

# **The Effect of Interaction Cross Section Systematics on the T2K $\nu_\mu$ Disappearance Measurement**

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**IOP Parallel Sessions - 30th March, 2010**

# Outline of Talk

- $\nu_\mu$  Disappearance measurement at T2K:
  - Current world limits.
  - Method and main source of background.
- Neutrino interaction systematics:
  - GENIE Monte Carlo generator.
  - Event reweighting.
  - Effect on oscillation measurement.
- Constraining cross section systematics using near detector fits:
  - $CC1\pi$  measurement at ND280, MC study of event rates.

# Current Knowledge of Atmospheric Mixing Parameters

Survival probability given by:

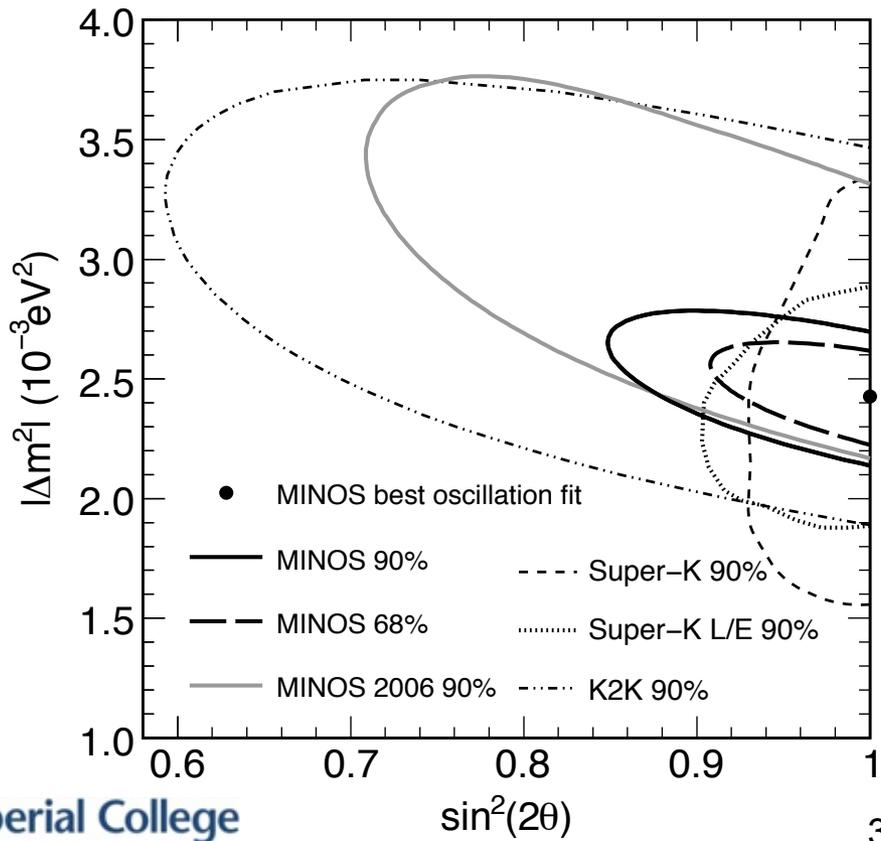
$$P(\nu_\mu \rightarrow \nu_\mu) \simeq 1 - \cos^4 \theta_{13} \sin^2 2\theta_{23} \sin^2 \left[ \frac{1.27 \Delta m_{23}^2 (\text{eV}^2) L (\text{km})}{E_\nu (\text{GeV})} \right]$$

Atmospheric  
> 0.92 (90% CL)

Accelerator  
(2.43 +/- 0.13) x 10<sup>-3</sup> (68% CL)

Compilation of world measurements:

Phys.Rev.Lett.101:131802,2008.



Expected sensitivity at T2K after 5 years (nominal running):

$$\delta(\sin^2 2\theta_{23}) \approx 0.01$$

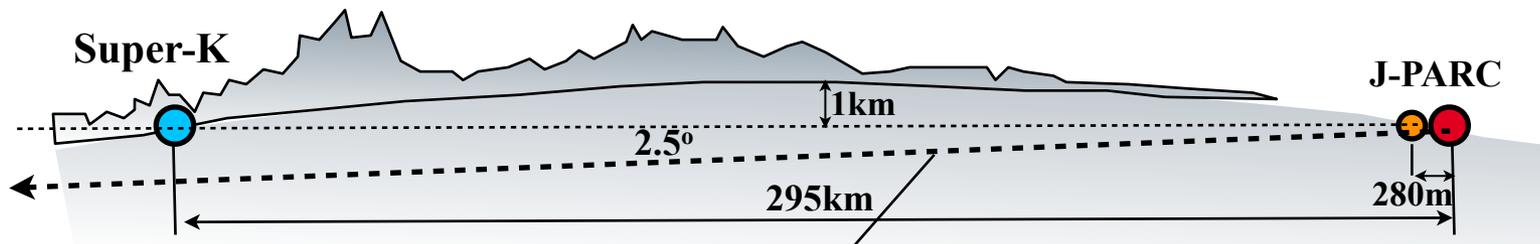
$$\delta(\Delta m_{23}^2) < 10^{-4} \text{eV}^2$$

# The $\nu_\mu$ Disappearance Measurement

Signal = anything that allows the species and energy of neutrino to be reconstructed.  
 Compare expected with observed at Super-K to extract oscillation parameters.

$$\frac{dN_\nu^{obs}}{dE_\nu^{reco}}$$

$$\frac{dN_\nu^{pred}(\sin^2 \theta_{23}, \Delta m_{23}^2)}{dE_\nu^{reco}}$$

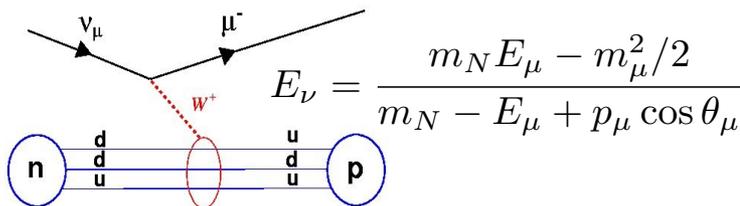


Off axis beam:

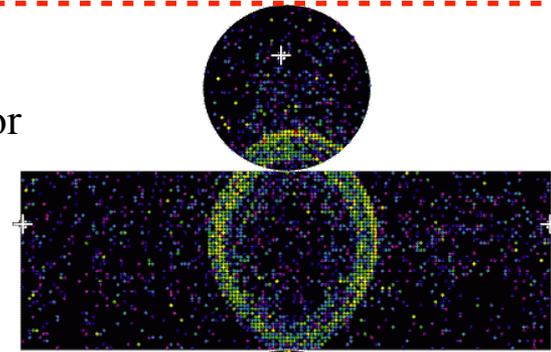
- Narrow energy spectrum
- Peak of spectrum --> oscillation maximum @ SK.

Charged current quasi-elastic (CCQE) interactions are ideal candidate for signal:

- Reconstruct energy using only muon.
- 50% of CC events.



At Super-K look for events with single clean muon-like ring (1R $\mu$ -like):



See backup slides for more on cuts

# Predicting what Passes the 1R $\mu$ -like cut at Super-K

$$\frac{dN_{\nu}^{pred}}{dE_{\nu}^{reco}} \propto \int dE_{\nu} \cdot \Phi^{SK}(E_{\nu}) \cdot \sigma(E_{\nu}) \cdot \epsilon_{1R\mu}^{SK}(E_{\nu}) \cdot p(E_{\nu}; E_{\nu}^{reco})$$

## Prediction of flux at Super-K:

- Flux Monte Carlo
- NA61 data.
- Measurements at near detectors.

## Neutrino cross-sections:

- Use neutrino MC generators (GENIE, NEUT).
- Generators act as interface to world neutrino cross-section data.
- Have to link together many theoretical and phenomenological models to cover necessary kinematical range.

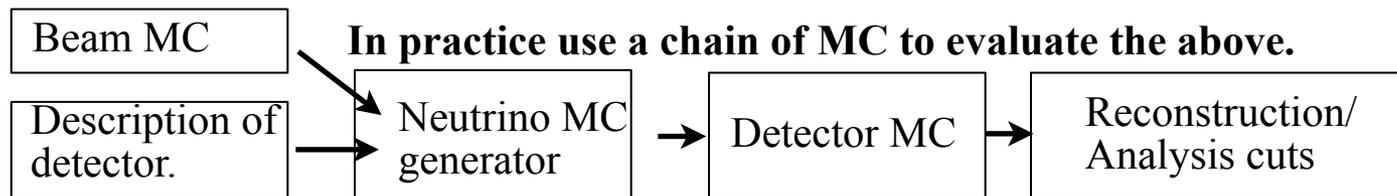
## Detection efficiency for 1R $\mu$ events:

- This is the sum over different types of event:

$$\sigma(E_{\nu}) \cdot \epsilon_{1R\mu}^{SK}(E_{\nu}) = \sum_{i=1}^N \sigma_i \cdot \epsilon_i$$

## Probability of reconstructing an event with true energy $E_{\nu}$ as $E_{\nu}^{reco}$ :

- For CCQE events this should be fairly well peaked around  $E_{\nu}$ .
- For non-CC-QEL event which pass the 1R $\mu$  this will be asymmetric.



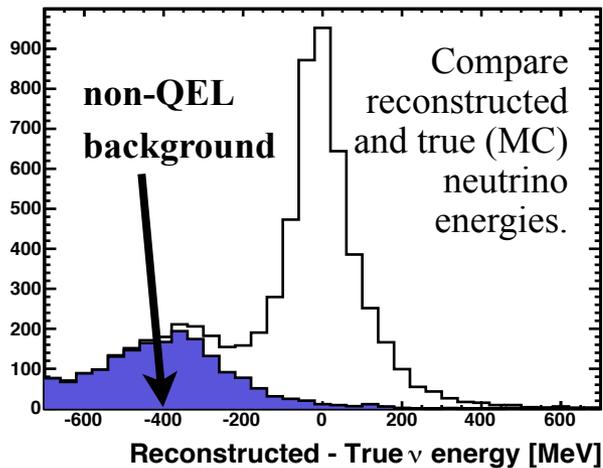
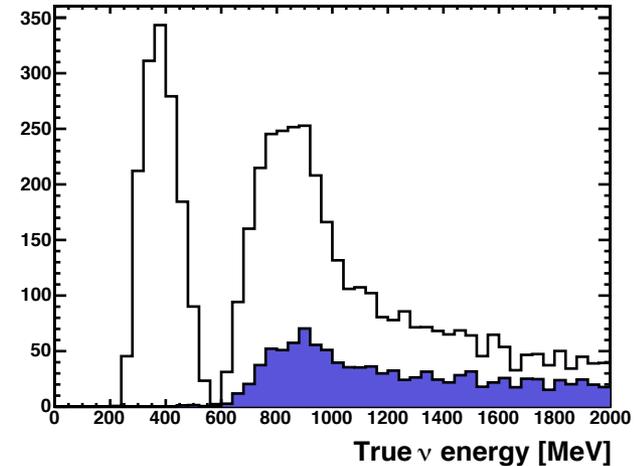
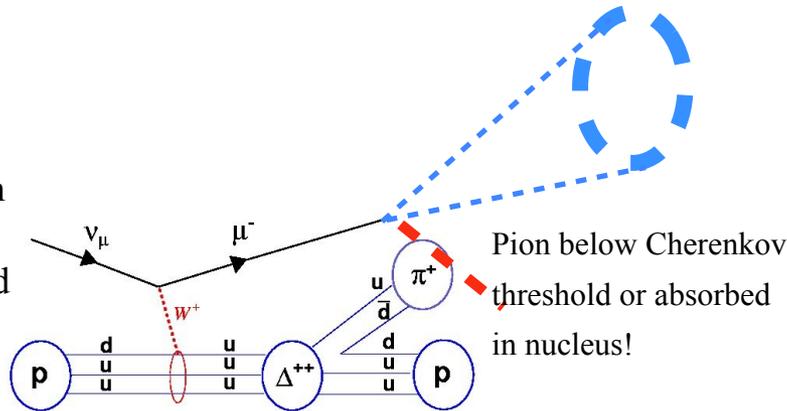
Computationally and logistically demanding! Size of data sets representing lifetime of experiment are prohibitive.

# CC1 $\pi^+$ Background

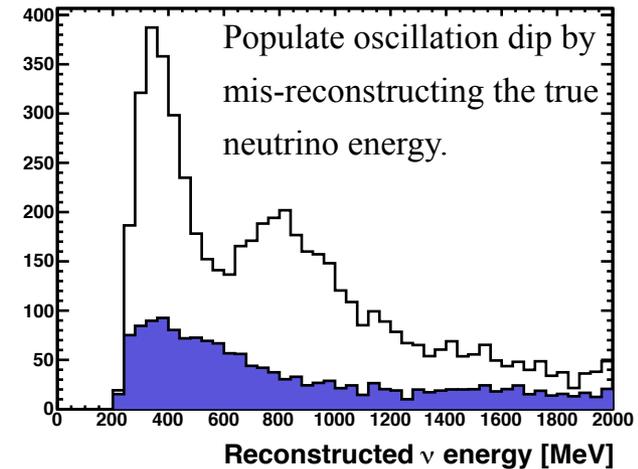
Main source of background is non-CC-QEL for which only the muon is detected.

## 19% non-CC-QEL background:

- Mostly (~70%) from CC 1 $\pi$  channel.
- Rest CC multi pi and NC 1 $\pi$  channels.



Systematically mis-reconstruct neutrino energy for non-QEL background.

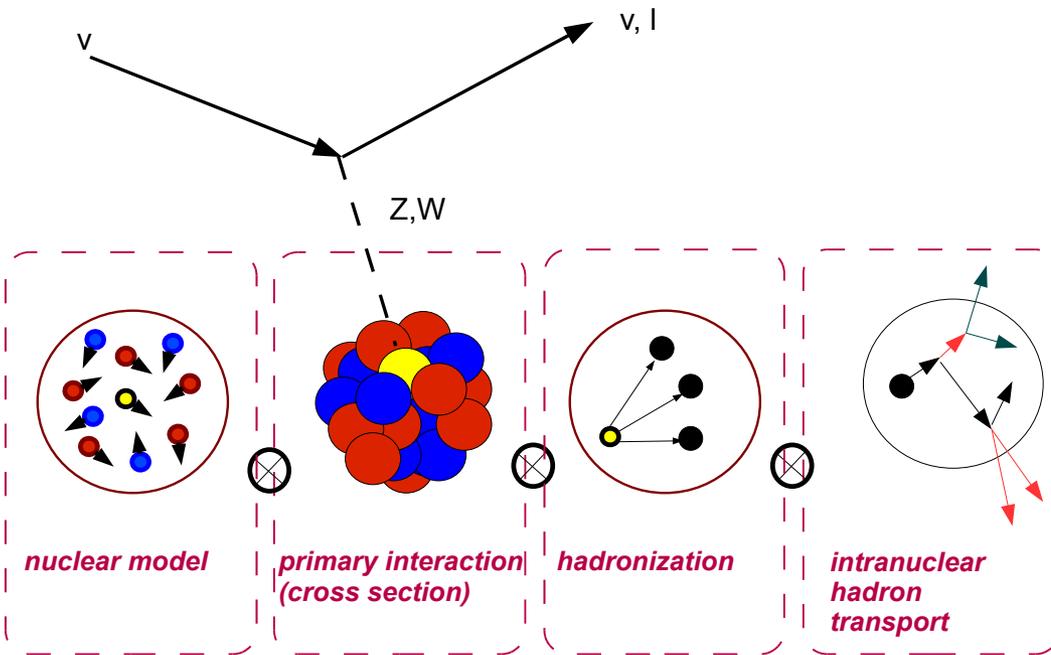


# Simulating Neutrino Interactions

At  $\sim 1\text{GeV}$  cross-sections are poorly known:

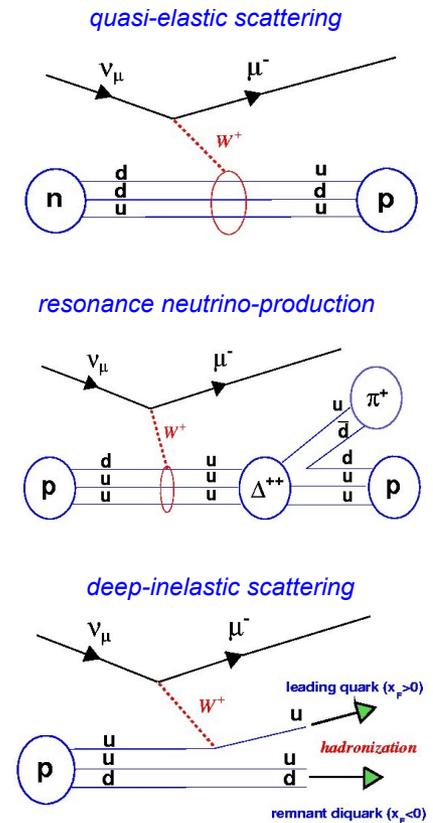
- Lack of data.
- Inadequate theoretical models.
- Uncertainties of order 20%.

with sensitivity @ T2K this is now relevant



Borrowed from GENIE workshop talk.

Dominant interaction modes at  $\sim 1\text{GeV}$ :



# GENIE Monte Carlo Generator



[www.genie-mc.org](http://www.genie-mc.org)

## Generates Events for Neutrino Interaction Experiments:

- Developed by an international collaboration of neutrino interaction experts and used on many experiments.
- Modern Object-Oriented Neutrino MC Generator:
  - Modular design.
  - Flexible to new experimental data and developments in theory.
- Combines many models to span a large kinematical range; Several MeV to several hundred GeV:
  - Maintains internal consistency and continuity.

Many, >100, configurable input physics parameters!

+

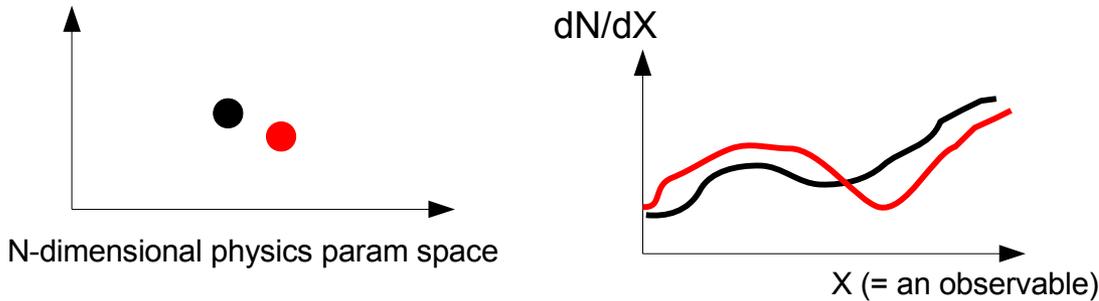
When added to the detector MC and the reconstruction stages the total production time is significant.



Fast simulation needed to evaluate changes in input parameters.

# Event Reweighting

Motivation: To evaluate the effect of changes in input physics parameters without re-running time intensive MC.



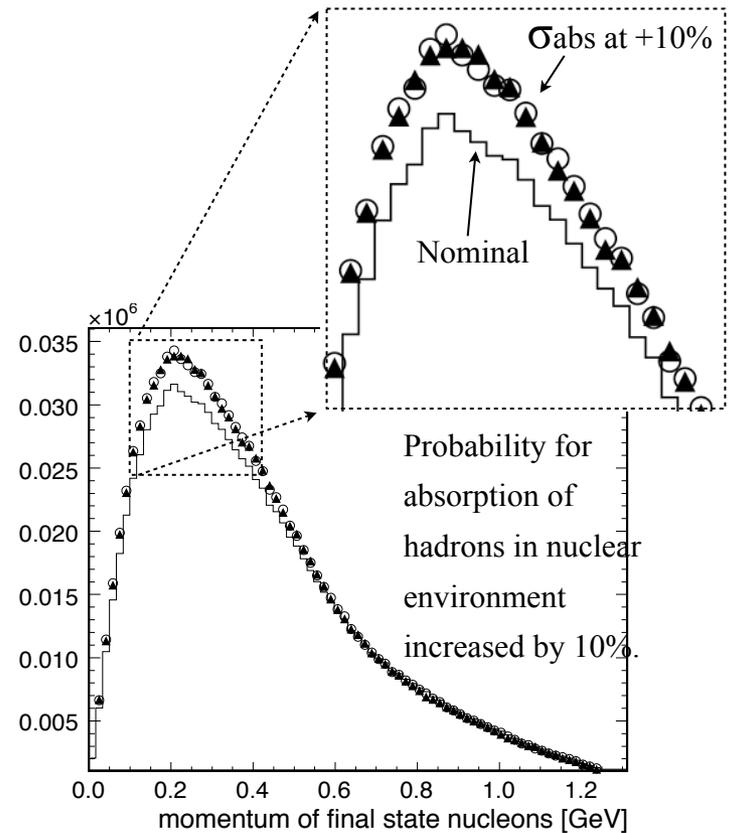
Can reweight parameters controlling:

- Cross-section models.
- Intranuclear hadron transport model.

Massive speed increase opens up lots of possibilities:

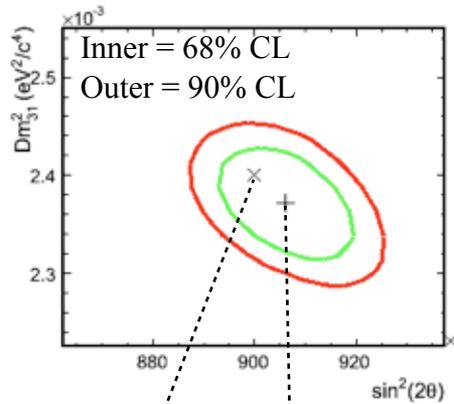
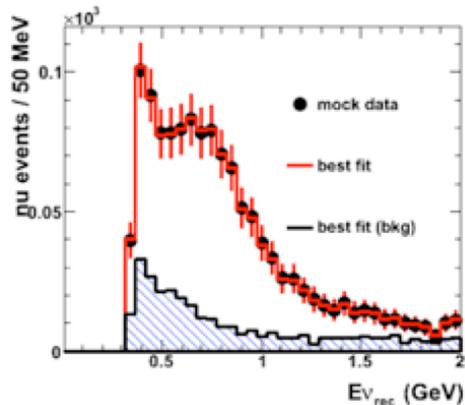
- Scan large volumes of input parameter space and evaluate systematic uncertainties.
- Use input parameters as free parameters in fits to data.

**Validation:** Compare reweighted (circle) with regenerated (triangle).



# Oscillation Systematics Study

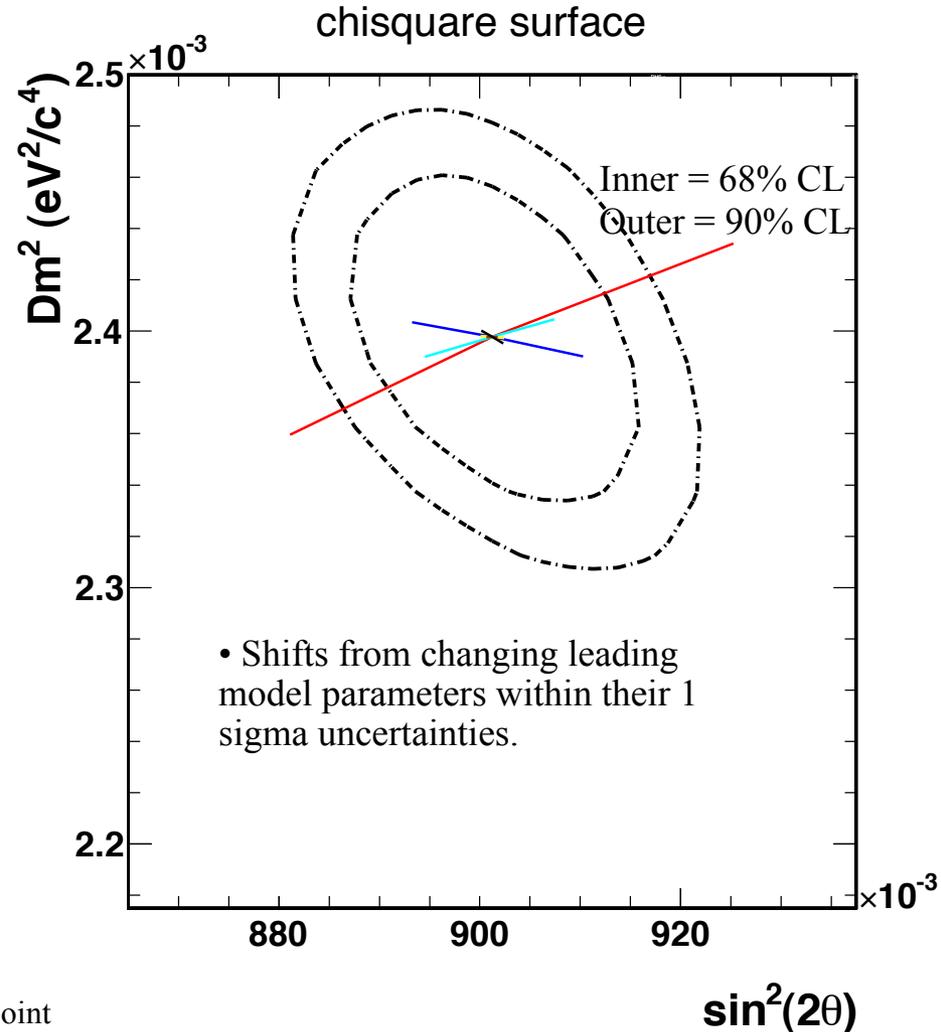
- Oscillation fit nominal mock data
- Mock data tweaked (reweighted) to account for a physics model change.
- Performed oscillation fit again.
  - Fit uses nominal MC as prediction.
- Studied how the best fit point shifts.



Nominal best fit point

Shift in best fit point for tweaked MaRES by -20%

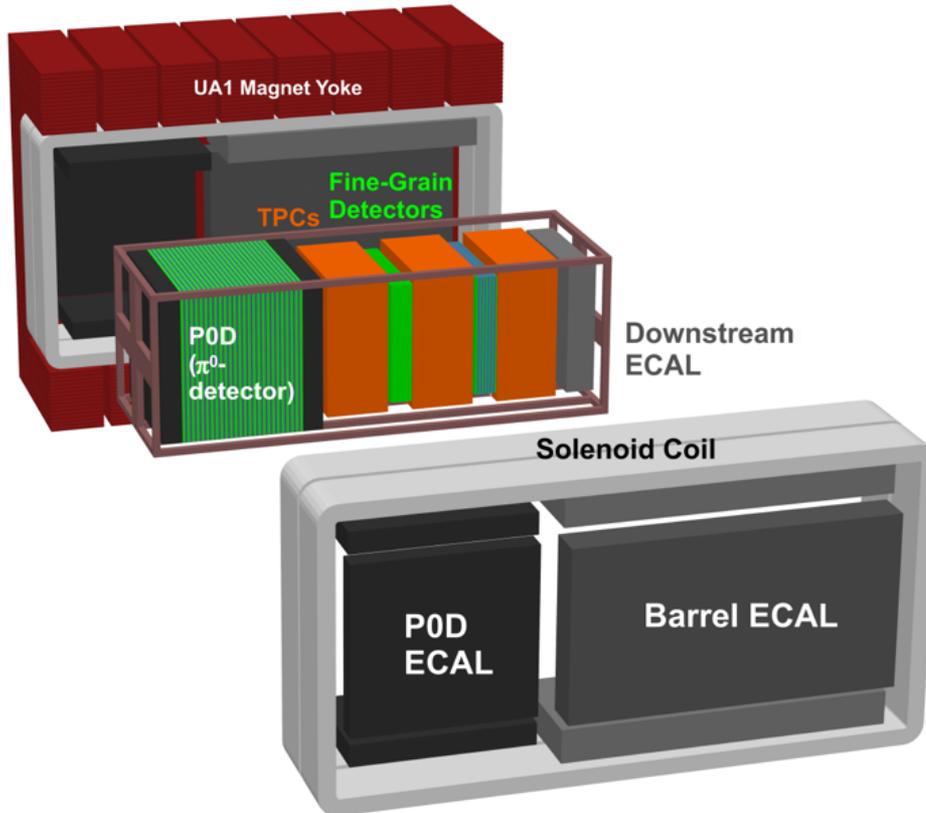
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# Constraining $CC1\pi$ Background at ND280 (1)

Uncertainties in neutrino interaction models give rise to systematic uncertainties in oscillation measurement. Make cross-section measurement at ND280 to constrain systematics.

## ND280:



### Fine Grain Detectors (FGDs):

- Fiducial volumes.
- Vertex location.

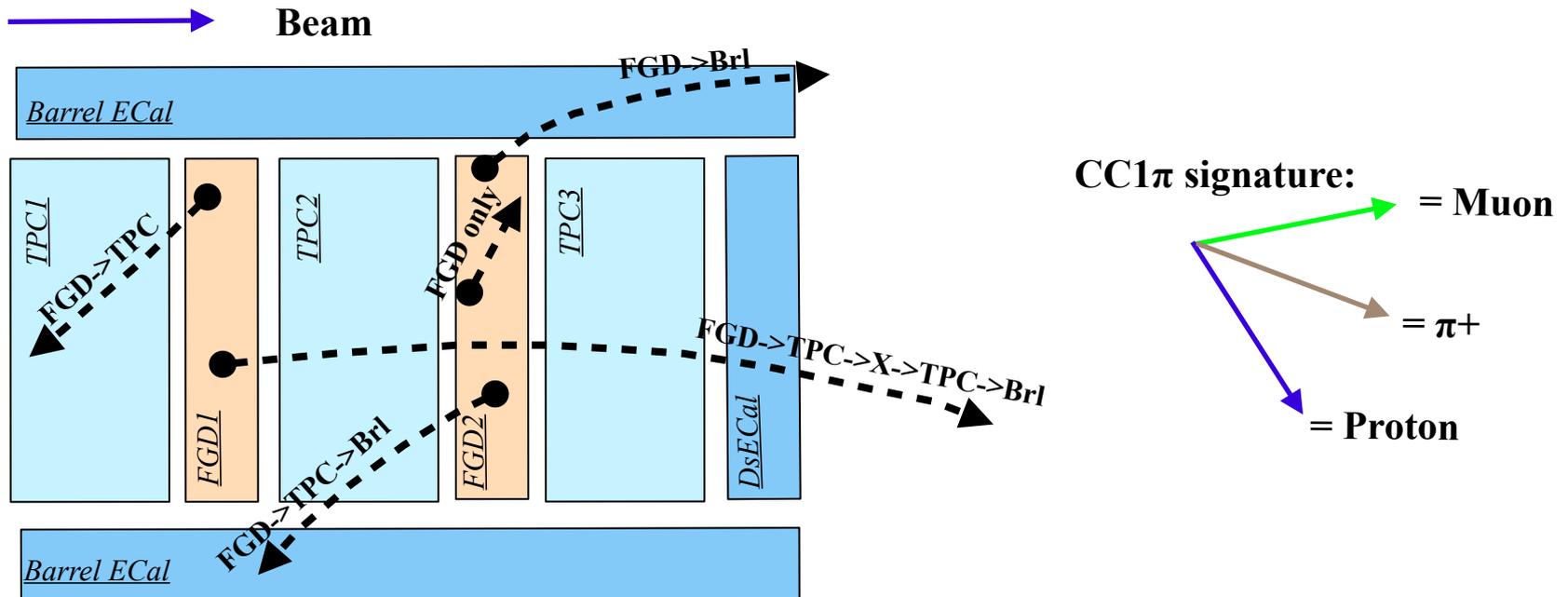
### Time Projection Chambers (TPCs):

- Momentum measurement..
- PID.
- Vertex location.

### Tracker ECAL:

- PID.
- Energy measurement.

# Constraining CC1 $\pi$ Background at ND280 (2)



30 % both pion and muon  
have paths through a  
TPC.

~ 24,000 events for 1yr  
@ full intensity

# Summary

- At T2K's sensitivity neutrino interaction systematics are important.
- $CC1\pi^+$  is the dominant background for the disappearance measurement.
- Using measurement at ND280:
  - High enough statistics to make very accurate measurements of  $CC1\pi^+$  channel.
  - Use this to reduce interaction systematics.

# BACKUPS

# Very Brief Overview of Neutrino Oscillations

Mass and flavour eigenstates different:

- Mass eigenstates propagate at different speeds:  $|\nu_i(\vec{x}, t)\rangle = |\nu_i\rangle e^{ip_i \cdot \vec{x} - iE_i \cdot t}$
- Quantum mechanical interference of flavour eigenstates  $\longrightarrow$  Neutrino oscillations.

Related by the PMNS matrix: 
$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U_{\text{MNS}} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

$$s_{ij} = \sin \theta_{ij}$$

$$c_{ij} = \cos \theta_{ij}$$

$$U_{\text{MNS}} = \begin{pmatrix} \text{“Atmospheric/Beam”} & \text{“Beam/Reactor - whoever is first”} & \text{“Solar/Reactor”} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & +c_{23} & +s_{23} \\ 0 & -s_{23} & +c_{23} \end{pmatrix} \begin{pmatrix} +c_{13} & 0 & +s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & +c_{13} \end{pmatrix} \begin{pmatrix} +c_{12} & +s_{12} & 0 \\ -s_{12} & +c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \approx \begin{pmatrix} 0.8 & 0.5 & s_{13}e^{-i\delta} \\ 0.4 & 0.6 & 0.7 \\ 0.4 & 0.6 & 0.7 \end{pmatrix}$$

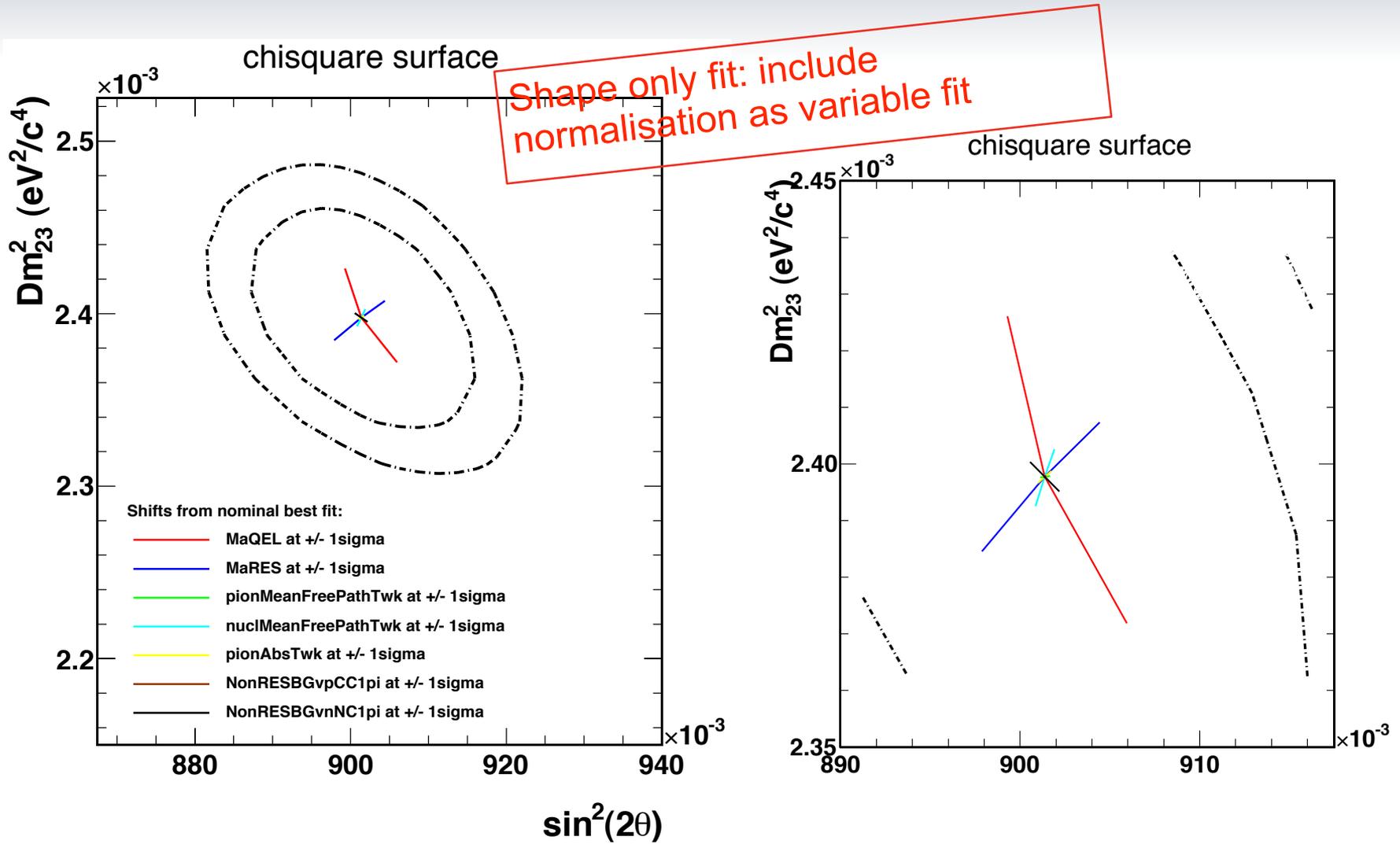
## Open questions for current generation of experiments:

- Is  $\theta_{23}$  maximal? Look at  $\nu_\mu \rightarrow \nu_\mu$ . T2K
- Is  $\theta_{13}$  non-zero? Look at sub-dominant  $\nu_\mu \rightarrow \nu_e$ . T2K
- Is there CP violation? Future beam experiments depending on size of  $\theta_{13}$ .
- Precise measurement of mass squared differences. T2K

# Super-K Cuts

- Fiducial Volume Cut: Require reconstructed vertex is contained inside the fiducial. Removes difficult to reconstruct events close to wall.
- Fully Contained Cut: Put limit on hits in outer detector to make sure event did started inside detector.
- Visible Energy Cut: visible energy in the inner detector (ID) is greater than 100 MeV/c . Removes noise and low energy events.
- Single ring cut: So dominantly select QEL events.
- Ring has to be muon-like.

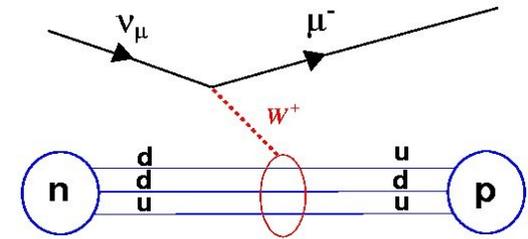
# Shape Only Fits



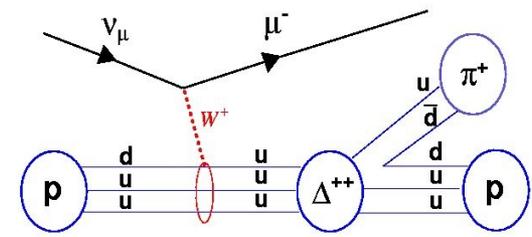
# Process - Topology Breakdown

$\pi$ topology	QEL	RES	DIS	COH	Other	Total
<b>Total</b>	51.65	28.03	19.36	0.72	0.24	
<b>Multi <math>\pi</math>s</b>		0.25	5.41		0.00	5.66
$1\pi^+ + 1\pi^0$	0.06	0.44	2.56		0.00	3.06
$1\pi^- + 1\pi^+$		0.23	0.91		0.00	1.14
$1\pi^- + 1\pi^0$		0.02	0.19		0.00	0.22
$2\pi^+$		0.07	0.78			0.85
$2\pi^0$		0.10	0.51		0.00	0.61
$2\pi^-$		0.00	0.03			0.03
$1\pi^+$	0.07	16.35	5.07	0.66	0.03	22.17
$1\pi^0$		4.26	2.35		0.02	6.63
$1\pi^-$		0.68	0.34	0.07	0.01	1.10
$0\pi$	51.52	5.64	1.20		0.17	58.53

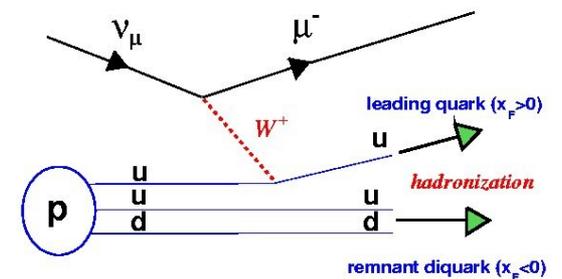
quasi-elastic scattering



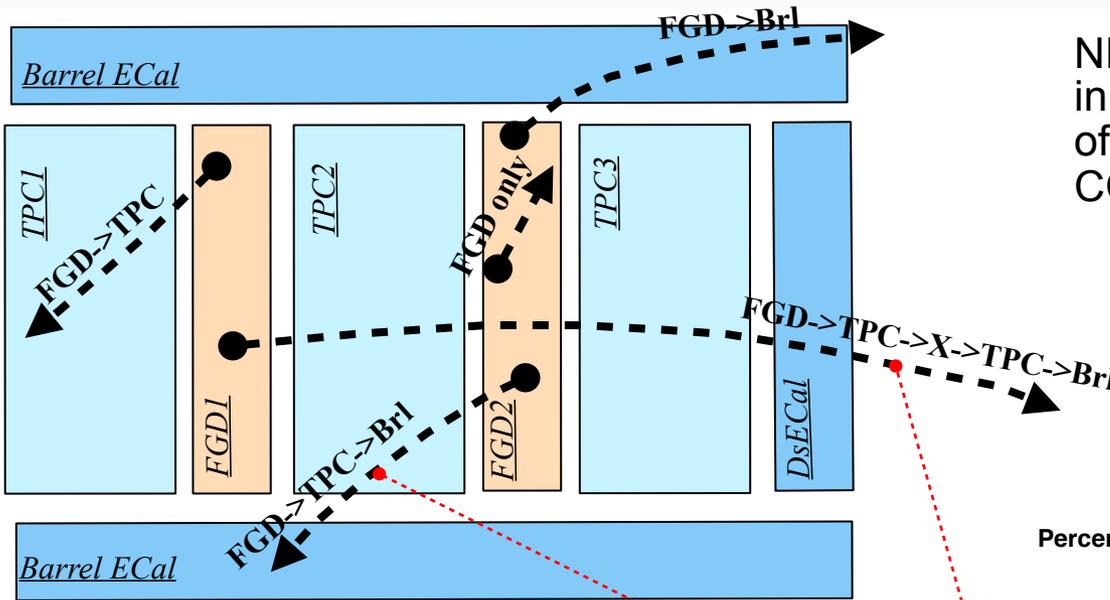
resonance neutrino-production



deep-inelastic scattering



# MC Study of Event Rates



ND280 is a complex detector: initially look at different types of detector topologies for CC1 $\pi$  measurement.

30 % both pion and muon have paths through a TPC.

~ 24,000 events for 1yr @ full intensity

Initial thoughts:

- Significant statistics for events with both  $\mu$  and  $\pi$  tracks going through TPC.
- Can recover events for which one track does not go through a TPC using the tracker ECal.
- Also a subset of events will have information on the proton track - detailed studies of kinematical dependencies of models.

Percentage of CC1 $\pi^+$  events in FGDs for given detector paths

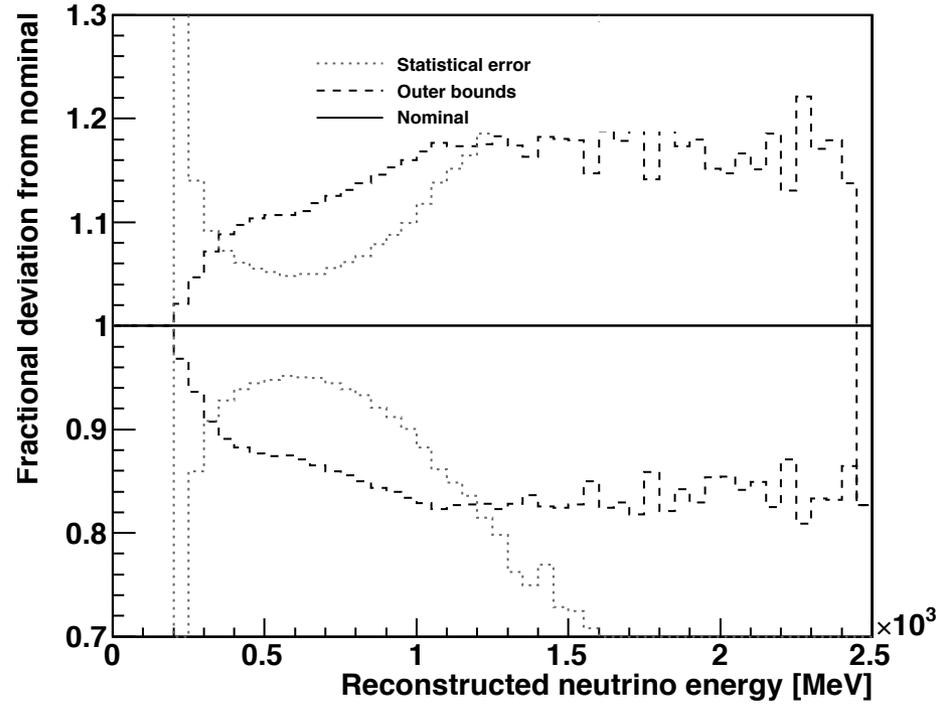
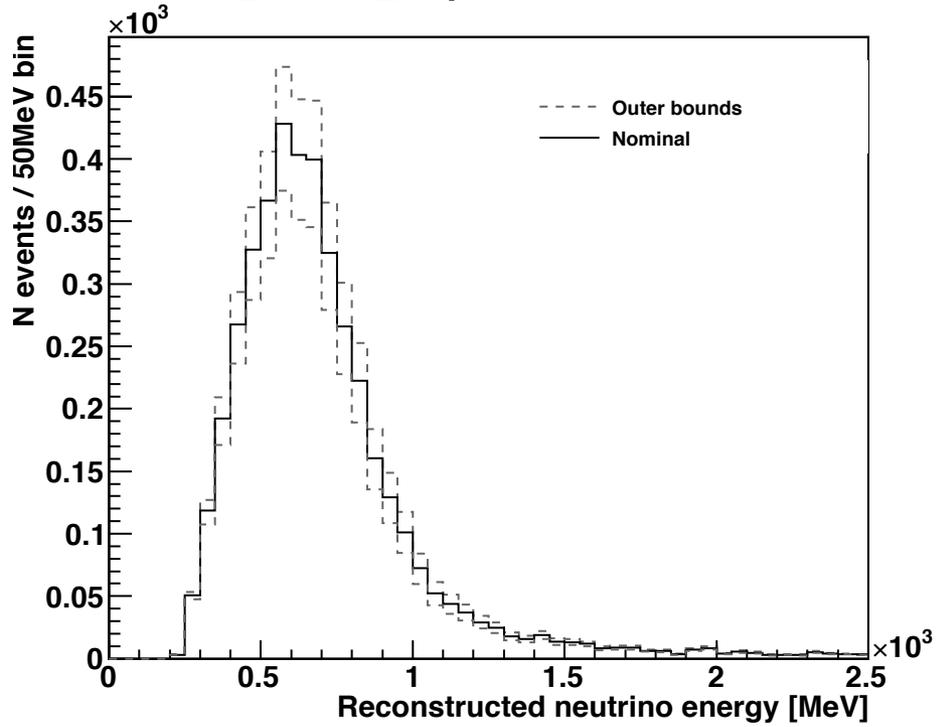
kOther	0.01	0.02	0.01	0.00	0.01	0.01	
FGD->TPC->X->TPC->Brl	0.09	0.09	0.02	0.26	0.19	0.05	
FGD->TPC->X->TPC	0.33	0.39	0.18	0.96	0.78	0.11	
FGD->TPC->Brl	2.58	1.96	4.09	4.76	3.31	0.54	
FGD->TPC	3.43	2.97	6.88	5.45	1.94	0.36	
FGD->Brl	1.49	1.99	2.07	1.53	1.05	0.21	
FGD only	9.30	6.49	12.32	13.37	6.28	1.27	
	FGD only	FGD->Brl	FGD->TPC	FGD->TPC->Brl	FGD->TPC->X->TPC	FGD->TPC->X->TPC->Brl	kOther

$\pi$  detector path

$\mu$  detector path

# SuperK CCQE Error Envelope: Tweaking QEL axial mass parameter by +/- 15%

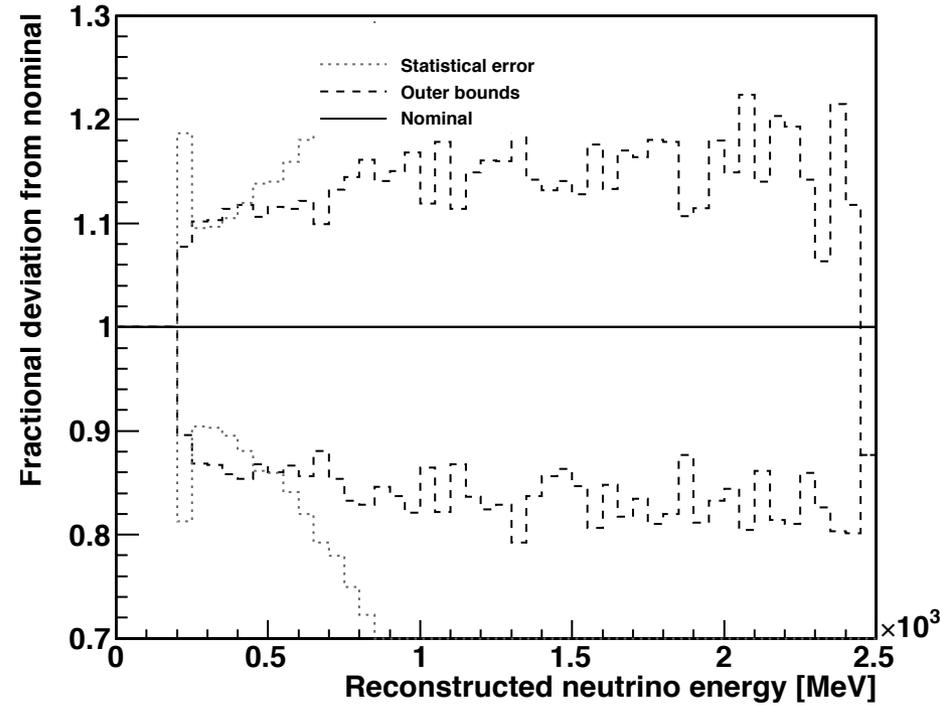
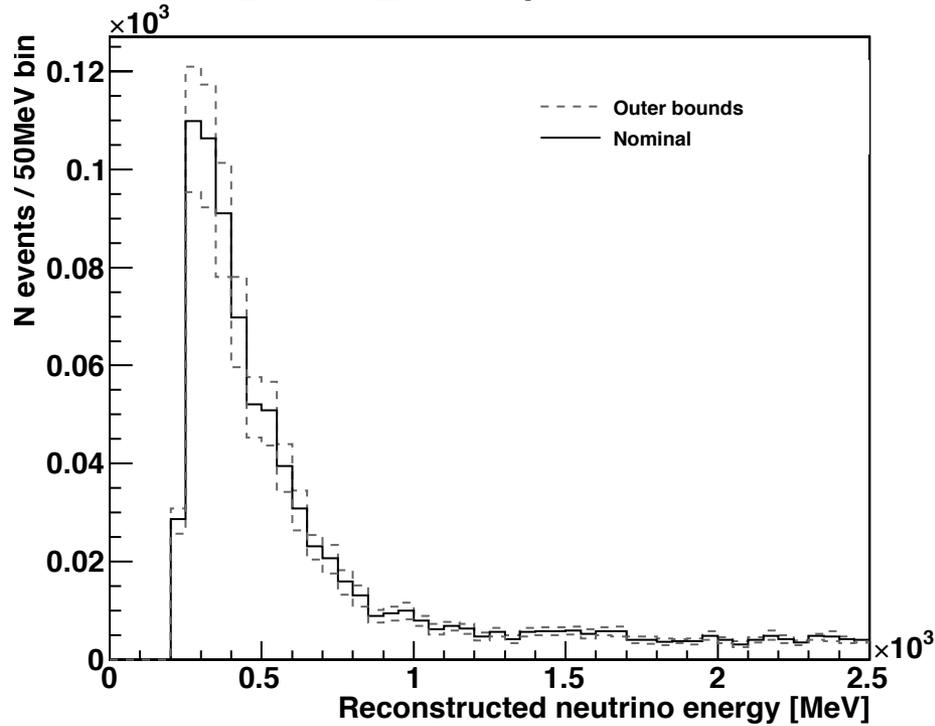
errEnvHists\_MaQEL\_ccqe



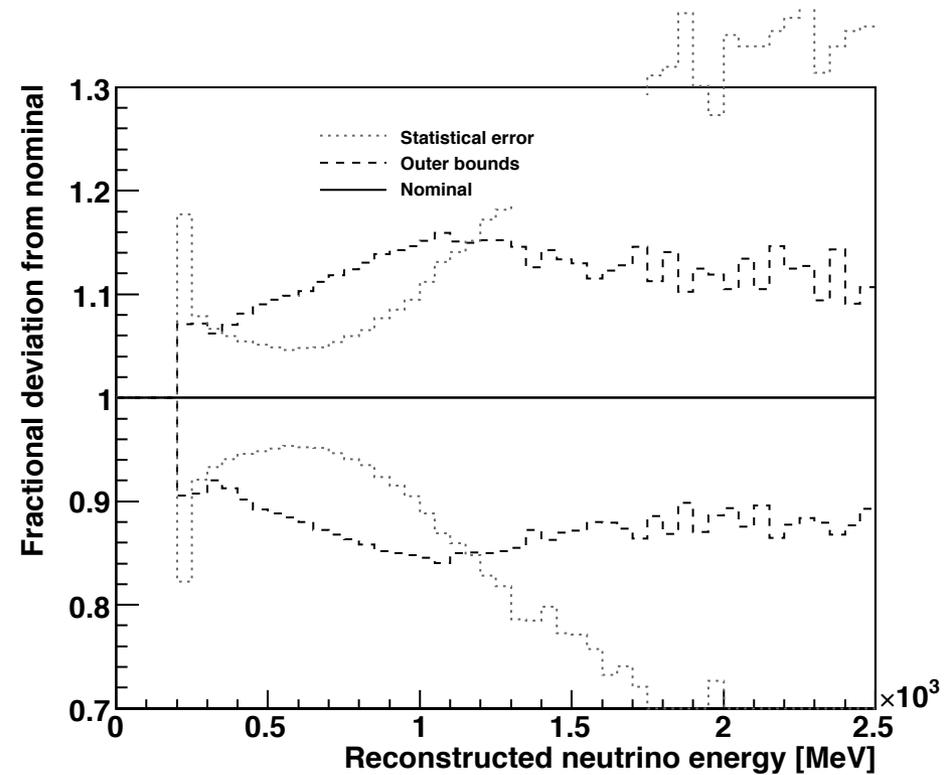
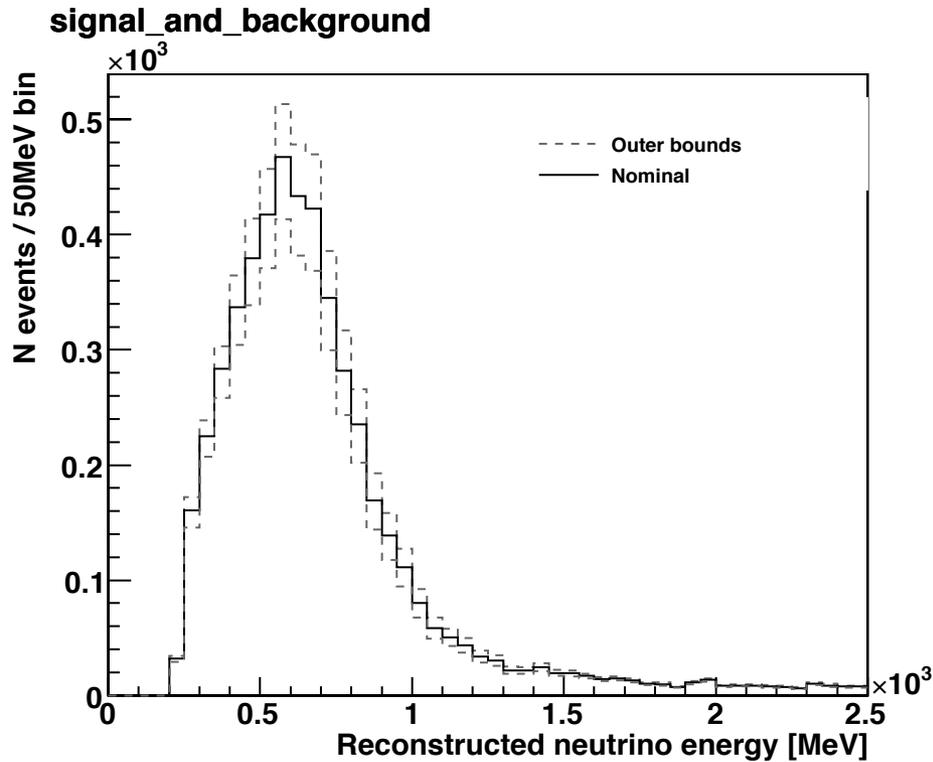
All error envelope studies are for 5 years nominal running assuming  $\sim 1200$  signal events/year.

# SuperK Non-CCQE Bkg Error Envelope: Tweaking RES axial mass parameter by +/- 20%

errEnvHists\_MaRES\_non-ccqe



# Error Envelope for events which pass FC1R cut: now include uncertainty on signal and background (add in quadrature)



# Including Nuisance Parameters in Fit

## [simplistic case: uncorrelated systematics]

**Systematic (nuisance)**

$$\chi^2(\Delta m_{mn}^2, \sin^2 2\theta_{mn}, \{a_0, a_1, \dots, a_j\}) = \sum_{i=0}^{n_{bins}} 2(e_i - o_i) + 2o_i \ln(o_i/e_i) + \sum_{j=0}^{n_{syst}} \frac{(a_j - \langle a_j \rangle)^2}{\sigma_{syst,j}^2}$$

Expected  
Observed

Updates

**'Monte Carlo'**

Tweaks @ nominal MC

REWEIGHT

$$e_i = e_i(\Delta m_{mn}^2, \sin^2 2\theta_{mn}, a_0, a_1, \dots, a_j)$$

$$= \left( \prod_{j=1}^{n_{syst}} w_j \right) * e_i(\Delta m_{mn}^2, \sin^2 2\theta_{mn}, \langle a_0 \rangle, \langle a_1 \rangle, \dots, \langle a_j \rangle)$$

Calculate gradients for optimised fitting techniques.

