Overview: Diffraction in ep and pp collisions

Graeme Watt

University College London

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In collaboration with H. Kowalski, A.D. Martin, L. Motyka and M.G. Ryskin

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What is diffraction?

Two equivalent definitions of what is meant by 'diffraction' in high-energy physics:

- "A reaction in which no quantum numbers are exchanged between the colliding particles is, at high energies, a diffractive reaction." [Good–Walker,'60]
- 2 "A diffractive reaction is characterized by a Large, non-exponentially suppressed, Rapidity Gap (LRG) in the final state." [Bjorken,'92]



Diffraction is 'Pomeron' (\mathbb{P}) exchange!

What is the 'Pomeron'?

• In Regge theory, asymptotic behavior $(s \gg |t|)$ of cross sections given by

$$\sigma_{\rm tot} \sim s^{\alpha(0)-1}, \quad \mathrm{d}\sigma_{\rm el}/\mathrm{d}t \sim s^{2[\alpha(t)-1]}, \quad \alpha(t) = \alpha(0) + \alpha' t.$$

- The 'Pomeron' was a Regge trajectory with intercept α_P(0) = 1 introduced to explain the asymptotically constant total cross sections expected in the '60s.
- Fit to soft hadron-hadron data gives 'soft' (or non-perturbative) Pomeron [Donnachie-Landshoff, hep-ph/9209205]:

$$\alpha_{\mathbb{P}}(t) = \alpha_{\mathbb{P}}(0) + \alpha'_{\mathbb{P}} t = 1.08 + (0.25 \text{ GeV}^{-2}) t.$$

- In pQCD, the 'hard' (or perturbative) Pomeron is a parton ladder, usually satisfying either BFKL evolution (strongly-ordered longitudinal momenta) or DGLAP evolution (strongly-ordered transverse momenta).
- Regge phenomenology useful in quantifying whether a process is 'soft' or 'hard'. 'Hard' processes have a higher effective $\alpha_{\mathbb{P}}(0)$, e.g., fit small- x_{Bj} HERA data to

$$\sigma_{\mathrm{tot}}^{\gamma^* p}(\mathsf{x}_{\mathrm{Bj}}, Q^2) = c(Q^2) \, \mathsf{x}_{\mathrm{Bj}}^{-\lambda_{\mathrm{tot}}(Q^2)}, \quad \text{where} \quad \lambda_{\mathrm{tot}} = \alpha_{\mathbb{P}}(0) - 1.$$

 Open question: how to unify 'soft' and 'hard' Pomerons? Insight from gauge/string duality [e.g. Brower–Polchinski–Strassler–Tan, hep-th/0603115]?



Some introductory references

- Proceedings of "HERA and the LHC: A Workshop on the implications of HERA for LHC physics" [hep-ph/0601013].
 - See in particular: M. Arneodo and M. Diehl, "Diffraction for non-believers" [hep-ph/0511047].
 - Ongoing meetings: see http://www.desy.de/~heralhc/.
- L. Frankfurt, M. Strikman and C. Weiss, "Small-x physics: From HERA to LHC and beyond", Ann. Rev. Nucl. Part. Sci. 55, 403 (2005) [hep-ph/0507286].
- B. Z. Kopeliovich, I. K. Potashnikova and I. Schmidt, "Diffraction in QCD", hep-ph/0604097.
- Textbooks:
 - V. Barone and E. Predazzi, "High-energy particle diffraction", Heidelberg, Germany: Springer-Verlag (2002).
 - J. R. Forshaw and D. A. Ross, "Quantum chromodynamics and the Pomeron", Cambridge, UK: Univ. Pr. (1997).

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Collinear factorization for exclusive hard processes Collins, Frankfurt, Strikman [hep-ph/9611433]:

$$\mathcal{A}(\gamma_L^* p \to V p) = \sum_{i,j} \int_0^1 \mathrm{d}z \int \mathrm{d}x_1 \underbrace{f_{i/p}(x_1, x - x_1, t; \mu)}_{f_{i/p}(x_1, x - x_1, t; \mu)} \underbrace{\mathsf{H}_{ij}(x_1, x, z, Q^2; \mu)}_{\mathsf{H}_{ij}(x_1, x, z, Q^2; \mu)} \underbrace{\mathsf{Meson \ dist. amp.}}_{\phi_j^V(z, \mu)}$$

+ power-suppressed corrections.



Kinematic variables:

- Label 4-momenta of photon, incoming proton, and outgoing proton by *q*, *p*, and *p'*.
- Photon virtuality, $q^2 = -Q^2$.
- $\gamma^* p$ center-of-mass energy squared, $W^2 = (p+q)^2$.

•
$$x_{\rm Bj} = Q^2/(2p \cdot q) \simeq Q^2/(Q^2 + W^2).$$

•
$$t = (p - p')^2$$
.

Alternative approach valid at high-energy (small- $x_{\rm Bj}$) is the dipole picture: $\mathcal{A}(\gamma^* p \to V p) \sim (\text{photon wave function}) \cdot (\text{dipole cross section}) \cdot (\text{meson wave function}).$

Exclusive processes at HERA within the dipole picture

Kowalski, Motyka, G.W. [hep-ph/0606272]

Munier, Staśto, Mueller [hep-ph/0102291]

Kowalski, Teaney [hep-ph/0304189]

$$\mathcal{A}(\gamma^* p \to E p) = \int \mathrm{d}^2 \mathbf{r} \, \int_0^1 \frac{\mathrm{d}z}{4\pi} \, \Psi^*(\gamma^* \to q\bar{q}) \, \mathcal{A}(q\bar{q} + p \to q\bar{q} + p) \, \Psi(q\bar{q} \to E),$$

where $E = \gamma^*$ (inclusive DIS), $E = \gamma$ (DVCS) or E = V (vector meson production).



- z = photon's light-cone momentum fraction.
- **r** = transverse dipole size.
- $t = (p p')^2 = -\Delta^2$.
- b = impact parameter: Fourier conjugate variable to Δ.

• Elastic amplitude for $q\bar{q}$ dipole scattering on the proton:

$$\begin{split} \mathcal{A}(q\bar{q}+p\to q\bar{q}+p) &= \\ &\mathrm{i} \int \mathrm{d}^2 \mathbf{b} \; \mathrm{e}^{-\mathrm{i}\mathbf{b}\cdot\mathbf{\Delta}} \, 2 \left[1-S(x,r,b)\right]. \end{split}$$

• Dipole cross section from optical theorem:

$$\begin{split} \sigma_{q\bar{q}}(x,r) &= \mathrm{Im} \ \mathcal{A}(q\bar{q}+p \to q\bar{q}+p)|_{\Delta=0} \\ \Rightarrow \quad \frac{\mathrm{d}\sigma_{q\bar{q}}}{\mathrm{d}^{2}\mathbf{b}} &= 2[1-\mathrm{Re}\,\mathcal{S}(x,r,b)]. \end{split}$$

(Will take S-matrix to be predominantly real.)

Dipole picture in the non-forward direction

Bartels, Golec-Biernat, Peters (BGBP) [hep-ph/0301192]



- Non-forward photon impact factor calculated in the high-energy limit.
- Transform from momentum space to coordinate space $(\mathbf{k} \rightarrow \mathbf{r})$, then to impact parameter space $(\mathbf{\Delta} \rightarrow \mathbf{b})$.
- Results obtained in color dipole picture: amplitude factorizes into (wave function).(dipole cross section).(wave function).
- Non-forward wave functions can be written as forward wave functions multiplied by $\exp[\pm i(1-z)\mathbf{r} \cdot \mathbf{\Delta}/2]$.
- Effectively, the momentum transfer Δ should conjugate to $\mathbf{b} + (1-z)\mathbf{r}$, the transverse distance from the centre of the proton to one of the two quarks of the dipole, rather than to \mathbf{b} .

$$\mathcal{A}_{T,L}^{\gamma^* p \to Ep}(x, Q, \Delta) = \mathrm{i} \int \mathrm{d}^2 \mathbf{r} \int_0^1 \frac{\mathrm{d}z}{4\pi} \int \mathrm{d}^2 \mathbf{b} \; (\Psi_E^* \Psi)_{T,L} \; \mathrm{e}^{-\mathrm{i}[\mathbf{b} - (1-z)\mathbf{r}] \cdot \mathbf{\Delta}} \; \frac{\mathrm{d}\sigma_{q\bar{q}}}{\mathrm{d}^2 \mathbf{b}}$$

Inclusive DIS in the dipole picture

Total cross section for inclusive DIS is

$$\sigma_{T,L}^{\gamma^* p}(x,Q) = \operatorname{Im} \mathcal{A}_{T,L}^{\gamma^* p \to \gamma^* p}(x,Q,\Delta=0)$$

$$= \sum_{f} \int d^2 \mathbf{r} \int_0^1 \frac{dz}{4\pi} (\Psi^* \Psi)_{T,L}^f \sigma_{q\bar{q}}(x,r),$$

1-2

i.e. depends on dipole cross section integrated over impact parameter \mathbf{b} . The squared (forward) photon wave functions are calculable in pQCD:

$$\begin{split} (\Psi^*\Psi)_T^f &\equiv \frac{1}{2} \sum_{\substack{h,\bar{h}=\pm\frac{1}{2}\\\lambda=\pm 1}} \Psi^*_{h\bar{h},\lambda} \Psi_{h\bar{h},\lambda} = \frac{2N_c}{\pi} \alpha_{\rm em} e_f^2 \left\{ \left[z^2 + (1-z)^2 \right] \epsilon^2 K_1^2(\epsilon r) + m_f^2 K_0^2(\epsilon r) \right\}, \\ (\Psi^*\Psi)_L^f &\equiv \sum_{h,\bar{h}=\pm\frac{1}{2}} \Psi^*_{h\bar{h},\lambda=0} \Psi_{h\bar{h},\lambda=0} = \frac{8N_c}{\pi} \alpha_{\rm em} e_f^2 Q^2 z^2 (1-z)^2 K_0^2(\epsilon r), \end{split}$$

where $\epsilon^2 \equiv z(1-z)Q^2 + m_f^2$ and $K_{0,1}$ are modified Bessel functions.

DVCS and exclusive diffractive vector meson production

$$\mathcal{A}_{T,L}^{\gamma^* p \to Ep}(x, Q, \Delta) = \mathrm{i} \int \mathrm{d}^2 \mathbf{r} \int_0^1 \frac{\mathrm{d}z}{4\pi} \int \mathrm{d}^2 \mathbf{b} \, (\Psi_E^* \Psi)_{T,L} \, \mathrm{e}^{-\mathrm{i}[\mathbf{b} - (1-z)\mathbf{r}] \cdot \Delta} \, \frac{\mathrm{d}\sigma_{q\bar{q}}}{\mathrm{d}^2 \mathbf{b}},$$

where $E = \gamma$ (DVCS) or E = V (vector meson production). The differential cross sections are then obtained from



$$\frac{\mathrm{d}\sigma_{T,L}^{\gamma^* p \to Ep}}{\mathrm{d}t} = \frac{1}{16\pi} \left| \mathcal{A}_{T,L}^{\gamma^* p \to Ep} \right|^2 [1 + \tan^2(\pi\lambda/2)], \quad \text{with} \quad \lambda \equiv \frac{\partial \ln\left(\mathcal{A}_{T,L}^{\gamma^* p \to Ep}\right)}{\partial \ln(1/x)}$$

For DVCS,

$$(\Psi_{\gamma}^*\Psi)_T^f = \frac{2N_c}{\pi} \alpha_{\rm em} e_f^2 \left\{ \left[z^2 + (1-z)^2 \right] \epsilon K_1(\epsilon r) m_f K_1(m_f r) + m_f^2 K_0(\epsilon r) K_0(m_f r) \right\}.$$

For vector meson production, however, some modeling of the wave functions, Ψ_V , is required. Constraints from normalization and experimental decay width. Will consider two alternatives denoted "Gaus-LC" and "boosted Gaussian" (see hep-ph/0606272 for details).

Review of (selected) dipole cross sections

$$\frac{\mathrm{d}\sigma_{q\bar{q}}}{\mathrm{d}^2\mathbf{b}} = 2[1 - \operatorname{Re} S(x, r, b)] \equiv 2\mathcal{N}(x, r, b),$$

where $\mathcal{N} \in [0, 1]$ and $\mathcal{N} = 1$ is the unitarity limit. First dipole models were integrated over **b** assuming proton is a disc in transverse plane:

 $\mathcal{N}(x, r, b) = \mathcal{N}(x, r) \Theta(b_{S} - b) \Rightarrow \sigma_{q\bar{q}}(x, r) = \sigma_{0}\mathcal{N}(x, r) \text{ with } \sigma_{0} = 2\pi b_{S}^{2}.$ Golec-Biernat–Wüsthoff (GBW) [hep-ph/9807513]:

$$\mathcal{N}(x,r) = 1 - e^{-r^2 Q_s^2(x)/4}$$
, where $Q_s^2(x) = (x_0/x)^{\lambda} \text{ GeV}^2$.

Decrease of $\lambda_{\rm tot}$ with decreasing ${\it Q}^2$ entirely due to saturation effects.

Bartels-Golec-Biernat-Kowalski (BGBK) [hep-ph/0203258]:

 $\mathcal{N}(x,r) = 1 - \exp\left[-\pi^2 r^2 \alpha_s(\mu^2) x g(x,\mu^2)/(3\sigma_0)\right]$

DGLAP evolution of gluon distribution. Charm neglected.

lancu-Itakura-Munier (CGC) [hep-ph/0310338]:

$$\mathcal{N}(x,r) = \begin{cases} \mathcal{N}_0 \left(\frac{rQ_s}{2}\right)^{2\left(\gamma_s + \frac{1}{\kappa\lambda Y} \ln \frac{2}{rQ_s}\right)} & : \quad rQ_s \leq 2, \\ 1 - \mathrm{e}^{-A \ln^2(BrQ_s)} & : \quad rQ_s > 2 \end{cases}$$

where $Y = \ln(1/x)$, $\gamma_s = 0.63$, $\kappa = 9.9$. Approximate solution of Balitsky–Kovchegov equation (sums 'fan' diagrams). Charm neglected.

Impact parameter dependent dipole cross sections

Kowalski-Teaney [hep-ph/0304189] used the Glauber-Mueller dipole cross section:



$$\mathcal{N}(x,r,b) = 1 - \exp\left(-\frac{\pi^2}{2N_c}r^2\alpha_5(\mu^2)xg(x,\mu^2)T(b)\right),$$

where $\mu^2 = 4/r^2 + \mu_0^2$. Gluon density, $xg(x, \mu^2)$, is evolved from a scale μ_0^2 up to μ^2 using LO DGLAP evolution without quarks:

$$\frac{\partial xg(x,\mu^2)}{\partial \ln \mu^2} = \frac{\alpha_{\rm S}(\mu^2)}{2\pi} \int_x^1 \mathrm{d}z \ P_{\rm gg}(z) \frac{x}{z} g\left(\frac{x}{z},\mu^2\right).$$

- Initial gluon density taken in the form $xg(x, \mu_0^2) = A_g x^{-\lambda_g} (1-x)^{5.6}$.
- Take $x = x_{\rm Bj}$ for light quarks, $x = x_{\rm Bj}(1 + 4m_c^2/Q^2)$ for charm quarks, and $x = x_{\rm Bj}(1 + M_V^2/Q^2)$ for vector meson production. Will use quark masses $m_{u,d,s} = 0.14$ GeV and $m_c = 1.4$ GeV.
- Exclusive processes: xg(x, µ²) → R_gxg(x, µ²) accounts for skewness of gluon distribution in the limit that x' ≪ x ≪ 1, where [Shuvaev et al., hep-ph/9902410]

$$R_g(\lambda) = \frac{2^{2\lambda+3}}{\sqrt{\pi}} \frac{\Gamma(\lambda+5/2)}{\Gamma(\lambda+4)}, \quad \text{with} \quad \lambda \equiv \frac{\partial \ln\left[xg(x,\mu^2)\right]}{\partial \ln(1/x)}$$

Impact parameter dependent dipole cross sections

"b-Sat" model

$$\mathcal{N}(x,r,b) = 1 - \exp\left(-\frac{\pi^2}{2N_c}r^2\alpha_5(\mu^2)xg(x,\mu^2)\mathcal{T}(b)\right)$$

Assume T(b) to have a Gaussian form:

$$T(b) = rac{1}{2\pi B_G} \exp\left(-rac{b^2}{2B_G}
ight),$$

where $B_G = 4 \text{ GeV}^{-2}$ from description of vector meson *t*-distributions.



"b-CGC" model

$$\mathcal{N}(x,r,b) = \begin{cases} \mathcal{N}_0 \left(\frac{rQ_s}{2}\right)^{2\left(\gamma_s + \frac{1}{r\lambda Y} \ln \frac{2}{rQ_s}\right)} & : & rQ_s \leq 2\\ 1 - e^{-A \ln^2(BrQ_s)} & : & rQ_s > 2 \end{cases}$$

where

$$Q_s \equiv Q_s(x,b) = \left(\frac{x_0}{x}\right)^{\frac{\lambda}{2}} \left[\exp\left(-\frac{b^2}{2B_{\rm CGC}}\right)\right]^{\frac{1}{2\gamma_s}},$$

and $B_{\rm CGC} = 5.5 \ {\rm GeV^{-2}}$ from description of vector meson *t*-distributions.

Fits to the total DIS cross section

Determine parameters in dipole cross section from fits to ZEUS $\sigma_{\text{tot}}^{\gamma^* p}(x_{\text{Bj}}, Q^2)$ data with $x_{\text{Bj}} \leq 0.01$:

Model	$Q^2/{ m GeV^2}$	μ_0^2/GeV^2	Ag	λ_g	χ^2 /d.o.f.
b-Sat	[0.25,650]	1.17	2.55	0.020	193.0/160 = 1.21
Model	$Q^2/{ m GeV^2}$	\mathcal{N}_0	$x_0/10^{-4}$	λ	χ^2 /d.o.f.

b-Sat model better than b-CGC model.

Model	$Q^2/{ m GeV^2}$	Charm?	$\sigma_0/{ m mb}$	$x_0/10^{-4}$	λ	χ^2 /d.o.f.
GBW	[0.25,45]	No	20.1	5.16	0.289	216.5/130 = 1.67
GBW	[0.25,45]	Yes	23.9	1.11	0.287	204.9/130 = 1.58
GBW	[0.25,650]	Yes	22.5	1.69	0.317	414.4/160 = 2.59
CGC	[0.25,45]	No	25.8	0.263	0.252	117.2/130 = 0.90
CGC	[0.25,45]	Yes	35.7	0.00270	0.177	116.8/130 = 0.90
CGC	[0.25,650]	Yes	34.5	0.00485	0.188	173.7/160 = 1.09

GBW model gives a relatively poor description; CGC better. Inclusion of data at larger Q^2 worsens fit: need DGLAP evolution. Presence of charm important.

The saturation scale Q_5^2

Define saturation scale $Q_S^2 \equiv 2/r_S^2$, where r_S^2 is the dipole size where

$$\mathcal{N} = 1 - e^{-1/2} \simeq 0.4.$$

(This definition of the saturation scale coincides with $Q_s^2 = (x_0/x)^{\lambda}$ GeV² in the GBW model, but is **not** equal to Q_s^2 in the CGC and b-CGC models.)





- DGLAP evolution, presence of charm, impact parameter dependence: all lower saturation scale.
- Median b ≃ 2.6 GeV⁻¹ ⇒ saturation effects not important for inclusive DIS in HERA kinematic regime.
- Detailed study of multiple interactions in b-Sat model by H. Kowalski [HERA–LHC proceedings, hep-ph/0601013]. Multiple scattering enhanced for large dipole sizes with b ≈ 0.



Description of HERA vector meson data in the b-Sat model

- Input gluon density fitted to $\sigma_{\rm tot}^{\gamma^* p}$ data.
- Parameter $B_G = 4 \text{ GeV}^{-2}$ giving width of Gaussian T(b) chosen to give best overall description of vector meson *t*-distributions.



t-slope parameter B_D

 $\gamma^* \mathbf{p} \rightarrow \mathbf{J}/\psi \mathbf{p}$

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H1 (40 < W < 160 GeV)
 ZEUS (W = 90 GeV)
 Boosted Gaussian Ψ_V
 Gaus-LC Ψ_V

 $Q^2 + M_{J/w}^2$ (GeV²)

B_b (GeV⁻²)

t-dependence of exclusive processes at HERA are well described by an exponential form:

$$\frac{\mathrm{d}\sigma^{\gamma^* p \to E p}}{\mathrm{d}t} \propto \mathrm{e}^{-B_D |t|},$$

where B_D is process dependent, but approaches a universal value at large $(Q^2 + M_V^2)$.

B_b (GeV⁻²

 $\gamma^* \mathbf{p} \rightarrow \phi \mathbf{p}$

ZEUS

..... Gaus-LC Ψ,

Boosted Gaussian Ψ_{v}

 $10 Q^2 + M_{\perp}^2 (GeV^2)$

W = 75 GeV



Transverse proton shape T(b)

• In limit of small dipole sizes:

$$T(b) = \frac{1}{2\pi B_{\mathcal{G}}} \exp\left(-\frac{b^2}{2B_{\mathcal{G}}}\right) \quad \Rightarrow \quad \frac{\mathrm{d}\sigma^{\gamma^* p \to Ep}}{\mathrm{d}t} \propto \left|\int \mathrm{d}^2 \mathbf{b} \, \mathrm{e}^{-\mathrm{i}\mathbf{b}\cdot\mathbf{\Delta}} \, T(b)\right|^2 \propto \mathrm{e}^{-B_{\mathcal{G}}|t|},$$

so $B_D = B_G = 4 \text{ GeV}^{-2}$ and $\sqrt{\langle b^2 \rangle} = \sqrt{2B_G} = 0.56 \text{ fm}.$

- cf. proton charge radius 0.870 \pm 0.008 fm [PDG].
- However, important modifications to B_D for finite dipole sizes due to eikonalization and BGBP factor, $\exp[i(1 z)\mathbf{r} \cdot \mathbf{\Delta}]$, in amplitude:



Alternative proton shape: step T(b)

$$T(b) = \frac{1}{\pi b_S^2} \Theta(b_S - b),$$

with
$$b_S = 4 \text{ GeV}^{-1} \Rightarrow \langle b^2 \rangle = b_S^2/2 = 8 \text{ GeV}^{-2}$$
.



- Assume a step T(b) instead of a Gaussian. Recall that this is implicitly assumed in *b*-independent dipole models (e.g. GBW, CGC).
- t-distribution from step T(b) not supported by J/ψ data.





W dependence of exclusive diffractive vector meson data



 Good agreement of b-Sat model with HERA data in both shape and normalization.

'Soft' vs. 'hard' Pomeron from W dependence

- Fit $\sigma \propto W^{\delta}$. In language of Regge theory, $\delta = 4[\alpha_{\mathbb{P}}(\langle t \rangle) - 1]$, where $\alpha_{\mathbb{P}}(\langle t \rangle) = \alpha_{\mathbb{P}}(0) - \alpha'_{\mathbb{P}}/B_D$, and $\delta \simeq 0.2$ corresponds to the 'soft' Pomeron.
- Fit $d\sigma/dt \propto W^{4[\alpha_{\mathbb{P}}(t)-1]}$, where $\alpha_{\mathbb{P}}(t) = \alpha_{\mathbb{P}}(0) + \alpha'_{\mathbb{P}} t$.

	$\alpha_{\mathbb{P}}(0)$	$\alpha'_{\mathbb{P}}$ (GeV ⁻²)
H1 $\gamma p \rightarrow J/\psi p$	1.22 ± 0.02	0.16 ± 0.04
ZEUS $\gamma p \rightarrow J/\psi p$	1.20 ± 0.01	0.12 ± 0.02
H1 $\gamma p \rightarrow \rho p$	1.09 ± 0.01	0.12 ± 0.05
ZEUS $\gamma p \rightarrow \rho p$	1.10 ± 0.02	0.13 ± 0.04
Donnachie–Landshoff	1.08	0.25

- *ρ* photoproduction is a 'soft' process: α_ℙ(0) compatible with 'soft' Pomeron value of 1.08.
- α'_P in γp only half value in pp, due to stronger absorptive effects in pp.
- J/ψ photoproduction is a 'hard' process: larger $\alpha_{\mathbb{P}}(0)$ but similar $\alpha'_{\mathbb{P}}$ compared to ρ photoproduction.







Q^2 dependence of exclusive diffractive vector meson data



• Again, good agreement of b-Sat model with HERA data in both shape and normalization.

σ_L/σ_T of exclusive diffractive vector meson data



• σ_L/σ_T sensitive to details of the vector meson wave functions.

 $\alpha'_{\mathbb{P}}$ from b-Sat and b-CGC models $B_D = B_0 + 4\alpha'_{\mathbb{P}}\ln(W/W_0)$



- The b-Sat model gives a much better overall description of both the total DIS cross section and exclusive processes than the b-CGC model.
- However, the b-Sat model predicts $\alpha'_{\mathbb{P}} \approx 0$ due to the assumed factorisation of T(b) from $xg(x, \mu^2)$, and the small saturation effects.
- In the b-CGC model, the W (or x) dependence is not factorized from the b dependence, therefore an appreciable α'_P is achievable.

Deeply virtual Compton scattering at HERA



- DVCS (γ*p → γp) is a much cleaner process to describe theoretically than exclusive vector meson production.
- Predicted *t*-slope $B_D = 5.29 \text{ GeV}^{-2}$ from b-Sat model slightly underestimates experimental value of $B_D = 6.02 \pm 0.52 \text{ GeV}^{-2}$.
- Good agreement of b-Sat model with data for Q² and W distributions in both shape and normalisation.

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Diffractive DIS kinematics



Diffractive reduced cross section $\sigma_r^{D(3)}$

• Diffractive cross section (integrated over *t*):

$$\frac{\mathrm{d}^{3}\sigma^{\mathrm{D}}}{\mathrm{d}\mathbf{x}_{\mathbb{P}}\,\mathrm{d}\beta\,\mathrm{d}Q^{2}} = \frac{2\pi\alpha_{\mathrm{em}}^{2}}{\beta\,Q^{4}}\,\left[1+(1-y)^{2}\right]\,\sigma_{r}^{\mathrm{D}(3)}(\mathbf{x}_{\mathbb{P}},\beta,Q^{2}),$$

where $y = Q^2/(x_{\rm\scriptscriptstyle Bj}s)$, $s = 4 E_e E_p$, and

$$\sigma_r^{\mathrm{D}(3)} = F_2^{\mathrm{D}(3)} - \frac{y^2}{1 + (1 - y)^2} F_L^{\mathrm{D}(3)} \approx F_2^{\mathrm{D}(3)}(\mathbf{x}_{\mathbb{P}}, \beta, Q^2),$$

for small y or assuming that ${\it F}_L^{{\rm D}(3)} \ll {\it F}_2^{{\rm D}(3)}$

• Measurements of $\sigma_r^{D(3)} \Rightarrow diffractive$ parton density functions (DPDFs) $a^{D}(\mathbf{x}_{\mathbb{P}}, z, Q^{2}) = zq^{D}(\mathbf{x}_{\mathbb{P}}, z, Q^{2})$ or $zg^{D}(\mathbf{x}_{\mathbb{P}}, z, Q^{2})$, where $\beta \leq z \leq 1$, cf. $x_{Bj} \leq x \leq 1$ in DIS.

Recent measurements of DDIS using three methods

- Detect leading proton. No proton dissociation background. Can measure t-dependence. Higher x_P accessible. But low statistics due to poor acceptance. Both Pomeron (P) and secondary Reggeon (R) contributions. [ZEUS LPS: hep-ex/0408009, H1 FPS: hep-ex/0606003]
- 2 Look for Large Rapidity Gap (LRG). (Non-diffractive contribution is exponentially suppressed as a function of the gap size.) Proton dissociation background (H1: $M_Y < 1.6$ GeV). Used in all final-state DDIS measurements (e.g. dijet and D^* meson production). Both \mathbb{P} and \mathbb{R} contributions. [H1 LRG: hep-ex/0606004]

$$\frac{\mathrm{d}N}{\mathrm{d}\ln M_X^2} = D + \underbrace{c \exp(b \ln M_X^2)}_{\text{non-diffractive}}$$

Proton dissociation background (ZEUS: $M_Y < 2.3$ GeV). Motivated by Regge theory assuming $M_X^2 \gg Q^2$, $\alpha_{\mathbb{P}}(0) \approx \alpha_{\mathbb{P}}(\langle t \rangle) \approx 1$, and neglecting \mathbb{P} - \mathbb{R} interference. Validity in general? [ZEUS M_X : hep-ex/0501060]



Comparison of H1 LRG with other data sets





- H1 FPS and ZEUS LPS scaled to M_Y < 1.6 GeV by an overall factor 1.23: good agreement with H1 LRG.
- ZEUS M_X scaled to M_Y < 1.23 by an overall factor 0.86. Difference expected at large x_P due to lack of ℝ contribution. However, some difference in Q² dependence even at low x_P ⇒ diffractive gluon density extracted from ZEUS M_X data roughly half gluon density from H1 LRG data.

Leading-twist collinear factorization in DDIS

$$F_2^{\mathrm{D}(3)} = \sum_{a=q,g} C_{2,a} \otimes a^{\mathrm{D}} + \text{power-suppressed corrections, (1)}$$

where $C_{2,a}$ are the **same** coefficient functions as in inclusive DIS. The DPDFs $a^{D} = zq^{D}$ or zg^{D} satisfy DGLAP evolution:

$$\frac{\partial a^{\mathrm{D}}}{\partial \ln Q^2} = \sum_{a'=q,g} P_{aa'} \otimes a'^{\mathrm{D}}$$
(2)



"The factorization theorem applies when Q is made large while x_{Bj} , $x_{\mathbb{P}}$, and t are held fixed." [Collins, hep-ph/9709499]

- Says little about the mechanism for diffraction: information about the diffractive exchange ('Pomeron') needs to be parameterized at an input scale Q_0 and fit to data. Will show later that assuming a perturbative Pomeron contribution, we need to modify both (1) and (2).
- Factorization should also hold for final states (jets etc.) in DDIS, but is broken in hadron-hadron collisions, although hope that same formalism can be applied with extra suppression factor calculable from eikonal models (more later).

LO diffractive dijet photoproduction: resolved photon contribution should be suppressed, but direct photon contribution unsuppressed. Complications at NLO [Klasen–Kramer, hep-ph/0506121].



H1 2006 extraction of DPDFs [hep-ex/0606004]

• Assume Regge factorization [Ingelman–Schlein,'85]:

$$a^{\mathrm{D}}(x_{\mathbb{P}}, z, Q^2) = f_{\mathbb{P}}(x_{\mathbb{P}}) a^{\mathbb{P}}(z, Q^2)$$
(3)

• Pomeron flux factor from Regge phenomenology:

$$f_{\mathbb{P}}(x_{\mathbb{P}}) = \int_{t_{\rm cut}}^{t_{\rm min}} \mathrm{d}t \, \mathrm{e}^{B_{\mathbb{P}} t} \, x_{\mathbb{P}}^{1-2\alpha_{\mathbb{P}}(t)} \qquad (\alpha_{\mathbb{P}}(t) = \alpha_{\mathbb{P}}(0) + \alpha'_{\mathbb{P}} t)$$

"Regge factorization relates the power of $x_{\mathbb{P}}$ measured in DDIS to the power of *s* measured in hadron-hadron elastic scattering." [Collins, hep-ph/9709499]

- Fit to H1 FPS data gives $\alpha_{\mathbb{P}}(t) = 1.11 + 0.06 t$. Fit to H1 LRG data gives $\alpha_{\mathbb{P}}(0) = 1.12$ if $\alpha'_{\mathbb{P}} = 0.06$, or $\alpha_{\mathbb{P}}(0) = 1.15$ if $\alpha'_{\mathbb{P}} = 0.25$.
- So the Pomeron in DDIS is **not** the 'soft' Pomeron with $\alpha_{\mathbb{P}}(t) = 1.08 + 0.25 t$. By Collins' definition, Regge factorization is broken. H1 assume that the $x_{\mathbb{P}}$ dependence factorizes as eq.(3) regardless, with the fitted $\alpha_{\mathbb{P}}(0)$ independent of β and Q^2 . However, this $x_{\mathbb{P}}$ factorization is also broken, see later.

H1 2006 extraction of DPDFs

hep-ex/0606004

• Pomeron PDFs $a^{\mathbb{P}}(z, Q^2) = z\Sigma^{\mathbb{P}}(z, Q^2)$ or $zg^{\mathbb{P}}(z, Q^2)$ are DGLAP-evolved from arbitrary inputs at $Q_0^2 \simeq 2 \text{ GeV}^2$:

$$a^{\mathbb{P}}(z, Q_0^2) = A_a z^{B_a} (1-z)^{C_a} e^{-\frac{0.01}{1-z}}$$

- Secondary Reggeon contribution with $\alpha_{\mathbb{R}}(0) = 0.50$ included using pion PDFs. Normalisation fitted to data.
- Fit to H1 LRG data with M_X ≥ 2 GeV and Q² ≥ 8.5 GeV² (190 data points).
- H1 2006 Fit A: fix $B_g = 0$ $\Rightarrow \chi^2 = 158.$

• H1 2006 Fit B: fix
$$B_g = 0$$
 and $C_g = 0$
 $\Rightarrow \chi^2 = 164$.



- Also, combined fit of inclusive DDIS data with diffractive dijet data [H1prelim-06-011].
- Constrains gluon density at z = z_ℙ directly, rather than indirectly from scaling violations.
- Dijet cross sections calculated using NLOJET++ by Z. Nagy.

H1 2006 extraction of DPDFs



 Dijet z_P distribution mainly constains z dependence of g^D.



 Cut of Q² ≥ 8.5 GeV² needed to achieve stable fit.

H1 2006 extraction of DPDFs



- Gluon density smaller at high z on inclusion of the dijet data.
- χ^2 for inclusive DDIS data increases from 158 (H1 Fit A) to 169 (H1 combined fit).
- Suggests some tension between inclusive DDIS and dijet data using this approach. Gluon determined directly from dijet data different from gluon determined indirectly from scaling violations of inclusive DDIS data.
- How reliable is the theory used in these fits?

Alternative approach: two-gluon exchange calculations



Two-gluon exchange calculations are the basis for the color dipole model description of DDIS.

ZEUS 1994



- Right: x_ℙF₂^{D(3)} for x_ℙ = 0.0042 as a function of β
 [Golec-Biernat-Wüsthoff, hep-ph/9903358].
 - dotted lines: $\gamma_T^* \rightarrow q\bar{q}g$,
 - dashed lines: $\gamma_T^* \rightarrow q\bar{q}$,
 - dot-dashed lines: $\gamma_L^* \to q \bar{q}$,

important at low, medium, and high β respectively.

• $\gamma_T^* \rightarrow q\bar{q}g$ and $\gamma_T^* \rightarrow q\bar{q}$ are partly higher-twist, $\gamma_L^* \rightarrow q\bar{q}$ is **purely** higher-twist, but H1 DPDFs only include leading-twist contributions.

Comparison of two approaches

'Regge factorization' approach

- \mathbb{P} is purely non-perturbative, i.e. a Regge pole.
- Q^2 dependence given by DGLAP.
- Need to fit β dependence.
- x_ℙ dependence taken as a power law, with the power either taken from soft hadron data or fitted.
- $x_{\mathbb{P}}$ dependence factorizes.
- Only leading-twist.
- Full DGLAP evolution in Pomeron structure function.
- Extract universal DPDFs.
- Only applies to inclusive DDIS.

Two-gluon exch. (e.g. dipole model)

- P is purely perturbative, i.e. a gluon ladder.
- Q^2 dependence predicted.
- β dependence predicted.
- x_ℙ dependence given by square of skewed gluon density (or dipole cross section).
- $x_{\mathbb{P}}$ dependence doesn't factorize.
- Goes beyond leading-twist.
- Only $q\bar{q}$ and $q\bar{q}g$ final states as products of photon dissociation.
- No concept of DPDFs.
- Also explains exclusive processes.

Is inclusive DDIS 'soft' or 'hard'?

	B_D (GeV ⁻²)	$lpha_{\mathbb{P}}(0)$	$lpha'_{\mathbb{P}}$ (GeV $^{-2}$)
ZEUS LPS	$7.9^{+1.0}_{-0.7}$	1.16 ± 0.3	0.25 (assumed)
H1 FPS	6	$1.11\substack{+0.05\\-0.03}$	$0.06^{+0.19}_{-0.06}$
H1 LRG	—	$1.12^{+0.03}_{-0.01}$	0.06 (assumed)
H1 combined fit	—	1.15	0.06 (assumed)
cf. $\gamma p \rightarrow \rho p$	~ 10	~ 1.09	~ 0.12
cf. $\gamma p \rightarrow J/\psi p$	\sim 4	~ 1.20	~ 0.12

Is inclusive DDIS 'soft' or 'hard'?

- Inclusive DDIS is harder than exclusive ρ photoproduction, but softer than exclusive J/ψ photoproduction (and softer than inclusive DIS at the same Q²).
- Above α_P(0) values are averaged over β and Q². Perturbative Pomeron contribution should break x_P factorization to some degree.
- Left plot: ZEUS M_X data show rise of α_P(0) with Q².
 Middle plot: H1 LRG data show constant α_P(0) when averaged over β or Q².
 Right plot (G.W.): H1 LRG data show rise of α_P(0) with Q² in some β bins.



Combination of two approaches

Martin, Ryskin, G.W. [hep-ph/0406224, hep-ph/0504132, hep-ph/0511333]

 In reality, both non-perturbative and perturbative Pomeron contributions to inclusive DDIS. Improve two-gluon exchange calculations by introducing DGLAP evolution in 'Pomeron structure function' allowing universal DPDFs to be extracted.

Non-perturbative ${\mathbb P}$ contribution

- P is purely partly non-perturbative, i.e. a Regge pole.
- Q^2 dependence given by DGLAP.
- Need to fit β dependence.
- x_P dependence taken as a power law, with the power either taken from soft hadron data or fitted.
- $x_{\mathbb{P}}$ dependence factorizes.
- Only leading-twist.
- Full DGLAP evolution in Pomeron structure function.
- Extract universal DPDFs.
- Only applies to inclusive DDIS.

Perturbative \mathbb{P} contribution

- P is purely partly perturbative, i.e. a gluon ladder.
- Q^2 dependence predicted.
- β dependence predicted.
- x_ℙ dependence given by square of skewed gluon density (or dipole cross section).
- $x_{\mathbb{P}}$ dependence doesn't factorize.
- Goes beyond leading-twist.
- Full DGLAP evolution in Pomeron structure function.
- Extract universal DPDFs.
- Also explains exclusive processes.

Perturbative Pomeron contribution to DDIS

- Generalize $\gamma^* \rightarrow q\bar{q}$ and $\gamma^* \rightarrow q\bar{q}g$ to arbitrary number of parton emissions [Ryskin,'90; Levin–Wüsthoff,'94].
- Work in Leading Logarithmic Approximation (LLA) \Rightarrow virtualities of *t*-channel partons are strongly ordered: $\mu_0^2 \ll \ldots \ll \mu^2 \ll \ldots \ll Q^2$, i.e. pQCD Pomeron is a DGLAP ladder rather than a BFKL ladder.



 New feature: integral over scale μ² (starting scale for DGLAP evolution of Pomeron PDFs).

$$\begin{split} F_2^{\mathrm{D}(3)} &= \int_{\mu_0^2}^{Q^2} \frac{\mathrm{d}\mu^2}{\mu^2} f_{\mathbb{P}}(x_{\mathbb{P}};\mu^2) F_2^{\mathbb{P}}(\beta,Q^2;\mu^2) \\ f_{\mathbb{P}}(x_{\mathbb{P}};\mu^2) &= \frac{1}{x_{\mathbb{P}}B_D} \left[R_g \frac{\alpha_S(\mu^2)}{\mu} x_{\mathbb{P}}g(x_{\mathbb{P}},\mu^2) \right]^2 \\ F_2^{\mathbb{P}}(\beta,Q^2;\mu^2) &= \sum_{a=q,g} C_{2,a} \otimes a^{\mathbb{P}} \end{split}$$

 $(B_D \text{ from } t\text{-integration}, R_g \text{ from skewness})$

- Pomeron PDFs $a^{\mathbb{P}}(z, Q^2; \mu^2)$ DGLAP-evolved from an input scale μ^2 up to Q^2 .
- For $\mu^2 < \mu_0^2 \sim 1$ GeV², replace lower parton ladder with usual Regge pole contribution. Take $\alpha_{\mathbb{P}}(0) \simeq 1.08$ (or fit) and fit Pomeron PDFs DGLAP-evolved from an input scale μ_0^2 .
- Important: scale that controls $x_{\mathbb{P}}$ dependence, e.g. effective $\alpha_{\mathbb{P}}(0)$, is μ^2 not Q^2 !

Gluonic and sea-quark Pomeron



- Pomeron structure function $F_2^{\mathbb{P}}(\beta, Q^2; \mu^2)$ calculated from quark singlet $\Sigma^{\mathbb{P}}(z, Q^2; \mu^2)$ and gluon $g^{\mathbb{P}}(z, Q^2; \mu^2)$ DGLAP-evolved from an input scale μ^2 up to Q^2 .
- Input Pomeron PDFs Σ^P(z, μ²; μ²) and g^P(z, μ²; μ²) to DGLAP evolution are Pomeron-to-parton splitting functions.

LO Pomeron-to-parton splitting functions



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• Notation: ' $\mathbb{P} = G$ ' means gluonic Pomeron, ' $\mathbb{P} = S$ ' means sea-quark Pomeron, ' $\mathbb{P} = GS$ ' means interference between these.

 LO Pomeron-to-parton splitting functions are [hep-ph/0504132]:

$$\begin{split} z\Sigma^{\mathbb{P}=G}(z,\mu^{2};\mu^{2}) &= P_{q,\mathbb{P}=G}(z) = z^{3} (1-z), \\ zg^{\mathbb{P}=G}(z,\mu^{2};\mu^{2}) &= P_{g,\mathbb{P}=G}(z) = \frac{9}{16} (1+z)^{2} (1-z)^{2}, \\ z\Sigma^{\mathbb{P}=S}(z,\mu^{2};\mu^{2}) &= P_{q,\mathbb{P}=S}(z) = \frac{4}{81} z (1-z), \\ zg^{\mathbb{P}=S}(z,\mu^{2};\mu^{2}) &= P_{g,\mathbb{P}=S}(z) = \frac{1}{9} (1-z)^{2}, \\ z\Sigma^{\mathbb{P}=GS}(z,\mu^{2};\mu^{2}) &= P_{q,\mathbb{P}=GS}(z) = \frac{2}{9} z^{2} (1-z), \\ zg^{\mathbb{P}=GS}(z,\mu^{2};\mu^{2}) &= P_{g,\mathbb{P}=GS}(z) = \frac{1}{4} (1+2z) (1-z)^{2} \end{split}$$

Evolve these input Pomeron PDFs from μ^2 up to ${\it Q}^2$ using NLO DGLAP evolution.

Contribution to $F_2^{\mathrm{D}(3)}$ as a function of μ^2

$$F_2^{\mathrm{D}(3)} = \int_{\mu_0^2}^{Q^2} \frac{\mathrm{d}\mu^2}{\mu^2} f_{\mathbb{P}}(x_{\mathbb{P}};\mu^2) F_2^{\mathbb{P}}(\beta,Q^2;\mu^2)$$
$$f_{\mathbb{P}}(x_{\mathbb{P}};\mu^2) = \frac{1}{x_{\mathbb{P}}B_D} \left[R_g \frac{\alpha_s(\mu^2)}{\mu} x_{\mathbb{P}}g(x_{\mathbb{P}},\mu^2) \right]^2$$

- Naïvely, f_P(x_P; μ²) ~ 1/μ², so contributions from large μ² are strongly suppressed.
- But x_Pg(x_P, μ²) ~ (μ²)^γ, where γ is the anomalous dimension. In BFKL limit γ ≃ 0.5, so f_P(x_P; μ²) ~ constant.
- HERA domain is in an intermediate region: γ is not small, but is less than 0.5.
- Upper plot: $\mu^2 x_{\mathbb{P}} f_{\mathbb{P}}(x_{\mathbb{P}}; \mu^2)$ is not flat for small $x_{\mathbb{P}}$. Lower plot: integrand as a function of μ^2 (using MRST2004F3 NLO PDFs) \Rightarrow large contribution from large μ^2 .
- Recall that fits using 'Regge factorization' include contributions from $\mu^2 \leq Q_0^2$ in the input densities, but neglect all contributions from $\mu^2 > Q_0^2$.





Inhomogeneous evolution of DPDFs

$$\begin{split} F_2^{\mathrm{D}(3)} &= \sum_{a=q,g} C_{2,a} \otimes a^{\mathrm{D}}, \\ \text{where } a^{\mathrm{D}}(x_{\mathbb{P}}, z, \mathbf{Q}^2) &= \int_{\mu_0^2}^{\mathbf{Q}^2} \frac{\mathrm{d}\mu^2}{\mu^2} f_{\mathbb{P}}(x_{\mathbb{P}}; \mu^2) \ a^{\mathbb{P}}(z, \mathbf{Q}^2; \mu^2) \\ \Rightarrow \frac{\partial a^{\mathrm{D}}}{\partial \ln \mathbf{Q}^2} &= \underbrace{\sum_{a'=q,g} P_{aa'} \otimes a'^{\mathrm{D}}}_{\mathrm{DGLAP \ term}} + \underbrace{f_{\mathbb{P}}(x_{\mathbb{P}}; \mathbf{Q}^2) P_{a\mathbb{P}}(z)}_{\mathrm{Extra \ inhomogeneous \ term}} \end{split}$$

• Inhomogeneous evolution of DPDFs is not a new idea:

"We introduce a diffractive dissociation structure function and show that it obeys the DGLAP evolution equation, **but**, with an additional inhomogeneous term." [Levin–Wüsthoff, '94]

Pomeron structure is analogous to photon structure

Photon structure function



Diffractive structure function



Dijets in diffractive photoproduction



Analysis of H1 LRG data

Motivation: What impact do the perturbative Pomeron terms have on the H1 2006 DPDF analysis?

• Take input quark singlet and gluon densities at $Q_0^2 = 2 \text{ GeV}^2$ in the form:

$$\begin{split} z \Sigma^{\mathrm{D}}(x_{\mathbb{P}}, z, Q_0^2) &= f_{\mathbb{P}}(x_{\mathbb{P}}) \, A_q \, z^{B_q} (1-z)^{C_q}, \\ z g^{\mathrm{D}}(x_{\mathbb{P}}, z, Q_0^2) &= f_{\mathbb{P}}(x_{\mathbb{P}}) \, A_g \, z^{B_g} (1-z)^{C_g}. \end{split}$$

- f_P(x_P) as in the H1 2006 fit with α_P(0), A_a, B_a, and C_a (a = q, g) as free parameters.
- Work in Fixed Flavor Number Scheme: no heavy quark DPDFs.
- Treatment of secondary Reggeon as in H1 2006 fit, i.e. using pion PDFs, but using GRV NLO instead of Owens LO. (N.B.: No good reason that the \mathbb{R} PDFs should be same as pion PDFs.)
- Fit H1 LRG data binned at fixed $x_{\mathbb{P}}$ values with cut $M_X \ge 2$ GeV. Will study effect of cut $Q^2 \ge Q_{\min}^2$ on fitted data.
- Statistical and systematic experimental errors added in quadrature.
- Two types of fits:
 - "Regge" = 'Regge factorization' approach (i.e. no $C_{2,\mathbb{P}}$ or $P_{a\mathbb{P}}$) \simeq H1 2006 Fit A.
 - "pQCD" = 'perturbative QCD' approach with LO $C_{2,\mathbb{P}}$ and $P_{a\mathbb{P}}$.
- Use MRST2004F3 NLO PDFs with $\Lambda_{\rm QCD}^{(n_f=3)}=407$ MeV.

Stability with respect to Q_{\min}^2 variation

• Stability analysis following MRST [hep-ph/0308087].

Q_{\min}^2 (GeV ²)	3.5	5.0	6.5	8.5	12	15
Number of data points	266	239	214	190	164	141
$\chi^2(Q^2 \ge 3.5 \; ext{GeV}^2)$	272					
	262					
$\chi^2(Q^2 \geq 5~{ m GeV^2})$	233	222				
	225	219				
$\chi^2(Q^2 \geq 6.5~{ m GeV^2})$	208	186	174			
	205	200	189			
$\chi^2(Q^2\geq 8.5~{ m GeV^2})$	178	155	144	142		
	181	174	156	153		
$\chi^2({\it Q}^2 \geq 12~{ m GeV}^2)$	156	136	124	123	122	
	162	155	139	134	134	
$\chi^2({\it Q}^2 \geq 15~{ m GeV}^2)$	133	111	100	98	97	96
	138	130	112	106	104	103
Stability measure Δ_i^{i+1}	0.4	0 0.4	45 0 .	07 0	.03	0.04
,	0.2	0 0.4	42 0.	14 0	.03	0.06

• Both Regge and pQCD fits stable for $Q_{\min}^2 \gtrsim 6.5 \text{ GeV}^2$. To compare directly with H1 2006 fits, take $Q_{\min}^2 = 8.5 \text{ GeV}^2$.

DPDFs with $Q_{\min}^2 = 8.5 \text{ GeV}^2$ compared to H1 DPDFs



- Regge fit \simeq H1 2006 Fit A.
- pQCD fit closer to H1 combined fit than H1 2006 Fit A without including dijet data in fit ⇒ should describe dijet data better than H1 2006 Fit A.
- Suggests tension between inclusive DDIS and diffractive dijet data is alleviated by inclusion of perturbative Pomeron terms.

Direct Pomeron contribution to dijet production



- Direct Pomeron contribution $(z_{\mathbb{P}} = 1)$ calculated with ZEUS (prel.) kinematic cuts: 31% of data in largest β bin.
- Exclusive diffractive dijet contribution to inclusive diffractive dijet production is small in the HERA kinematic regime.
- H1 combined fit is to dijet data with z_P < 0.9 integrated over β. Therefore, safe to neglect direct Pomeron contribution and include only the resolved Pomeron contribution calculated using NLOJET++.
- Searches for exclusive dijets in progress at HERA by H1 and ZEUS.
- Alternative calculations for exclusive dijets using LO collinear factorization by Braun and Ivanov [hep-ph/0505263].

Predictions for diffractive charm production



- Direct Pomeron contribution, i.e. γ^{*} P → cc̄ (z_P = 1), is significant at moderate/high β.
- If the direct Pomeron contribution is neglected, the diffractive gluon density would need to be artificially large to fit the charm data.

Comment on the LRG method



 LRG method: event selection using cut on maximum (pseudo)rapidity η_{max} < η_{cut} = 3.3 [H1, hep-ex/0606004].

• Kinematics of
$$\mathbb P$$
 remnant:
 $E = p_t \cosh \eta_{\max} \simeq (1-z) x_{\mathbb P} E_p$

$$\Rightarrow p_t > (1-z) x_{\mathbb{P}} E_p \operatorname{sech} \eta_{\operatorname{cut}}.$$

- Therefore, strong cut on η_{\max} increases relative contribution to DDIS from perturbative Pomeron, i.e. large virtuality $\mu^2 \simeq p_t^2/(1-z) \gtrsim 1 \text{ GeV}^2$.
- Originally discussed by J. Ellis and G. Ross [hep-ph/9604360, hep-ph/9812385].
- In recent H1 measurements, effect of cut on η_{max} is compensated as part of acceptance corrections using RAPGAP event generator.
 - Pomeron remnant p_t [H1, hep-ex/0012051] and η_{max} distributions are well described by RAPGAP.
 - Good agreement of LRG data with leading-proton data.

Gives confidence that procedure is correct (although uncertainty due to acceptance correction for cut on η_{\max} is dominant uncertainty at high $x_{\mathbb{P}}$).

• Interesting experimental possibility to enhance perturbative Pomeron contribution by event selection with a strong cut on η_{max} .

Further corrections to DPDF evolution

- NNLO parton-to-parton splitting functions (known).
- NLO Pomeron-to-parton splitting functions (unknown).
- Absorptive corrections. Schematically,

$$\frac{\partial g^{\mathrm{D}}}{\partial \ln Q^2} = P_{gg} \otimes g^{\mathrm{D}} + P_{g\mathbb{P}} \otimes g^2 - 4P_{g\mathbb{P}} \otimes gg^{\mathrm{D}} + \dots$$



Possible that further corrections will stabilize the results of the fit with respect to the $Q^2_{\rm min}$ cut.

Non-linear evolution of inclusive PDFs



• Regge theory expectation for small-x PDFs at low scales $Q \lesssim Q_0 \sim 1~{\rm GeV}$ is that:

$$xg \sim x^{-\lambda_g}$$
 and $xS \sim x^{-\lambda_S}$,

with $\lambda_g = \lambda_S = \lambda_{\text{soft}} \simeq 0.08$, then at higher $Q^2 \gtrsim 1$ GeV, QCD evolution should take over, increasing λ_g and λ_S .

• Current PDF sets exhibit a very different behavior.

Gribov-Levin-Ryskin ('83) and Mueller-Qiu ('86) (GLRMQ):

$$\frac{\partial xg(x,Q^2)}{\partial \ln Q^2} = \frac{\alpha_S}{2\pi} \sum_{a'=q,g} P_{ga'} \otimes a' - \frac{9}{2} \frac{\alpha_S^2(Q^2)}{R^2 Q^2} \int_x^1 \frac{\mathrm{d}x'}{x'} \left[x'g(x',Q^2) \right]^2$$

(BFKL-based refinements: Balitsky–Kovchegov and JIMWLK. See review by Jalilian-Marian and Kovchegov [hep-ph/0505052].)

 Are the input MRST/CTEQ gluon densities at small-x and low Q² forced to be artificially small in order to mimic the neglected screening corrections?



Non-linear evolution of inclusive PDFs

Martin, Ryskin, G.W. [hep-ph/0406225, hep-ph/0508093]:



Outline

1 Introduction

2 Exclusive diffraction in *ep* collisions

Exclusive processes within collinear factorization Exclusive processes within the dipole picture Dipole picture in the non-forward direction Impact parameter dependent dipole cross sections Description of HERA vector meson data Description of HERA DVCS data

3 Inclusive diffraction in *ep* collisions

Diffractive DIS kinematics and structure functions Collinear factorization in DDIS Perturbative Pomeron contribution to DDIS Analysis of HERA DDIS data Non-linear evolution of inclusive PDFs

4 Diffraction in pp and $p\bar{p}$ collisions

Factorization breaking in diffractive hadron-hadron collisions Exclusive diffractive Higgs production at LHC

5 Summary and outlook

Factorization breaking in diffractive pp and $p\bar{p}$ collisions

- Factorization is broken in diffractive hadron-hadron collisions by (soft) interaction between spectator partons of the colliding hadrons.
- Can be accounted for with suppression factor S² calculable from eikonal models with parameters fitted to soft hadron-hadron data [review by Gotsman *et al.*, hep-ph/0511060].
- Consider diffractive dijet production at Tevatron. Diffractive structure function of the antiproton:

$$ilde{F}^{\mathrm{D}}_{JJ}(eta) = rac{1}{\xi_{\mathrm{max}} - \xi_{\mathrm{min}}} \int_{\xi_{\mathrm{min}}}^{\xi_{\mathrm{max}}} \mathrm{d}\xi \left[eta g^{\mathrm{D}}(\xi,eta,Q^2) + rac{4}{9}eta \Sigma^{\mathrm{D}}(\xi,eta,Q^2)
ight],$$

measured by CDF [PRL 84, 5043 (2000)].

 Prediction using DPDFs from HERA agree with *F*^D_{JJ} data when S² factor included [Kaidalov *et al.*, hep-ph/0105145].



Exclusive diffractive Higgs production at LHC

Khoze, Martin, Ryskin (KMR) (+ Kaidalov, Stirling) ['97–]. Review by J. Forshaw [hep-ph/0508274].



$$\sigma(pp
ightarrow p + H + p) \sim 3 \, {
m fb}$$

 $\sim 10^{-4} \, \sigma(pp
ightarrow HX),$

for a Standard Model Higgs with $M_H \simeq 120$ GeV.

Advantages:

- 1 Tag outgoing protons: measure Higgs mass with resolution $\sim 1~{
 m GeV}.$
- 2 Investigate quantum numbers of produced states.
- 3 Clean environment with low background.
- @ Regions of SUSY parameter space where exclusive Higgs production enhanced compared to inclusive Higgs production.

 $\rm FP420$ proposal to add forward proton tagging detectors 420 m from the interaction points of the ATLAS/CMS experiments [see http://www.fp420.com/].

Main ingredients of KMR approach

$$\sigma(pp \to p + H + p) \sim \frac{S^2}{B_D^2} \left| N \int \frac{\mathrm{d}Q_T^2}{Q_T^4} f_g(x_1, x_1', Q_T^2, \mu^2) f_g(x_2, x_2', Q_T^2, \mu^2) \right|^2$$

where $S^2\simeq$ 0.026, $B_D\simeq$ 4 GeV $^{-2}$, $\mu\simeq M_H/2$, and

$$f_g(x, x', Q_T^2, \mu^2) = R_g \frac{\partial}{\partial \ln Q_T^2} \left[\sqrt{T_g(Q_T^2, \mu^2)} xg(x, Q_T^2) \right],$$

with R_g = skewness. The Sudakov factor, $T_g(Q_T^2, \mu^2)$, suppresses the infrared Q_T region:



- Plot by J. Forshaw [hep-ph/0508274].
- Integrand dominated by $Q_T \sim 1-2$ GeV \Rightarrow pQCD applicable (just!).
- Calculations implemented in ExHuME Monte Carlo program [hep-ph/0502077].

Check KMR approach at HERA and Tevatron

- Skewed unintegrated gluon densities, f_g(x, x', Q²_T, μ²), give reasonable description of exclusive diffractive vector meson production at HERA [Martin-Ryskin-Teubner, hep-ph/9912551].
- Predictions for the suppression factor S^2 can be tested at Tevatron, and for the resolved photon contribution to photoproduction at HERA (in both diffraction and with leading neutrons).
- Searches in progress at Tevatron for exclusive dijet $(p\bar{p} \rightarrow p + jj + \bar{p})$ and diphoton $(p\bar{p} \rightarrow p + \gamma\gamma + \bar{p})$ production $[\rightarrow \text{talk by C. Mesropian}].$

Hard rescattering corrections to exclusive Higgs production

Bartels–Bondarenko–Kutak–Motyka [hep-ph/0601128] find that hard rescattering corrections give large negative contribution, using pQCD with infrared behavior stabilized by saturation scale:



Rebuttal by Khoze–Martin–Ryskin [hep-ph/0602247], who argue that hard rescattering corrections must be small because:

- Similar effect not observed for leading neutron production at HERA.
- Rapidity interval at LHC not large enough for hard rescattering corrections.
- LO pQCD approach invalid: no evidence in data that saturation scale is large enough to provide infrared cutoff, gluon density not constrained at very small x.
- If first hard rescattering corrections important, would need to consider additional corrections and would need to recalculate S^2 .

Better theoretical understanding needed to clarify this issue.

Outline

1 Introduction

2 Exclusive diffraction in *ep* collisions

Exclusive processes within collinear factorization Exclusive processes within the dipole picture Dipole picture in the non-forward direction Impact parameter dependent dipole cross sections Description of HERA vector meson data Description of HERA DVCS data

3 Inclusive diffraction in *ep* collisions

Diffractive DIS kinematics and structure functions Collinear factorization in DDIS Perturbative Pomeron contribution to DDIS Analysis of HERA DDIS data Non-linear evolution of inclusive PDFs

4 Diffraction in pp and pp̄ collisions

Factorization breaking in diffractive hadron–hadron collisions Exclusive diffractive Higgs production at LHC

5 Summary and outlook

Summary

Exclusive diffraction in ep collisions

- Exclusive diffractive processes are well described within the **dipole picture** using an impact parameter dependent (Glauber–Mueller) dipole cross section.
- *t*-distributions show that the proton shape in the transverse plane takes a **universal Gaussian form** in the limit of small dipole sizes, with $\sqrt{\langle b^2 \rangle} = 0.56$ fm (cf. the proton charge radius of 0.87 fm).

Inclusive diffraction in ep collisions

- Perturbative Pomeron contribution leads to an **inhomogeneous** evolution equation for the diffractive PDFs, analogous to the evolution equation for the photon PDFs.
- Evidence of instability in the fits for $Q^2 \lesssim 6.5 \text{ GeV}^2$: further theoretical corrections such as NLO Pomeron-to-parton splitting functions or absorptive corrections may help.

Diffraction in pp and $p\bar{p}$ collisions

- Factorization broken in hadron-hadron collisions, but can be accounted for with an extra suppression factor calculable from eikonal models of soft interactions.
- Case for installing proton taggers at the LHC to detect exclusive diffractive Higgs production. Calculations can be checked at HERA and Tevatron.

Outlook

Diffraction in ep collisions at a future EIC

- Cleanest measurements of diffraction by tagging outgoing proton. Requires proper integration of forward detectors.
- Measure *t*-distributions of exclusive vector meson production and DVCS to high accuracy to give information about the proton shape in the transverse plane and the small-*x* gluon density.
- Precise measurements of $F_L^{D(3)}$ could clarify role of higher-twist contributions in diffractive DIS. (First measurements expected from HERA low-energy running in 2007.)
- Search for exclusive diffractive dijet production.
- Strong rapidity cut requirement could enhance perturbative Pomeron contribution. Interesting to measure transverse momentum of Pomeron remnant.
- Diffractive DIS offers a more direct way to study perturbative multi-ladder diagrams than inclusive DIS.