesis, the definition used for the minimum detectable activity is given in 'Radiation Detection and Measurement' by G. F. Knoll [46]. Knoll uses a binary pretence of whether the detector output represents a background only or a combination of backgrounds plus signal. By establishing the probability of a false positive as an identified signal even though only background is present and a false negative as the probability a signal is misidentified as a background, a critical count number n_c can determine the minimum threshold count, above which a signal is present.

For a Poisson distributed background B and a probability of a false positive less than 1 - CL, n_c must be increased until the following is satisfied,

$$P_B(n \ge n_c) = \sum_{n=n_c}^{\infty} Pois(n; B) = 1 - \sum_{n=0}^{n_c-1} e^{-B} \frac{B^n}{n!} \le 1 - CL$$
(4.22)

Once the probability of a false positive is reduced to below 1 - CL, the false negative probability is used to calculate the minimum expected signal count S. S can be determined by increased it's value until the following equation is satisfied,

$$P_{S+B}(n < n_c) = \sum_{n=0}^{n_c-1} \text{Pois}(n; S+B) = \sum_{n=0}^{n_c-1} e^{-(S+B)} \frac{(S+B)^n}{n!} \le 1 - \text{CL}$$
(4.23)

The MDA method is illustrated in figure 4.8, with the black curve representing the Poisson distributed background B and the red curve representing the combined signal and background expectation. Both shaded areas illustrate the 1 - CL from equations 4.22 and 4.23. For the purpose of this work, the confidence level is set at 90% and so the shaded areas represent 10% of the total area of each curve. The minimum signal S and critical count n_c are then used to determine N_{obs} , in order to set a half-life limit using equation 4.19.

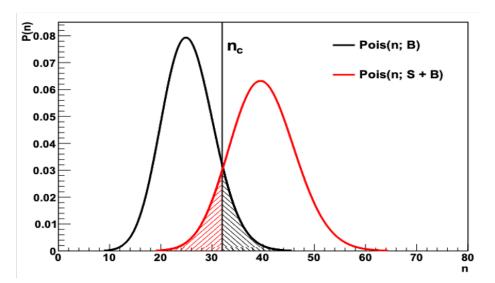


Figure 4.8: Probability distributions for the two Poisson variables, B and S + B. The black curve represents the background distribution and the red curve signal + background, with the shaded areas each corresponding to 1 - CL [16].

Chapter 5

Double Beta Decay Event Selection

The sensitivity to neutrinoless double decay is the primary metric of success for the magnetic field analysis described in this work. The results from the double beta decay simulations (signal) will be discussed, including the impact of the 2e topology cuts from chapter 4 on the concurrent and final detection efficiency for each of the three magnetic field scenarios. For the $0\nu\beta\beta$ analysis, $2\nu\beta\beta$ is treated as a background and contributes to the total background contamination. The high energy window/region of interest established in the previous chapter ensures the contamination of $2\nu\beta\beta$ is suppressed however a very small number of $2\nu\beta\beta$ events still remain. Additionally, the best case scenario SuperNEMO detector will be discussed, that is, a radiopure detector with only $2\nu\beta\beta$ as an irreducible background to $0\nu\beta\beta$. With improved processing methods it may be feasible to reduce or eliminate other backgrounds, improving detector conditions for probing neutrinoless double beta decay.

5.1 Neutrinoless Double Beta Decay $(0\nu\beta\beta)$

The primary goal of the SuperNEMO experiment is to search for the neutrinoless double beta decay of ⁸²Se, by optimising the sensitivity of the detector to the decay. Parallel to this, SuperNEMO aims to improve on the previous half-life measurement for the two neutrino decay of ⁸²Se and increase the precision of the two neutrino decay nuclear matrix elements. In order to determine the neutrinoless double beta decay sensitivity, the detection efficiency of $0\nu\beta\beta$ (equation 4.9) must first be extracted from simulated data. For each of the three magnetic fields, 10⁸ simulated decays of $0\nu\beta\beta$ were uniformly distributed in the bulk of the source foil using the official Falaise 4.0.0 reconstruction with an exposure of 15.275 Kg yr⁻¹ (6.110Kg × 2.5 years). As previously mentioned, the cut flow is applied to simulated date in order to extract $N_{Survived}$, which is used to calculate the detection efficiency of the simulated isotope in the 2e channel and is briefly described below.

5.2 Identifying Double Beta Events

The search for ⁸²Se neutrinoless double beta decay is measured in the two electron channel, but not all events found in the two electron channel are necessarily from real double beta decays and may in fact materialise from specific backgrounds. The reconstructed topology of an electron was established, in section 4.2.1, as a negatively curved track with a vertex on the source foil and an associated calorimeter hit. For a double beta candidate event in the 2e channel, the reconstructed topologies of two electrons are combined with additional constraints, all of which are outlined below.

5.2.1 2e Channel Selection

• Two calorimeter hits

Two calorimeter hits above 50 keV, with at least one hit above 150 keV, measuring the energies of the two double beta decay electrons. The minimum energy requirement is determined by the trigger energy of the detector.

• Two tracker clusters and two tracks

Two tracks, derived from two tracker clusters are selected to represent the tracks of the two emitted electrons during double beta decay.

• Each track associated to a unique calorimeter

Each track is associated to a calorimeter ensuring the two beta electron tracks correspond to the two calorimeter hits. Additionally the two calorimeter hits belong to two unique calorimeters. One of the main benefits of SuperNEMO is that it allows the energy of each individual electron to be measured which can only be achieved when electrons hit separate calorimeters.

• Two vertices on the source foil

The two electron vertices should be located on the source foil, ensuring a reconstructed path from the foil, through the tracker and finally into the calorimeters for the two electrons.

• Internal and External Probability

The timing of the calorimeter hits must be within a certain boundary to ensure the electrons originated from within the source foil and did not enter the tracker from an external source. Internal and external probability essentially act as time of flight cuts.

• No Positrons

The double beta decay charged particle tracks can belong to either electrons or positrons. The charge of each track can be identified from the curvature of the track so electrons and positrons can be differentiated. Identifying both tracks as electrons is the final step for 2e selection.

5.2.2 2e Channel Optimization

The 2e channel cuts help to identify double beta candidate events however additional cuts are necessary for improving the overall detection efficiency of double beta decay simulations. Three additional optimization cuts are,

• Maximum vertex separation

The maximal separation between the vertices is $\Delta R < 1$ cm and $\Delta Z < 3$ cm, where ΔR represents the radial separation and ΔZ the vertical separation.

• No delayed alpha tracks

No delayed/alpha tracks, between 13 and 700 μ . The 13 μs lower limit includes detector effects like the tracker response time and the upper limit is approximately 4 × the half-life of ²¹⁴Po. The delayed window is kept open so as to measure BiPo decays.

• ROI energy

No events are allowed outside of the energy window (ROI). The nominal ROI is 2.8 - 3.2 MeV for 82 Se, however the ROI is subject to optimization. The ROI selects a bin of a specified width for estimating the sensitivity using a counting method.

Together, the two electron channel and optimization cuts combine to form the double beta decay cut flow, for the purpose of extracting the detection efficiency and subsequently the contribution of background decays, such as $2\nu\beta\beta$, to the ⁸²Se sensitivity. The cuts are selected in order to maximise the reconstruction efficiency of true double beta decays, whilst reducing the prevalence of background induced two electron events.

	Magnetic Field Configuration		
Cut Descriptions	Uniform Field	No Field	Realistic Field
Only two calorimeter hits above 50 keV, at least one >150 keV	0.562	0.594	0.589 📮
Two tracker clusters with 3 or more cells	0.380	0.446	0.436
Two reconstructed tracks	0.378	0.443	0.433
Remove events with two electron hits to the same calorimeter	0.373	0.438	0.429
Each track associated to a calorimeter	0.338	0.400	0.390
Two vertices on the source foil	0.337	0.399	0.389
Vertex ΔR <1cm and ΔZ <3cm (separation between vertices)	0.240	0.281	0.274
Internal Probability ${>}1\%$ and External Probability ${<}4\%$	0.226	0.265	0.259
No delayed alpha tracks (no tracks with $13\mu s < t < 700\mu s$)	0.226	0.265	0.259
Remove positrons (unavailable for no field)	0.211	_†	0.179
ROI energy (between 2.8 and 3.2 MeV) $$	0.0653	0.0790	0.537

Table 2: $0\nu\beta\beta$ cut flow for the three magnetic field configurations. Each row lists a short description of the cut as well as the concurrent detection efficiency.

[†]For no field, the no positron cut is not applied as without a magnetic field, the charges of the particle tracks are indeterminable. The magnetic field curves electrons and positrons in opposite directions as a result of their differing charges and so without a magnetic field, the charged particle tracks are straight, ignoring any low energy scattering.

The breakdown of the $0\nu\beta\beta$ cut flow is provided in table 2, illustrating how the detection efficiency changes with each sequential cut. A short description of each of the cuts is provided. The cut flow follows the ordering shown in section 5.2.1, however the three additional optimization cuts; the maximum vertex separation, no delayed tracks and the energy window (or ROI) are added to the cut flow as cuts seven, nine and eleven respectively. The order of the cut flow is important for studying the impact of each individual cut on the concurrent detection efficiency and importantly, understand how the different magnetic fields influence the overall final detection efficiency. In the following section, a short explanation of the most impactful cuts will be presented and their inclusions in the cut flow justified.

5.2.3 Most Impactful Cuts

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The cut flow is required to determine whether a simulated event has a two electron topology, so it is vital that the cuts not just identify two electrons from the topologies discussed in chapter 4, but also target and remove events with reconstructed topologies found in one of the various background decay channels, such as $e\gamma$ and $e\alpha$. The cut flow begins with the two calorimeter cut, which removes almost 50% of events, for all three magnetic fields. Requiring two calorimeter hits is most effective for removing $1e2(+)\gamma$ events that have more than two calorimeter hits and any 1e events from background decays or improper double beta decays where one of the electrons doesn't escape the foil or tracker volume. Removing events with two electron hits to the same calorimeter ensures the energy of individual electrons can be measures which is one of the significant advantages of the SuperNEMO demonstrator. The fifth cut, which requires both particle tracks to be associated to a calorimeter, targets both $1e1\gamma$ and $1e1\alpha$ backgrounds that have only one associated track, belonging to the single electron.

Additional noteworthy cuts include the vertex separation, no positron and finally the ROI window. The vertex separation cut applies a harsher constraint compared to previous studies. In [47], ΔR is required to be <6cm and ΔZ <7cm, culminating in over 95% of double beta candidate events from the source foil surviving the cut, compared to the approximately 70% survival rate with ΔR <1cm and ΔZ <3cm. The appointed constraint is a consequence of the expected spatial resolution of roughly 8%, with an effective maximum longitudinal resolution of \approx 1.1 cm at the mid length of a cell [48].

The penultimate no positron cut is used to remove double beta candidate events that have at least one charged particle labelled as a positron. As previously stated, the no positron cut is inapplicable for the no field scenario. Moreover, the cut removes a large number of events for the realistic field, around 30%, and close to 7% of events for the uniform field, as the increased field strength increases the efficiency of labelling charged particles correctly. Finally, the energy window removes the majority of remaining events as the ROI encompasses only a small segment of the overall energy spectrum. Between the three magnetic fields, the shape of the spectra is unchanged, resulting in a similar proportion of events removed.

	Detection Efficiency ϵ		
Cut Descriptions	Uniform Field	No Field	Realistic Field
Only two calorimeter hits above 50 keV, at least one ${>}150{\rm keV}$	0.237	0.287	0.279
Two tracker clusters with 3 or more cells	0.147	0.205	0.195
Two reconstructed tracks	0.146	0.204	0.194
Remove events with two electron hits to the same calorimeter	0.143	0.201	0.191
Each track associated to a calorimeter	0.125	0.179	0.170
Two vertices on the source foil	0.125	0.178	0.169
Vertex ΔR <1cm and ΔZ <3cm (separation between vertices)	0.072	0.101	0.096
Internal Probability ${>}1\%$ and External Probability ${<}4\%$	0.068	0.095	0.090
No delayed alpha tracks (no tracks with $13\mu s < t < 700\mu s$)	0.068	0.095	0.090
Remove Positrons (unavailable for no field)	0.063	_†	0.060
ROI energy (between 2.8 and 3.2 MeV)	3×10^{-8}	2×10^{-8}	1×10^{-8}
Number of Expected Events	$\begin{array}{c} 0.15 \\ \pm \ 0.09 \end{array}$	$\begin{array}{c} 0.10 \\ \pm \ 0.07 \end{array}$	$\begin{array}{c} 0.05 \\ \pm \ 0.05 \end{array}$

5.3 Two Neutrino Double Beta Decay $(2\nu\beta\beta)$

Table 3: $2\nu\beta\beta$ cut flow and number of expected events for the three magnetic field configurations. Each row lists a short description of the cut as well as the concurrent detection efficiency.

 † No positron cut for no field scenario.

The cut flow for $2\nu\beta\beta$ double beta candidate events is shown in table 3, alongside the number of expected events with 2.5 years of exposure. The overall detection efficiency is significantly lower for $2\nu\beta\beta$ compared to $0\nu\beta\beta$, particularly in the ROI, where the detection efficiencies are of the order 10^{-8} . A low detection efficiency for $2\nu\beta\beta$ is important when measuring the sensitivity to neutrinoless double beta decay as $2\nu\beta\beta$ is the single irreducible background for the neutrinoless search.

The sum of the two electron distribution is shown in figure 5.1. For neutrinoless double beta decay, the total energy correlates well with the expected Landau distribution seen for charged particles traversing a thin film. The distribution peaks around the decay energy of ⁸²Se (figure 3.3) and the Landau tail extends back to the 200 keV trigger energy. The shape of the distribution is unchanged between the three magnetic fields. The tail of the two neutrino distribution barely penetrates into the ⁸²Se ROI, resulting in the low detection efficiencies for the three fields as shown in table 3. The majority of $2\nu\beta\beta$ events are found at lower energies, with the peak of the distribution close to 1 MeV.

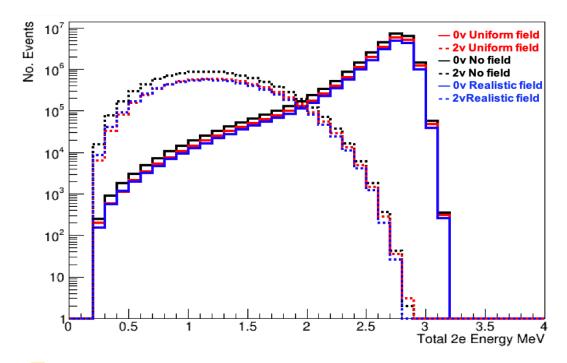


Figure 5.1: 0 and $2\nu\beta\beta$ total energy spectra for events with a 2e topology with all three magnetic fields. The $0\nu\beta\beta$ spectra are illustrated by the thick line and $2\nu\beta\beta$ by the dotted line.

SuperNEMOs modular structure provides the ability to reconstruct the entire topology of individual particles. One of the most important variables for studying the intermediate decay mechanism of ⁸²Se $0/2\nu\beta\beta$ decay, is the single electron energy. The single electron energy distribution is presented in figure 5.2, for both 0 and $2\nu\beta\beta$ and can be used to infer the mechanism underlying the decay itself and whether the decay prefers HSD or SSD as discussed in chapter ***ref HSD/SSD. The distribution shape of the total energy is independent of the magnetic field choice, for both the neutrinoless and two neutrino decays.

Similarly, the angular distribution is also sensitive to the underlying decay mechanism of $0\nu\beta\beta$ and the cosine of the angle between the two electron tracks is shown in figure 5.3. The cosine(θ) curve for $0\nu\beta\beta$ is expected to follow a 1 - cos(θ) distribution with the addition of detector effects, however, as shown in figure 5.3, the number of events reduces as you get closer to cos(θ) = 0. Again, both variables are important for analysing the underlying double beta decay mechanism.

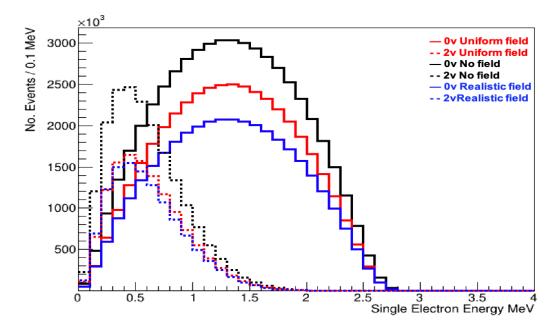


Figure 5.2: 0 and $2\nu\beta\beta$ single electron energy spectra for events with a 2e topology with all three magnetic fields. The $0\nu\beta\beta$ spectra are illustrated by the thick line and $2\nu\beta\beta$ by the dotted line.

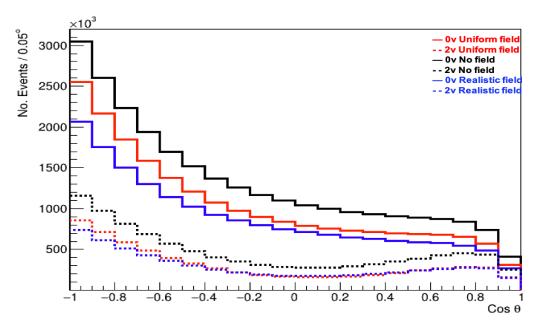


Figure 5.3: 0 and $2\nu\beta\beta$ cos θ spectra for events with a 2e topology with all three magnetic fields. The $0\nu\beta\beta$ spectra are illustrated by the thick line and $2\nu\beta\beta$ by the dotted line. All events have a total energy within the ⁸²Se ROI (2.8 - 3.2 MeV).

5.3.1 SuperNEMO Sensitivity with $2\nu\beta\beta$ Background Only

Prior to investigating the contributions from the other background sources, it is useful to consider the case of the best case scenario detector, which only includes the irreducible $2\nu\beta\beta$ as a background. Although SuperNEMO has a number of different backgrounds that contribute towards the ⁸²Se ROI, from internal, radon and external sources, it may be possible to further reduce and perhaps eliminate all of the reducible backgrounds. To reduce the internal contamination, the source foils can undergo increased processing which is made easier by the modular structure of the SuperNEMO demonstrator, allowing the source foils to be easily removed and replaced. Radon and external backgrounds can be reduced by improving the radon flushing inside the tracker and increasing shielding provess respectively. For the best case scenario detector, this would result in a reduction or elimination of all backgrounds leaving only $2\nu\beta\beta$. The best tool for minimising the $2\nu\beta\beta$ backgrounds contribution is the decay energy. The $2\nu\beta\beta$ total energy spectra is skewed to lower energies, whereas the $0\nu\beta\beta$ energy spectra peaks around the ⁸²Se ROI (figure 5.1), as there are no neutrinos to reduce the energy carried by the electrons. By maximising the energy resolution, the rare $0\nu\beta\beta$ background peak can be most optimally separated from the $2\nu\beta\beta$ background continuum, particularly when probing the ROI at the ⁸²Se Q value. The width and position of the ROI is dependent upon the energy resolution of the experiment, so it is important to maximise this resolution, particularly for the ideal case scenario, where the most optimal strategy for separating the signal and 2ν background uses the measured energy of the decay progeny.

Using the associated cut flows and expected events, the sensitivity of the best case scenario detector setup with no reducible backgrounds is shown in figure 4,

	S	ensitivity \times 10	24
Approximation Method	Uniform Field	No Field	Realistic Field
Sensitivity Feldman-Cousins	2.22	2.63	1.75
MDA	-	-	-

Table 4: Best case scenario detector sensitivity estimate for the three magnetic fields. Best case scenario assumes only $2\nu\beta\beta$ as a contributing background to the ⁸²Se $0\nu\beta\beta$ ROI.

As mentioned in section 4.5, the Poissonian approximation provides greater precision with higher statistics but struggles with a number of expected backgrounds close to zero. However for a relative study between the three magnetic field scenarios it can still be useful for determining which magnetic field delivers the greatest detector sensitivity. Of the three fields, no field has the highest sensitivity with all three estimation methods, culminating in a sensitivity of ***confirm MDA result***, owing

to the much greater detection efficiency of $0\nu\beta\beta$. *** calc detection efficiency of MDA ***

	Ma	gnetic Field Configura	tion
0ν Detection Efficiency	0.0653	0.0790	0.0537
$2\nu\beta\beta$ Detection Efficiency	3×10^{-8}	2×10^{-8}	1×10^{-8}
$2\nu\beta\beta$ Number of Expected Events	0.15 ± 0.09	0.10 ± 0.07	0.05 ± 0.05
Sensitivity Feldman-Cousins	2.217	2.625	1.747
MDA	-	-	-

5.4 Summary of Double Beta Decays

Table 5: Summary table of the $0/2\nu\beta\beta$ detection efficiency, $2\nu\beta\beta$ number of expected events and the sensitivity estimates for the three magnetic fields.

Of the three magnetic field configurations, the no field scenario maintains the greatest detection efficiency after applying the two electron cut flow outlined in section 4.5. Additionally, as a result of the high energy region of interest, the two neutrino detection efficiency is suppressed and accordingly the background contribution is extremely small. When considering the ideal detector scenario, the highest sensitivity is achieved for no field as a result of the superior 0.0790 detection efficiency. The Poissonian approximations of the sensitivity are imprecise for low background statistics, nonetheless, when taking into account the additional background sources, the precision should improve. Although the idealistic detector assumes zero non DBD backgrounds, the current demonstrator module has non-zero background contributions from all different parts of the detector. To measure the sensitivity inclusive of the other backgrounds, the same procedure carried out to determine the $2\nu\beta\beta$ background count will be used for the remaining reducible backgrounds.

Chapter 6

Conclusion

Conclusion

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References

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