

# Jets, Jets, Higgs & Jets

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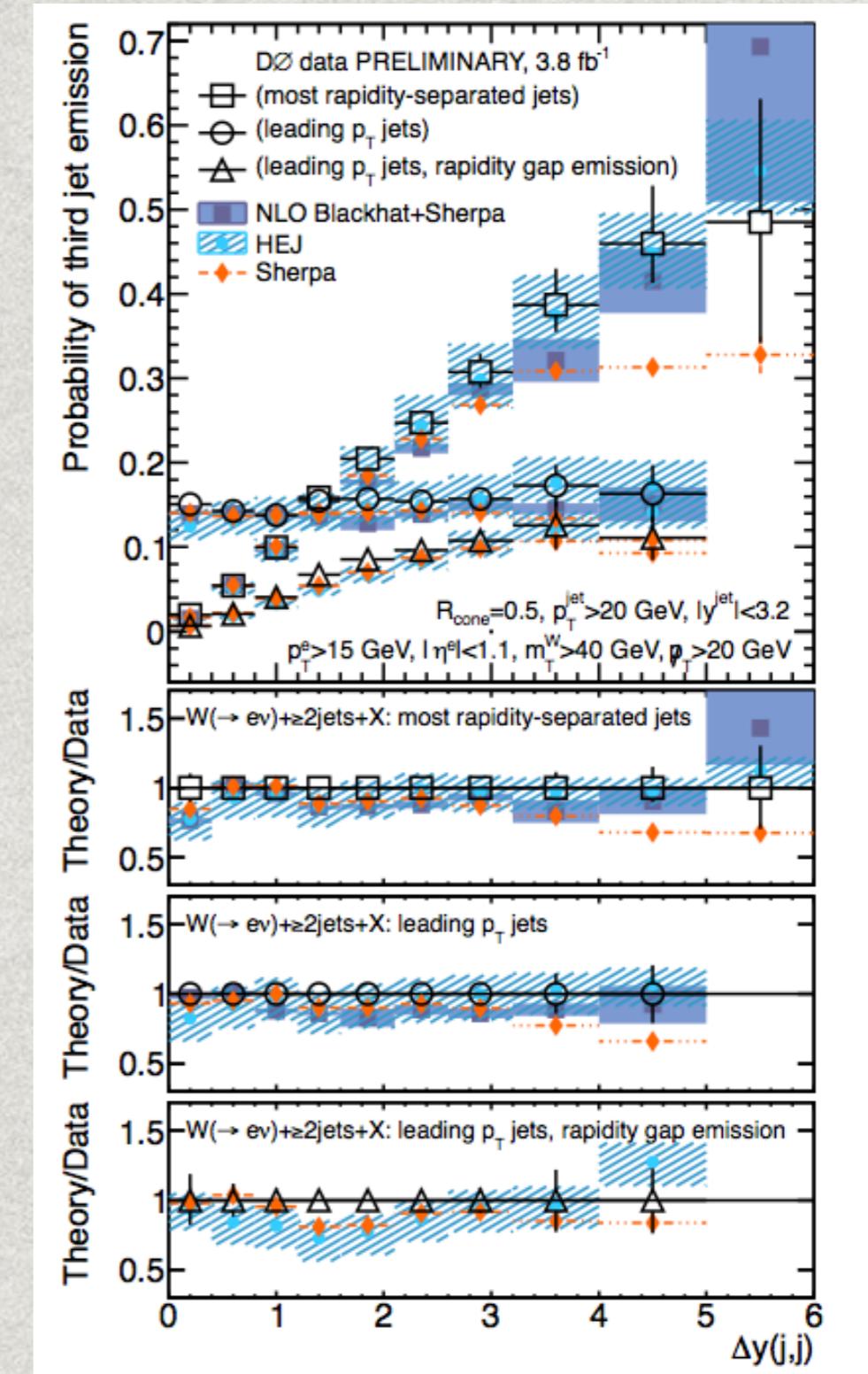
**Mostly HEJ = with J. Andersen, T. Hapola, J. Medley  
(+ J. Cockburn, H. Brooks)**

**UCL Seminar**

**24 Jan 2014**

# Outline

- ✳ Introduction
- ✳ High Energy Jets
- ✳ Recent Jet Results
- ✳ Higgs Plus Jets



# Why Study Jets?

- \* Complex Standard Model Process  
Therefore complex test of tools
- \* Test models of jet vetoes etc. here before Higgs
- \* **IF** new physics is hiding, need precision to find it
- \* Many tools available... with different strengths

# Higher Orders

- \* Already seen  $(n+1)$ -jet rates are not small

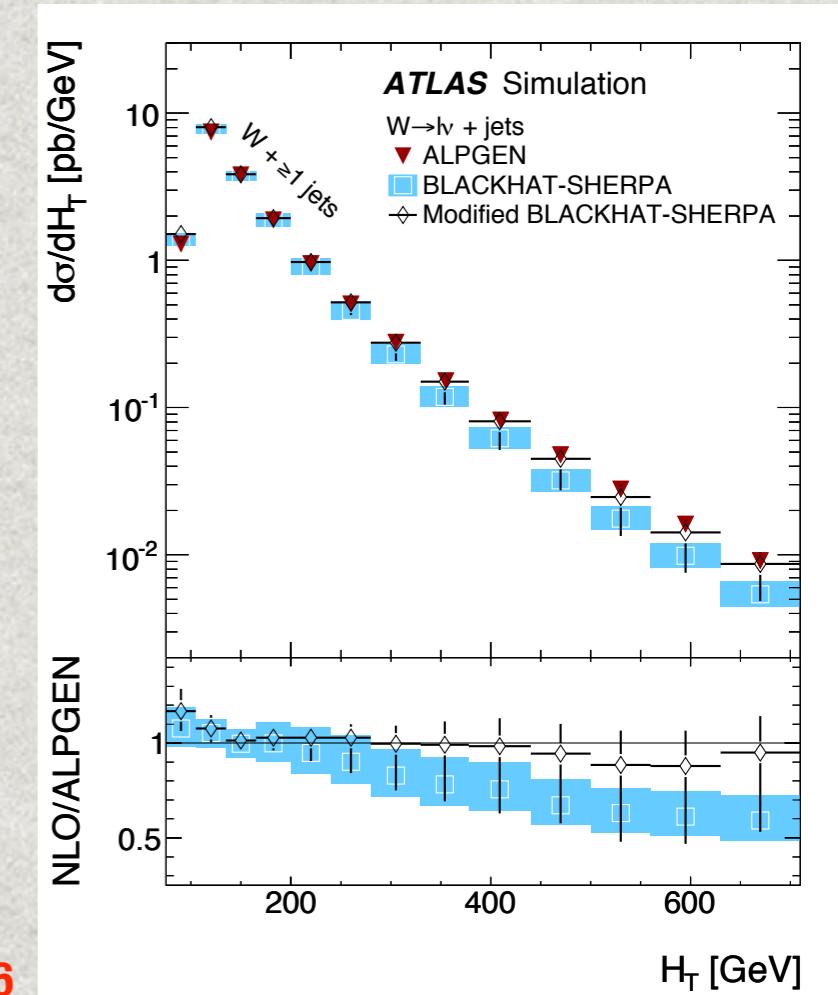
e.g. ATLAS Z+jets

$$\frac{(n+1)\text{-jet rate}}{n\text{-jet rate}} \approx 0.2, n=1,\dots,6 (!)$$

Rises to 0.3 after VBF cuts!

arXiv:1304.7098

- \* NLO is only one more emission  
Consistently need to combine orders  
to describe data



# Merging Higher Orders

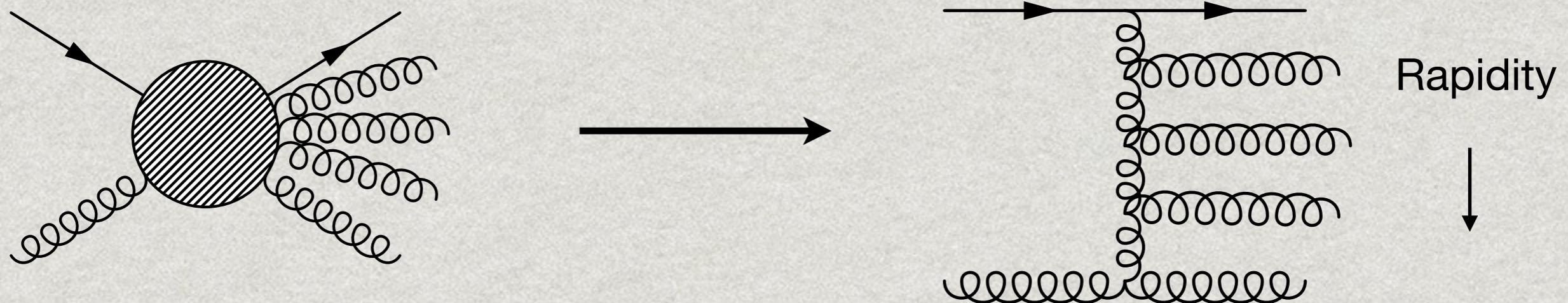
- \* NLO + Parton Shower: **POWHEG, MC@NLO**
- \* New approaches available to merge NLO at different orders. **Lönnblad & Prestel (UNLOPS), Plätzer**
- \* Alternatively: calculate all-orders in the first place!
- \* High Energy Jets provides systematic description of hard, wide-angle emissions at all orders
- \* Price: have to approximate the matrix element

# High Energy Limit

- \* The High Energy (Multi-Regge) limit is:

$$s_{ij} \rightarrow \infty, \quad |p_{\perp i}| \sim |p_{\perp j}|, \quad i, j = 1, \dots, n$$

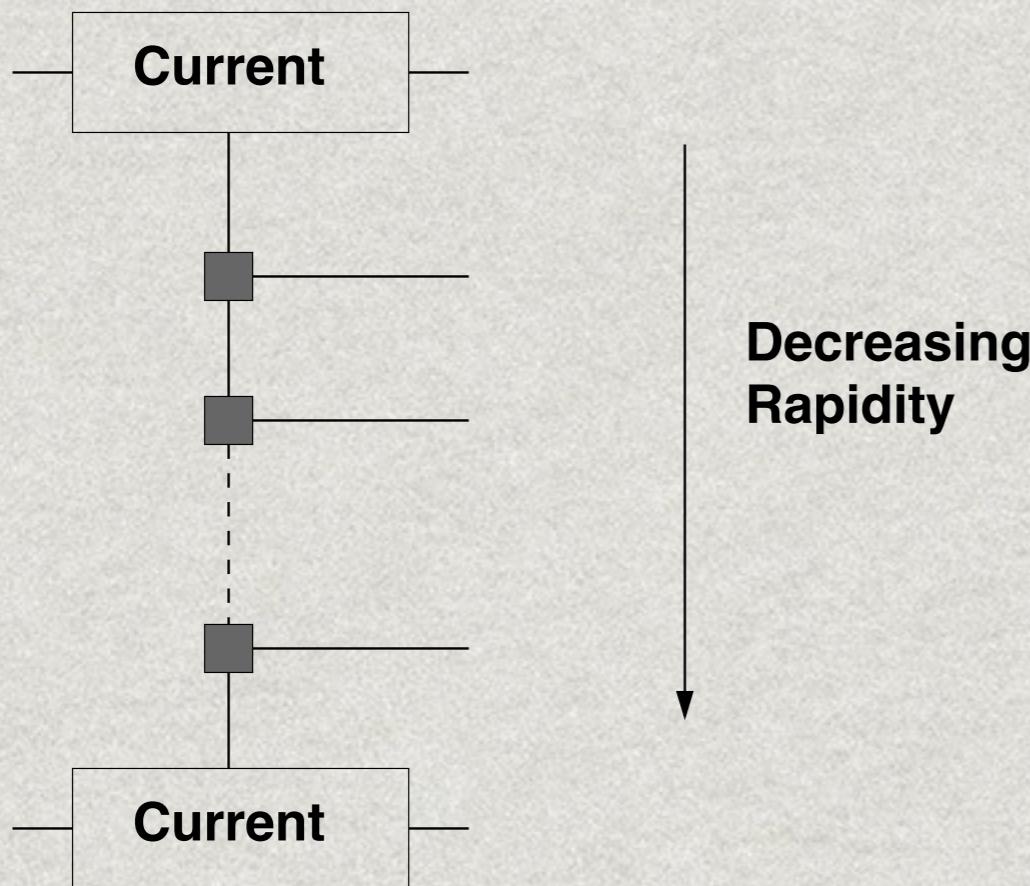
In practice, particles spread out in rapidity



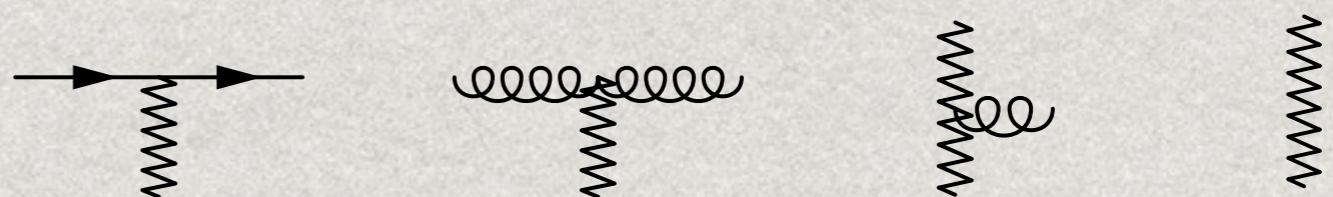
- \* Dominant Momentum Configurations in HE limit correspond to those which would allow maximum t-channel gluon exchanges:
- \* Other orderings are logarithmically suppressed.

# A HEJ Amplitude

- \* All scattering amplitudes factorise in this limit  
⇒ Can exploit this to build a simple approximation.



- \* A HEJ amplitude is structured:  
current-current  
x product-of-emissions

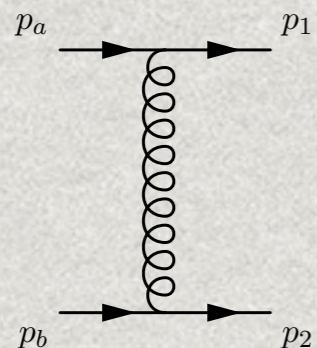


Applies to loop diagrams too (needed to regulate soft).

# Pieces I: Currents

Pieces independent of rest of chain - pick convenient processes

- \* Incoming quarks: straight-forward

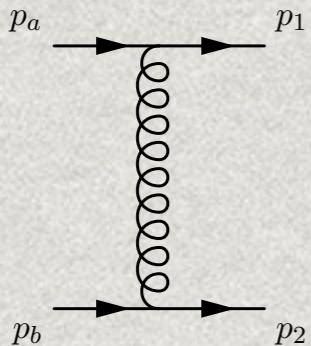


$$\frac{8g_s^4}{9} \frac{|j^\mu(p_a, p_1) \cdot j_\mu(p_b, p_2)|^2}{\hat{t}^2} = \frac{4g_s^4}{9} \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2}$$

# Pieces I: Currents

Pieces independent of rest of chain - pick convenient processes

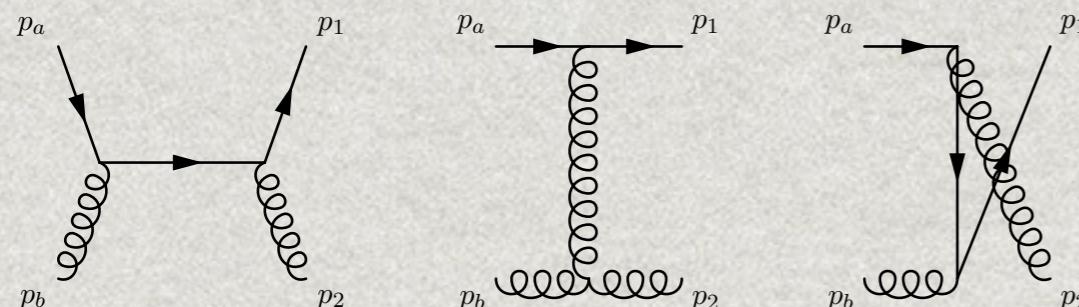
- \* Incoming quarks: straight-forward



$$\frac{8g_s^4}{9} \frac{|j^\mu(p_a, p_1) \cdot j_\mu(p_b, p_2)|^2}{\hat{t}^2}$$
$$= \frac{4g_s^4}{9} \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2}$$

- \* Incoming gluons: surprisingly so!

- \* Exact result:  $\frac{g_s^4 C_{CAM}}{6} \frac{|j^\mu(p_a, p_1) \cdot j_\mu(p_b, p_2)|^2}{\hat{t}^2}$

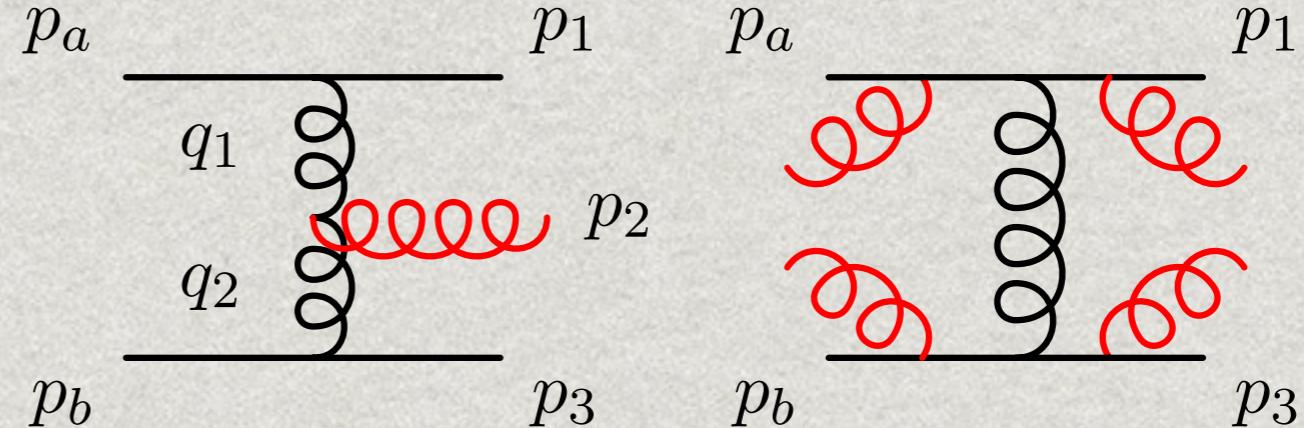


with  $C_{CAM} = \frac{1}{2} \left( C_A - \frac{1}{C_A} \right) \left( \frac{p_b^-}{p_2^-} + \frac{p_2^-}{p_b^-} \right) + \frac{1}{C_A}$

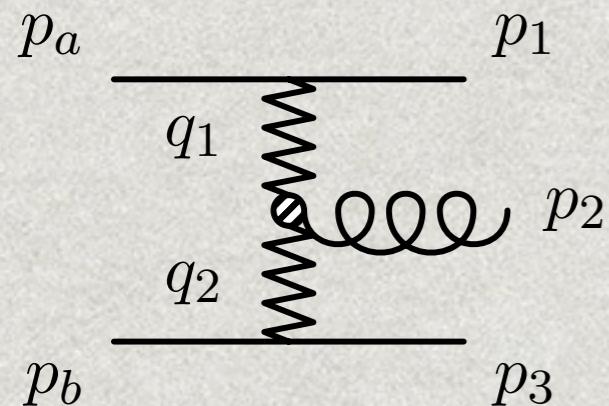
- \* Only t-pole remains explicitly

# Pieces II: Emission Vertices

- \* Use  $qQ \rightarrow qgQ$



- \* In HE limit, colour factors combine to give



$$\mathcal{A}_{qQ \rightarrow qgQ} = g_s^3 \mathcal{C}_g \varepsilon_\rho^* \frac{j^\mu(p_a, p_1) \cdot j_\mu(p_b, p_3)}{q_1^2 q_2^2} V^\rho(q_1, q_2)$$

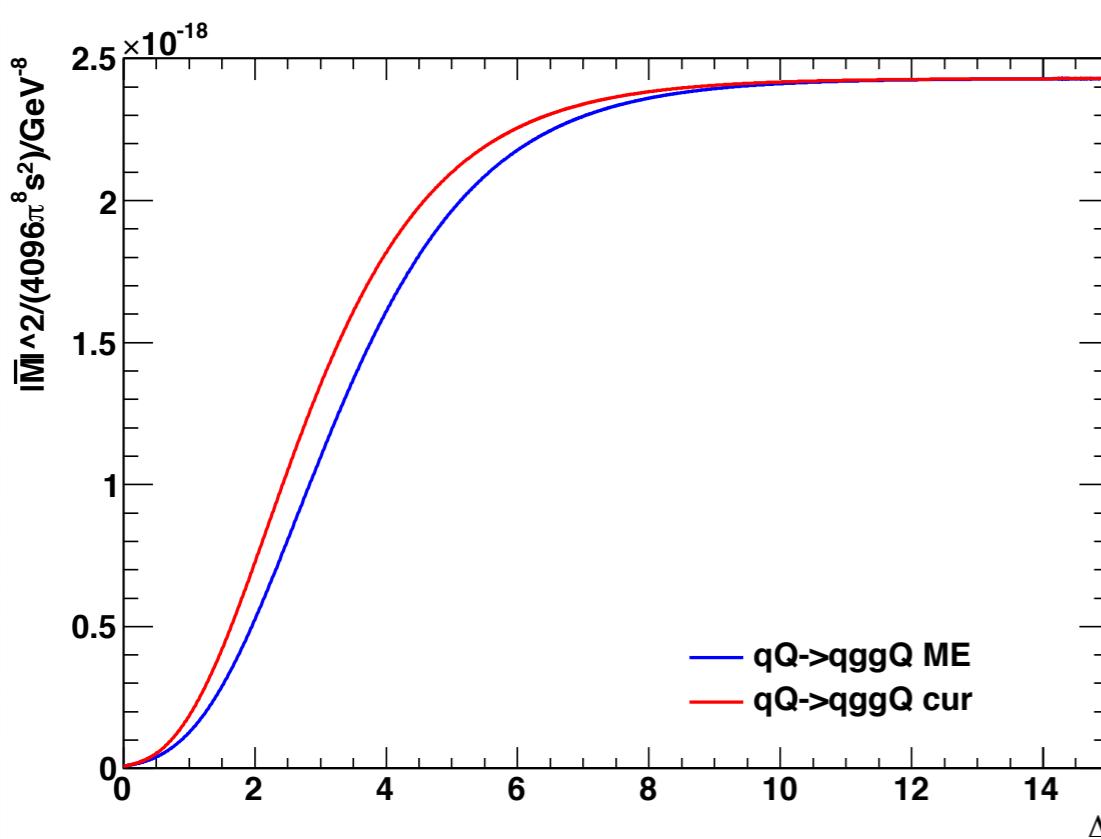
$$V^\rho(q_1, q_2) = - (q_1 + q_2)^\rho$$

$$+ \frac{p_a^\rho}{2} \left( \frac{q_1^2}{p_2 \cdot p_a} + \frac{p_2 \cdot p_b}{p_a \cdot p_b} + \frac{p_2 \cdot p_3}{p_a \cdot p_3} \right) + p_a \leftrightarrow p_1$$

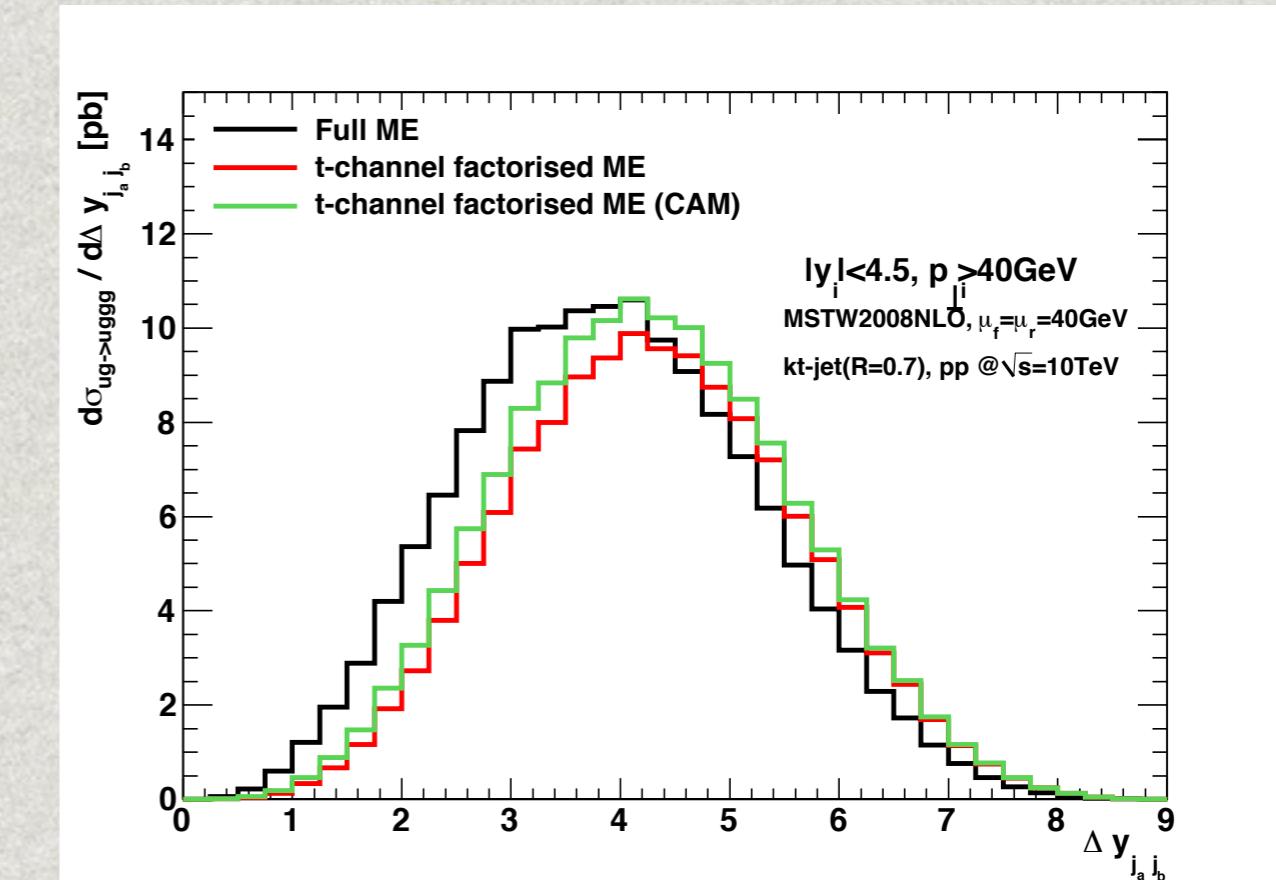
$$- \frac{p_b^\rho}{2} \left( \frac{q_2^2}{p_2 \cdot p_b} + \frac{p_2 \cdot p_a}{p_b \cdot p_a} + \frac{p_2 \cdot p_1}{p_b \cdot p_1} \right) - p_b \leftrightarrow p_3.$$

Gauge invariant in *all* of phase space.

# Does It Work?



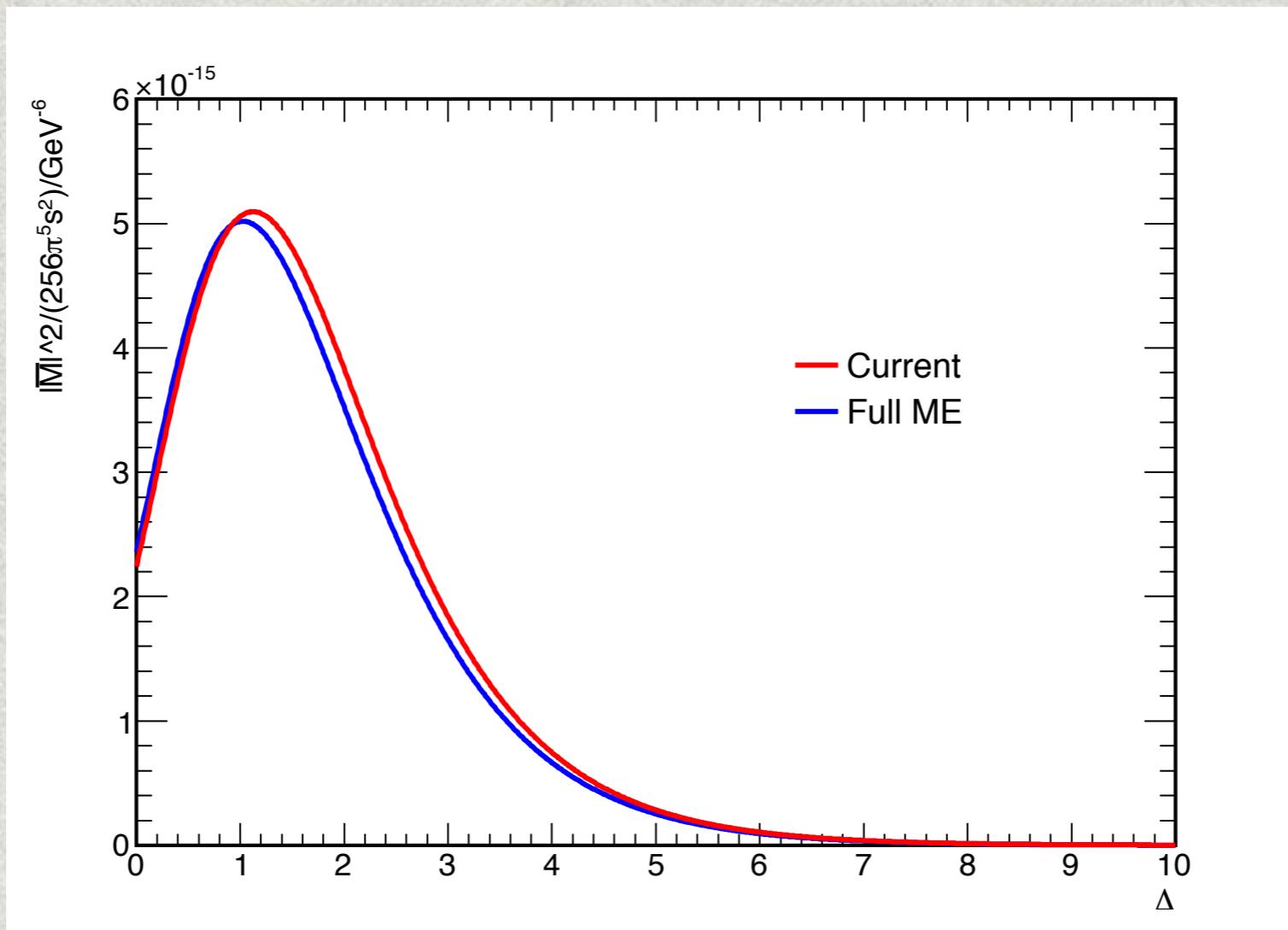
$qQ \rightarrow qggQ$



$qg \rightarrow qggg$

# Even when it's not supposed to!

Gluon now pulled forward of both quarks:



$\text{us} \rightarrow \text{usg}$

# Pieces III: Regulation

Last part is to regulate divergences when  $p_i \rightarrow 0$

HE limit of virtual corrections is given by the Lipatov Ansatz

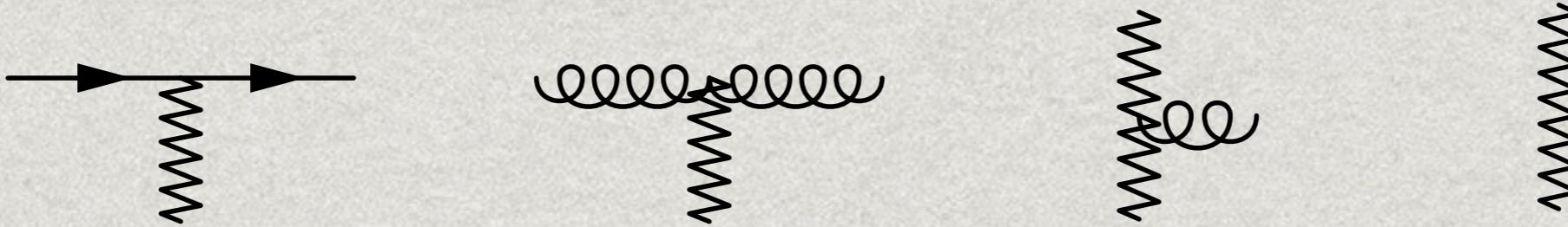
$$\text{---} = \frac{1}{t_i} \exp[\hat{\alpha}(q_i)(y_{i-1} - y_i)]$$

$$\begin{aligned}\hat{\alpha}(q_i) &= \alpha_s C_A t_i \int \frac{d^{2+2\epsilon} k_\perp}{(2\pi)^{2+2\epsilon}} \frac{1}{k_\perp^2 (q_i - k)_\perp^2} \\ &\rightarrow -g_s^2 C_A \frac{\Gamma(1-\epsilon)}{(4\pi)^{2+\epsilon}} \frac{2}{\epsilon} \left(\mathbf{q}^2/\mu^2\right)^\epsilon\end{aligned}$$

Proved to next-to-leading log

Fadin, Fiore, Kozlov & Reznichenko: [hep-ph/0602006](#)

# Assembly



Build fully-flexible Monte Carlo from these

Match to exact LO if cluster into 2, 3 or 4 jets

Add missing momentum configurations for 2,3 & 4j

Publicly available at

<http://cern.ch/hej>

Jets, W+jets, Higgs+jets, HEJ+ARIADNE

# In a Nutshell:

- \* High Energy Jets describes QCD emissions at large  $s_{ij}$

⇒ Captures hard jet production

$$s_{ij} = 2p_{Ti}p_{Tj} (\cosh(y_i - y_j) - \cos(\phi_i - \phi_j))$$

- \* Opposite limit to a parton shower, which sums large contributions at small  $s_{ij}$

⇒ Good at jet substructure, underestimates rate/hardness

- \* Can combine both (but not straight-forward).

# Early Jet Results

# ATLAS: gap fraction

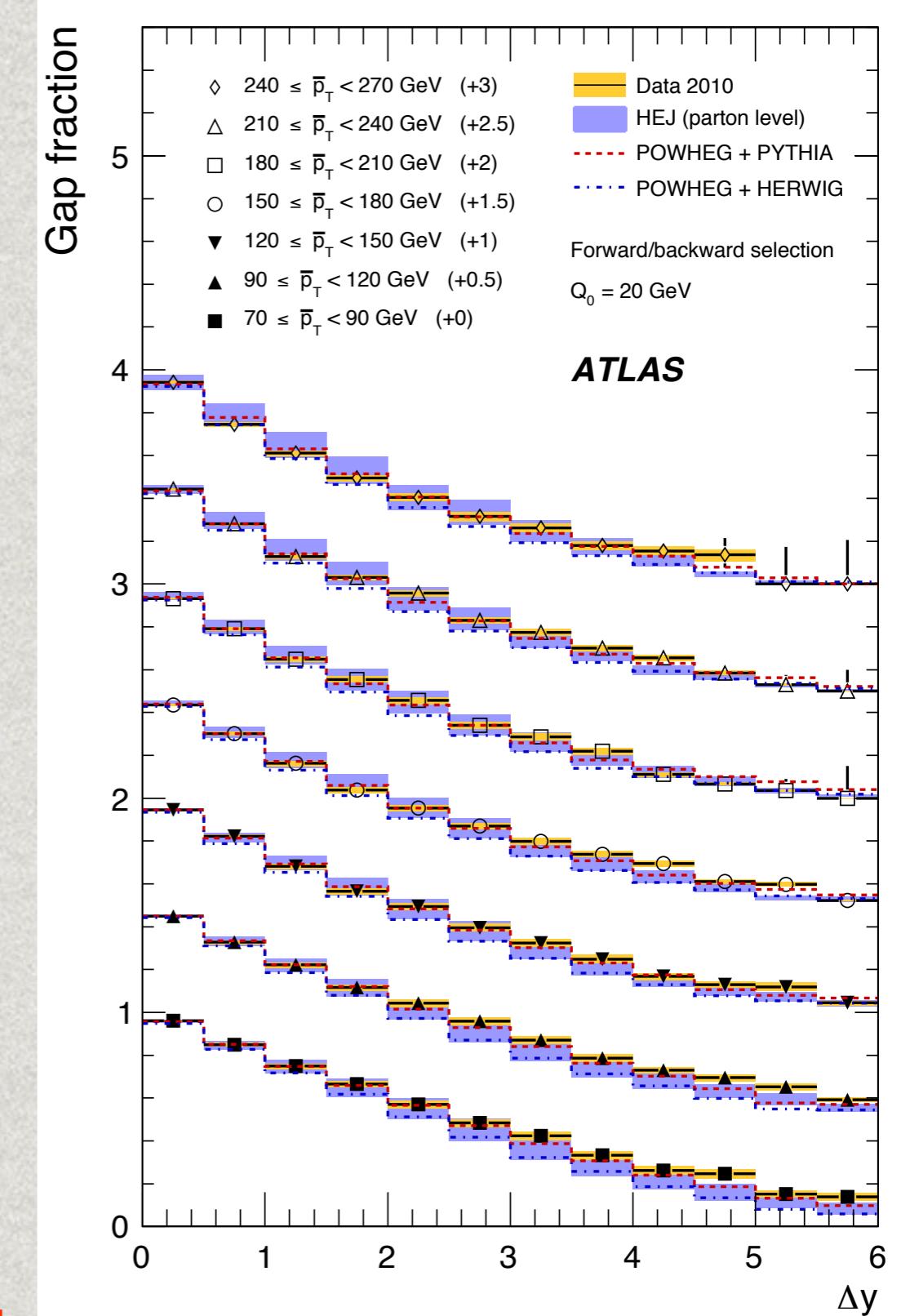
$$\text{Gap Fraction} = \frac{\sigma(\text{no jets in gap})}{\sigma(2j \text{ inclusive})}$$

$\bar{p}_T$  = average  $p_T$  of tagging jets

Tagging = most forward/  
backward

Good agreement with  
POWHEG+PYTHIA & HEJ

arXiv:1107.1641



# ATLAS: jet veto analysis

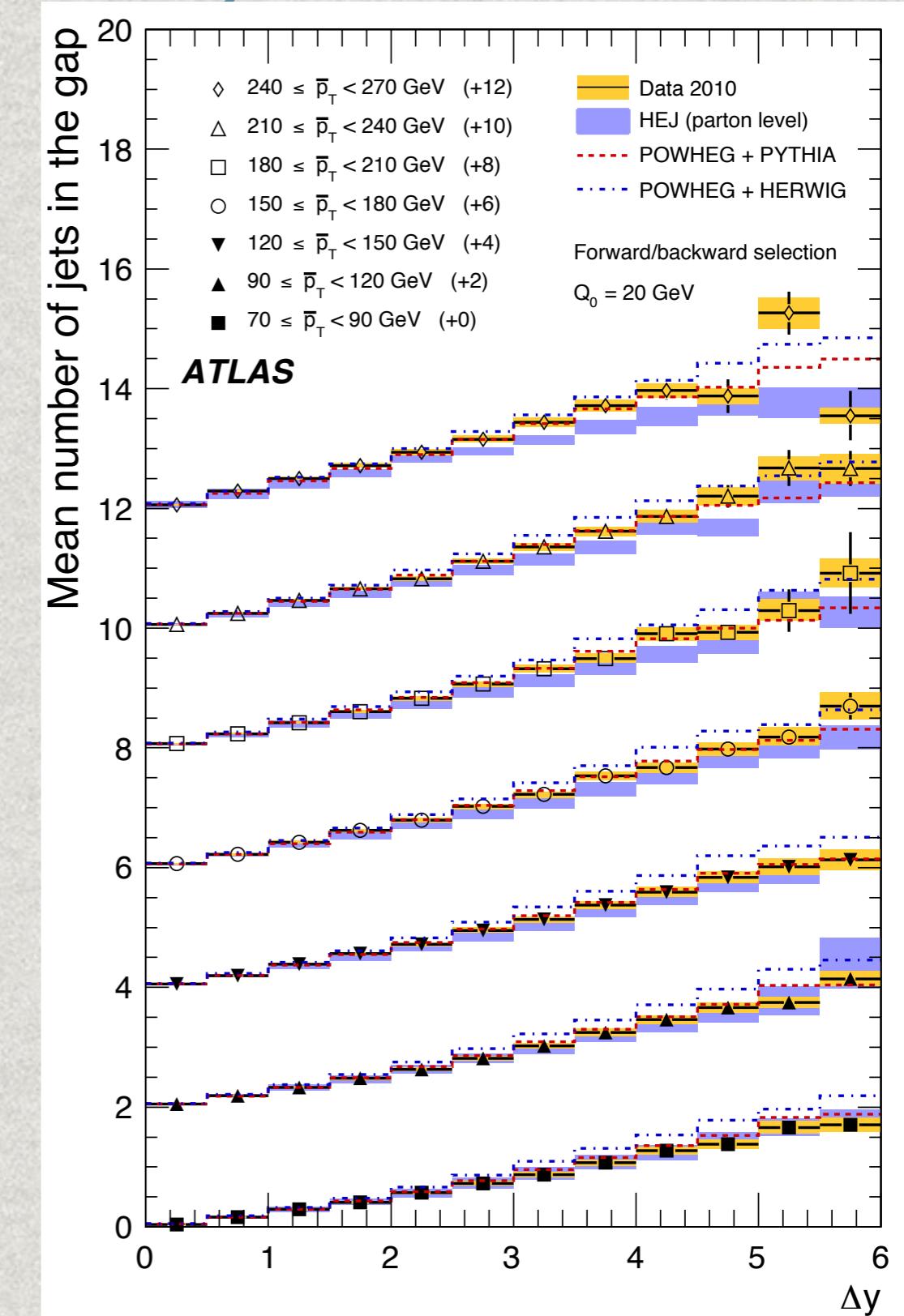
Now, average number of additional jets.

More than one extra jet on average for  $\Delta y > 3$

Clearly beyond NLO!

Tagging = most forward/backward

Still good agreement



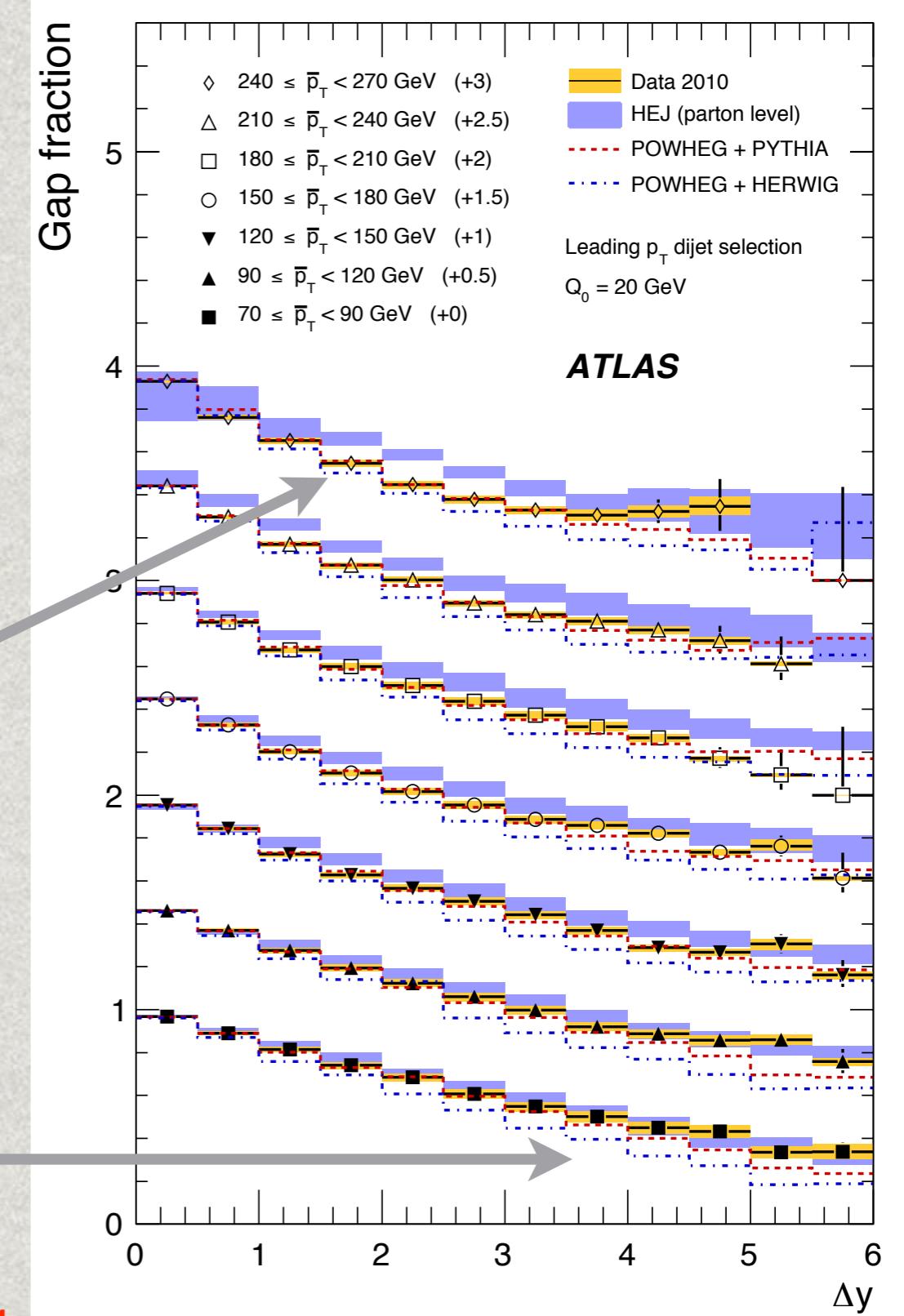
# ATLAS: gap fraction

$$\text{Gap Fraction} = \frac{\sigma(\text{no jets in gap})}{\sigma(2j \text{ inclusive})}$$

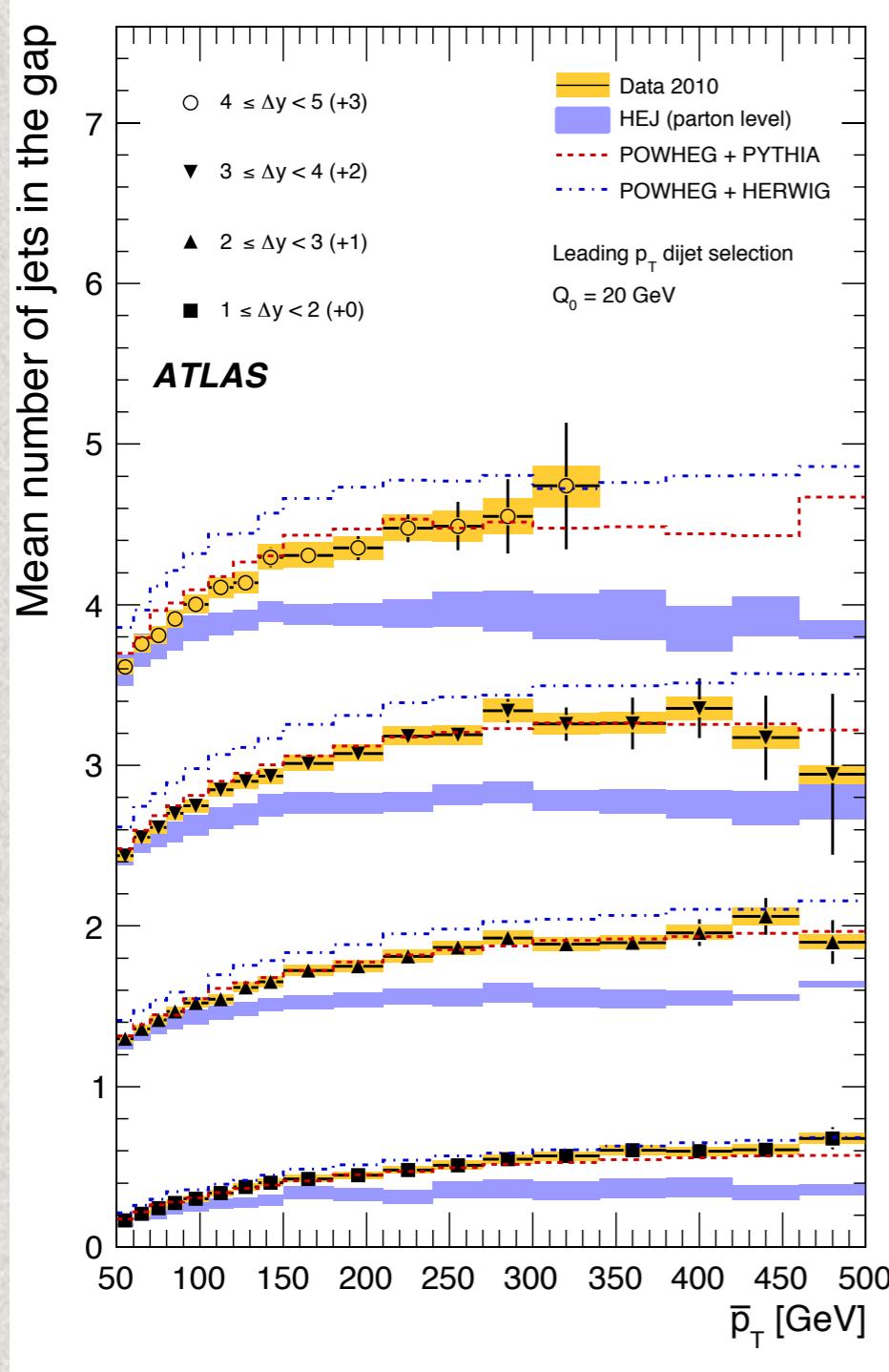
Now, tagging jets are leading  $p_T$

Hierarchy in  $p_T$  (up to factor 10!)  
 $p_T$  evolution not in HEJ

Evolution in rapidity  
 HEJ description good,  
 POWHEG undershoots

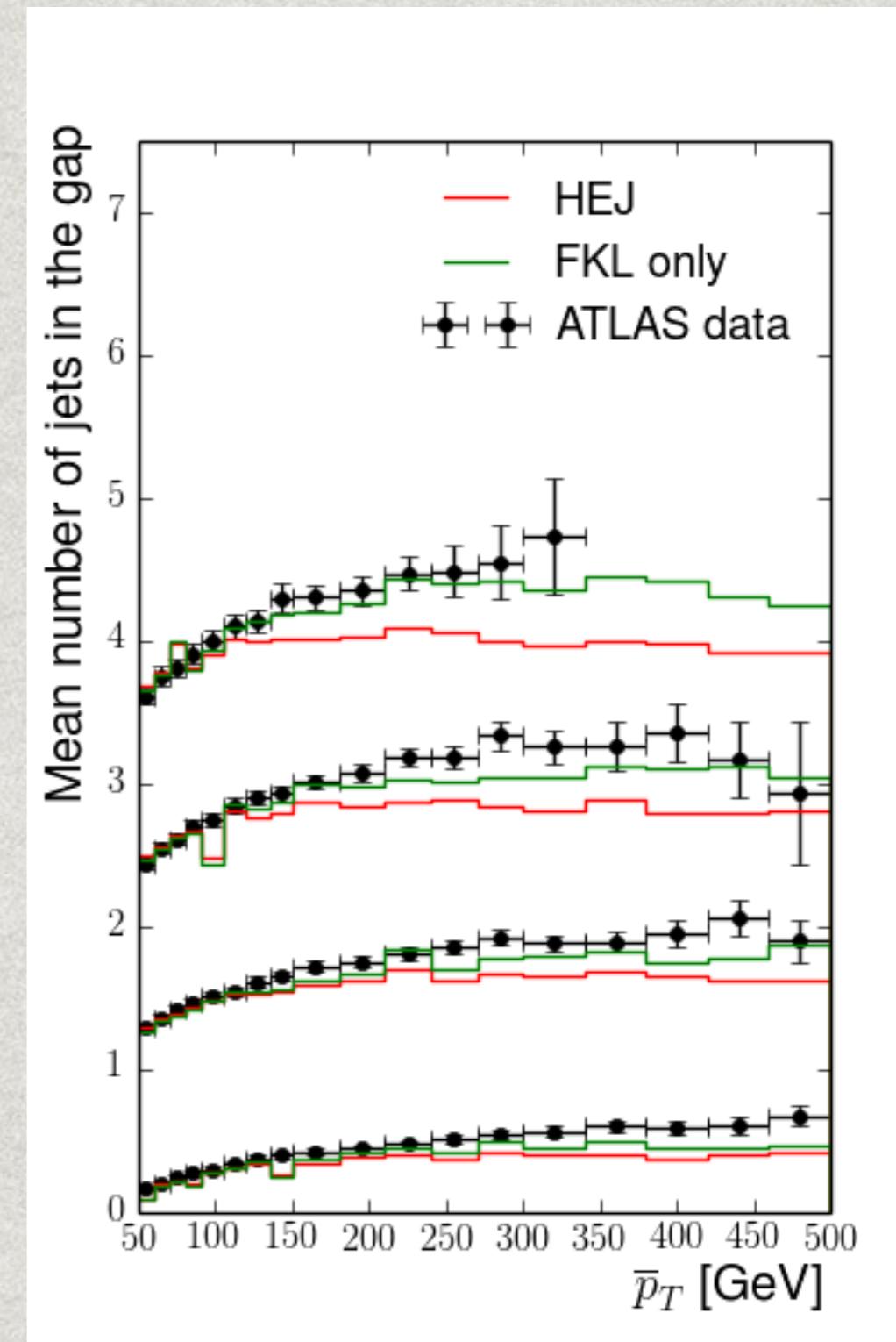


# ATLAS: What we now know!



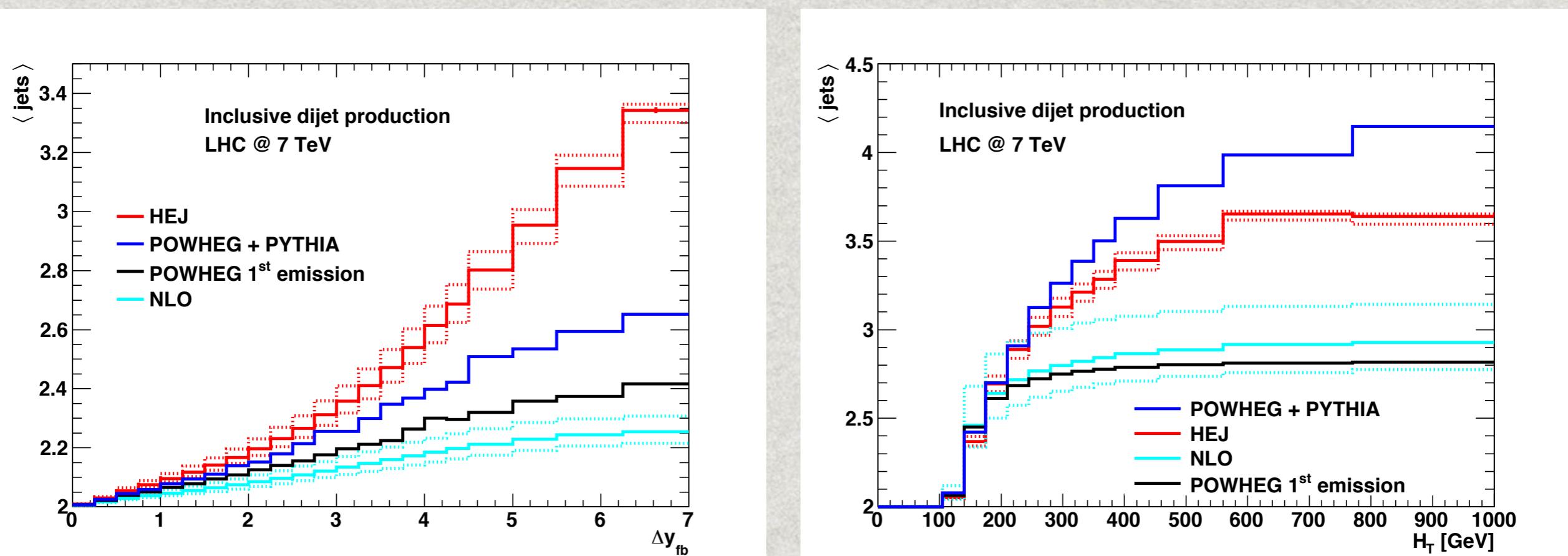
→  
Turning off  
matching (green)  
improves HEJ  
description

No resummation  
included in the  
matching and it  
dominates the  
cross section at  
large  $p_T$



# DiJet Comparison

POWHEG+PYTHIA and HEJ gave very similar predictions  
Can they be distinguished?



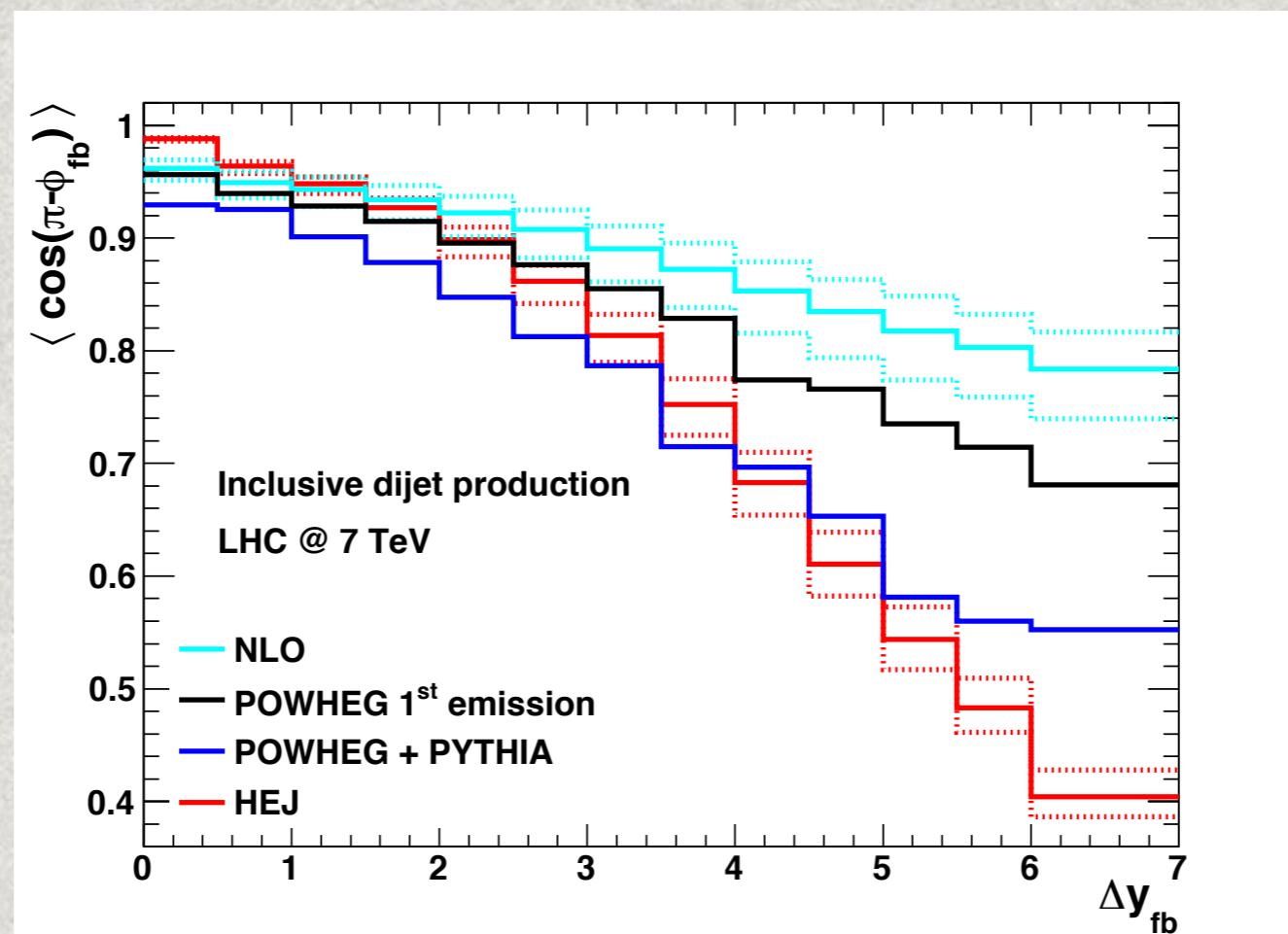
$$p_{T,j} > 35 \text{ GeV}, \ p_{T,j1} > 45 \text{ GeV}, \ |y_j| < 4.7$$

Choose cuts which do not induce  $p_T$  hierarchy

# DiJet Comparison

Other variables show little difference, e.g.  $\cos(\phi_{fb})$

$\phi_{fb}$  = azimuthal angle between forward and backward jet

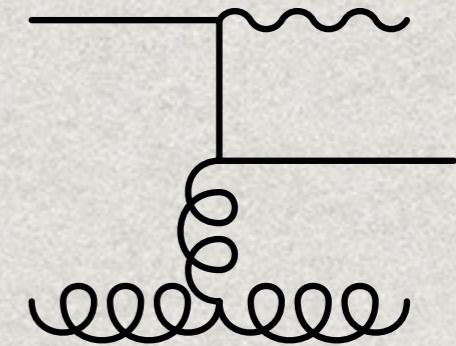


Azimuthal decorrelation gives measure of extra radiation

# Recent W+jets Results

# Extension to Ws

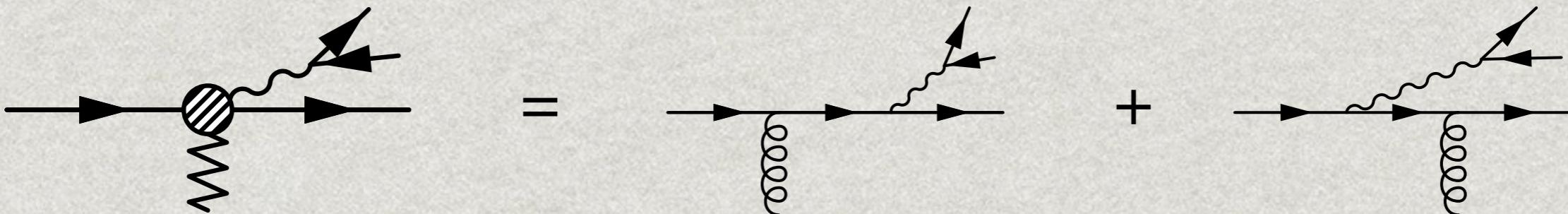
qg-channel dominant for W+nj at LHC



Treated in HE limit before, with constraint on decays

Andersen, Del Duca, Maltoni & Stirling: [hep-ph/0105146](#)

In HEJ:

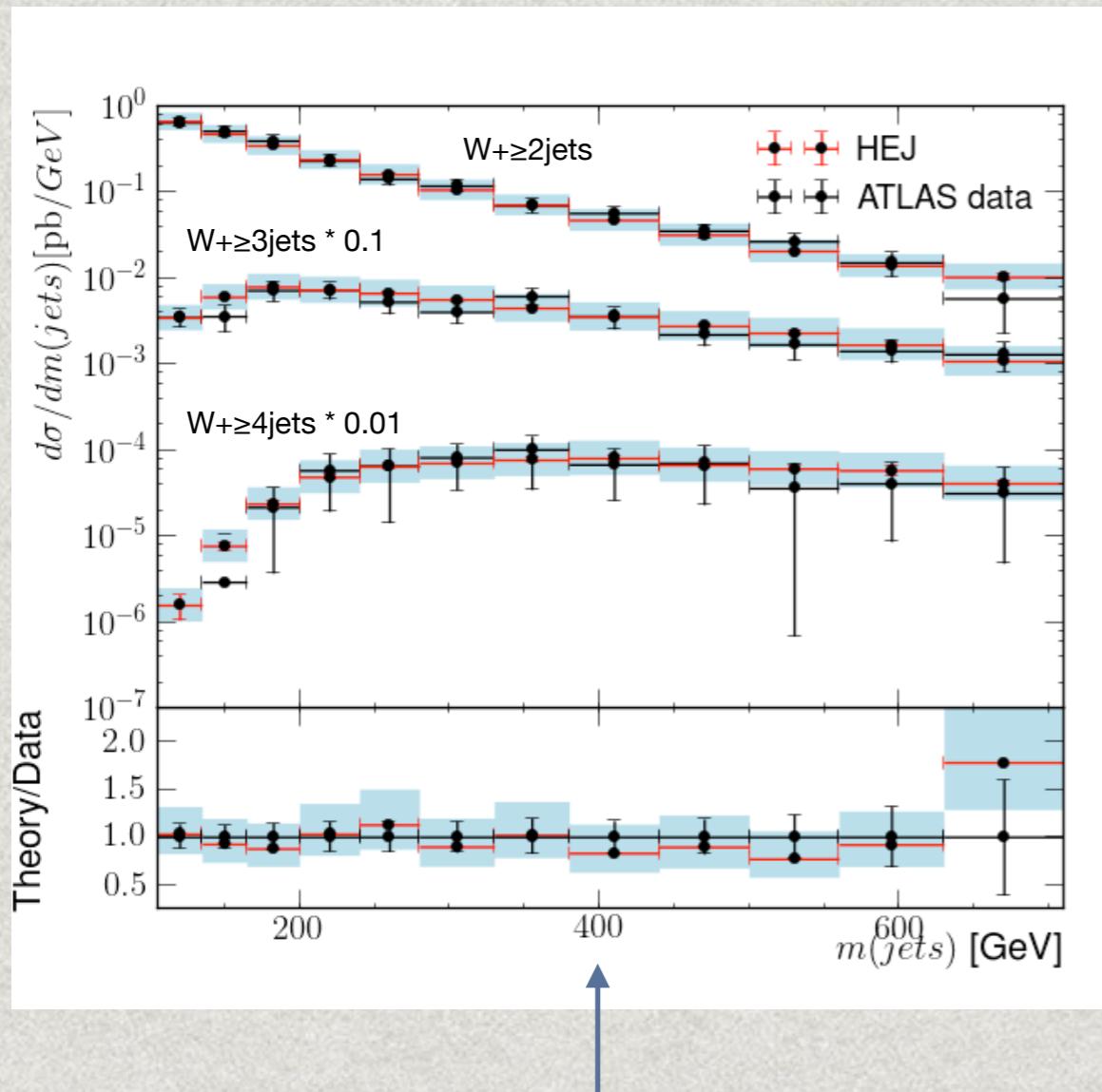


No constraints on decay products of W (or Z/ $\gamma^*$ )

Andersen, Hapola & JMS arXiv:1206.6763

# ATLAS W+dijets

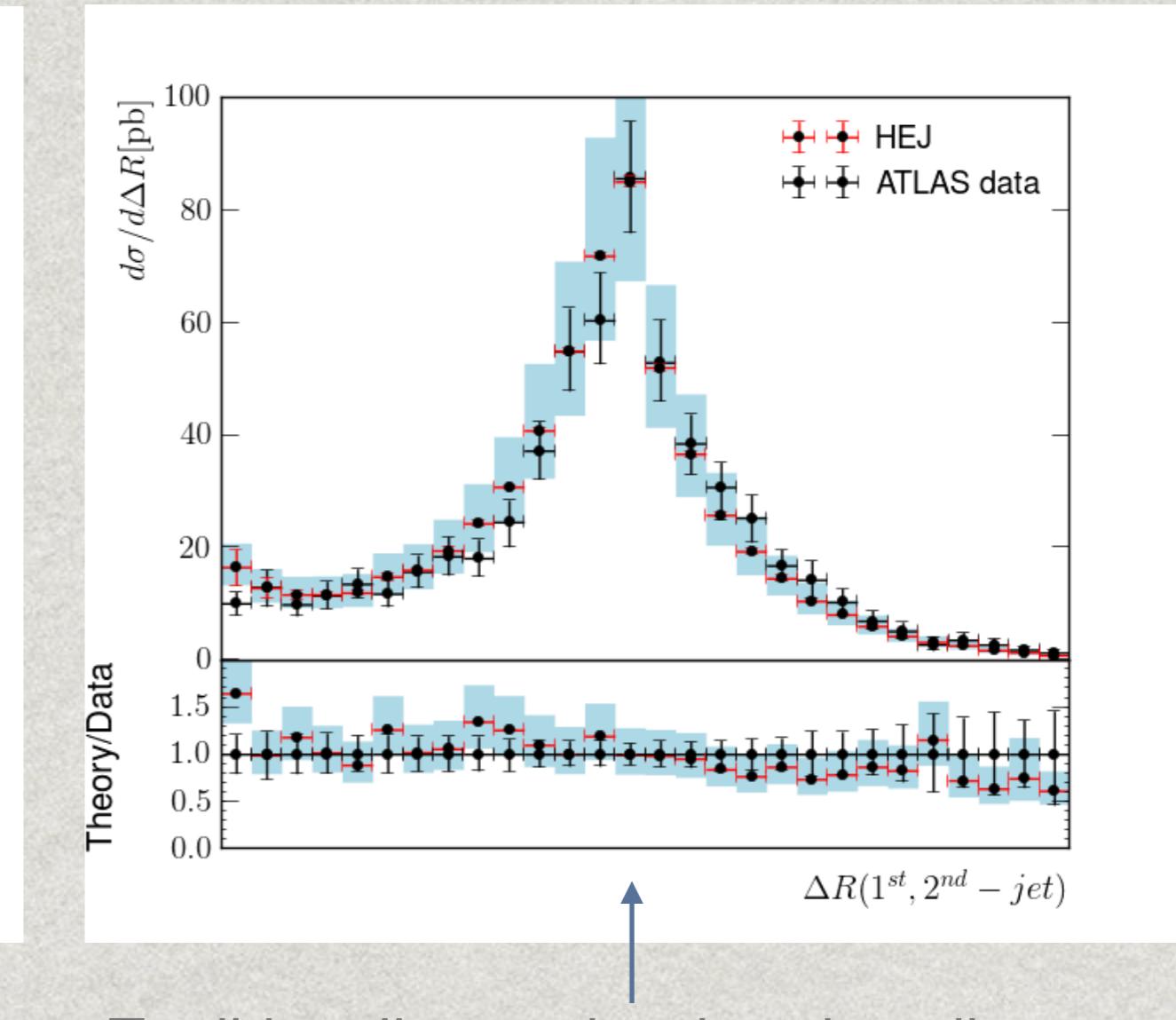
HEJ again gives good description:



Note large impact of higher orders!

ATLAS (2010) data arXiv:1201.1276

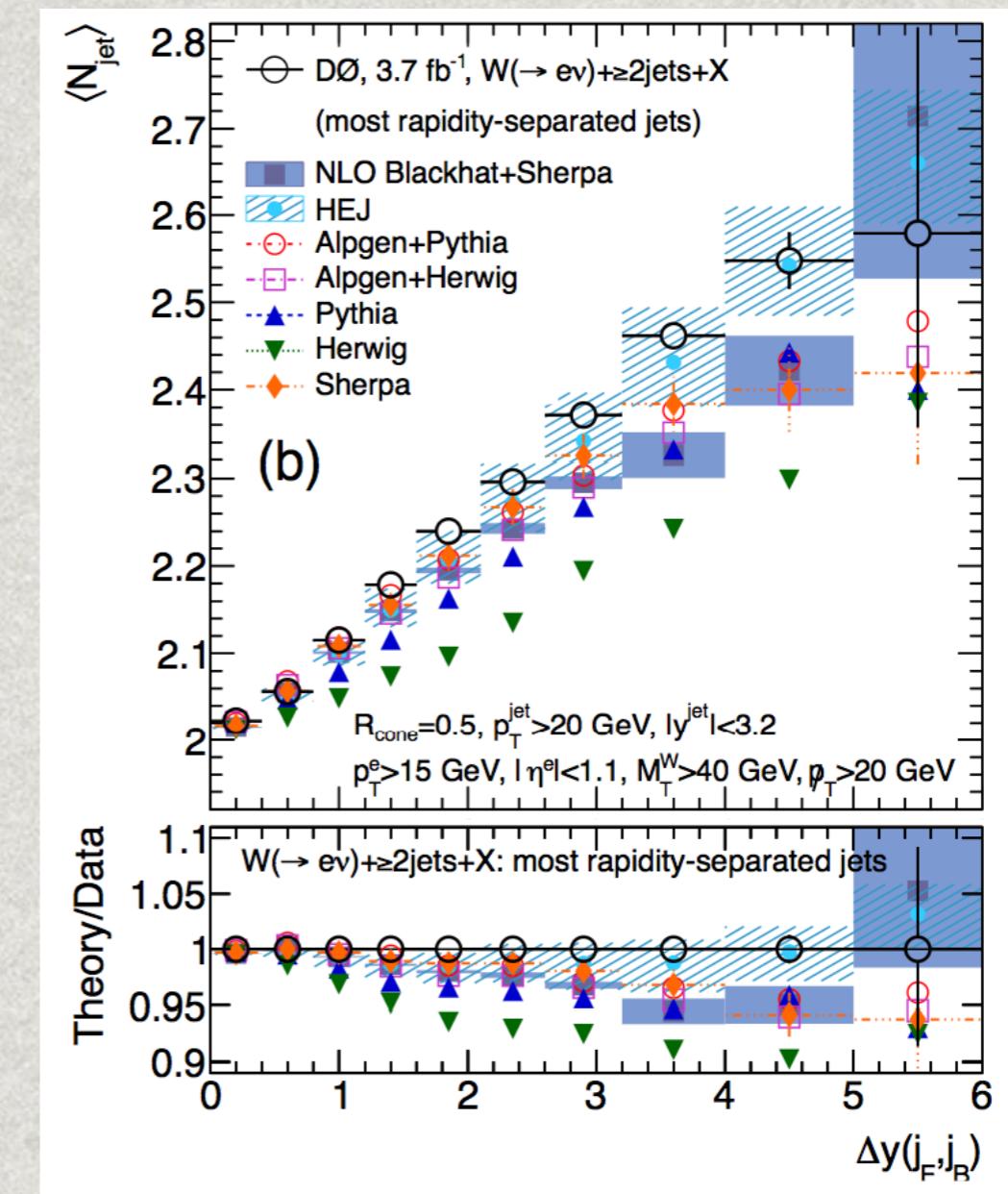
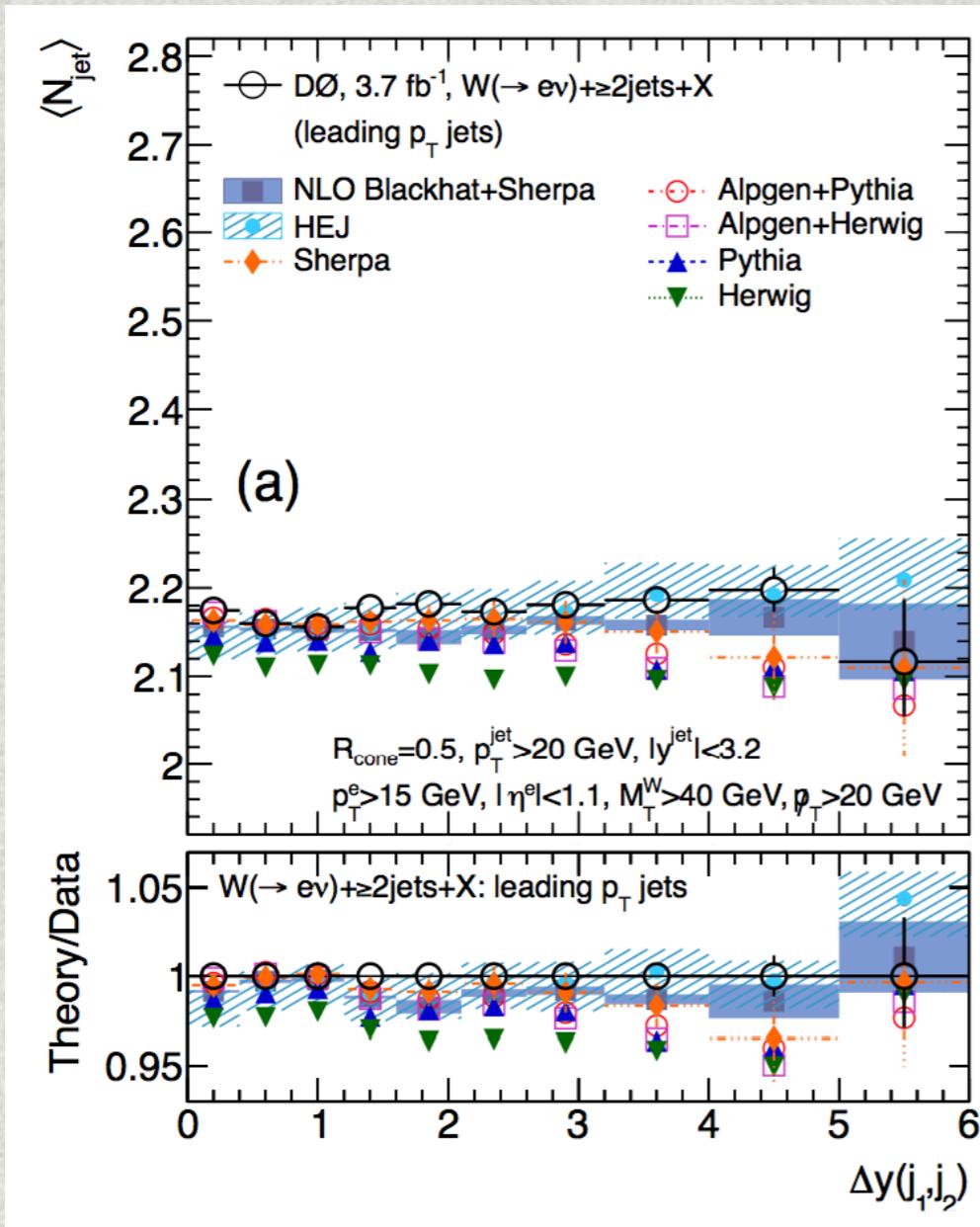
Andersen, Hapola & JMS arXiv:1206.6763



Traditionally very hard to describe  
(testing ground for state-of-the-art)  
HEJ gives good description

# D0 W+Jets

Really thorough analysis: 40 observables!



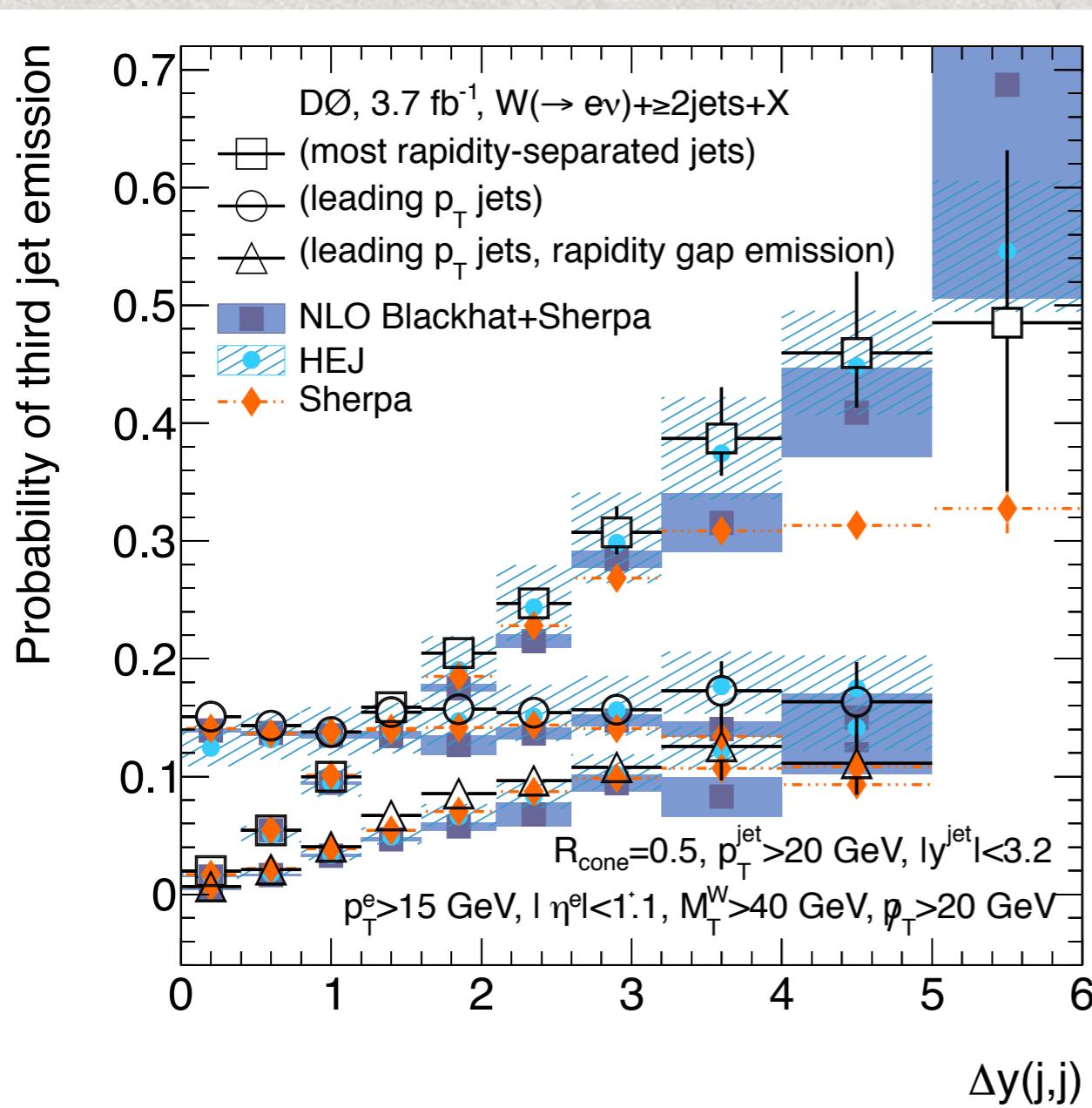
This is the difference between:  
Leading Jets

Most forward/backward Jets

arXiv:1302.6508

# D0 W+Jets

Probability of third jet emission versus  $\Delta y$  of:

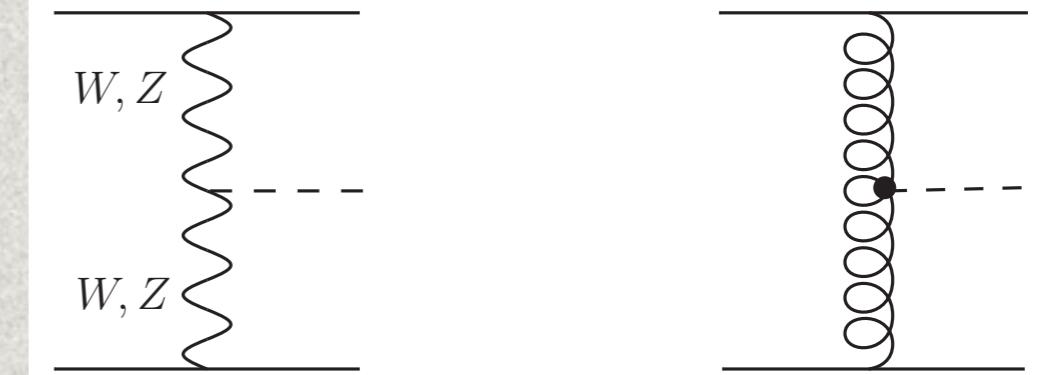


- \* Most forward/backward Jets
- \* Hardest Jets
- \* Hardest Jets, counting only jets between

# Higgs Plus Dijets

# Higgs Plus Dijets

- \* Vector Boson Fusion is 2nd largest production channel



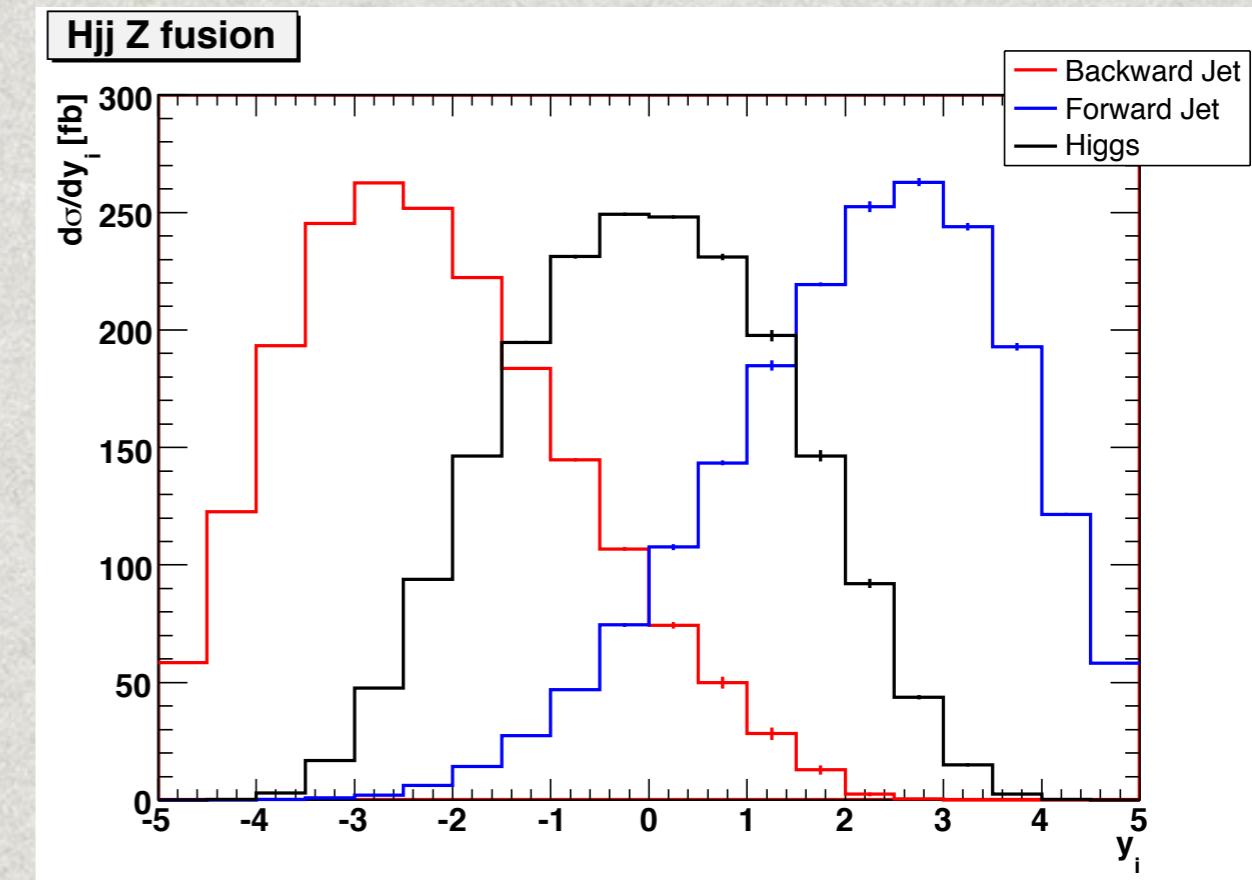
- \* Key opportunity to study VVH vertex

- \* Use distinctive topology to select events

Here:

$$p_{T,j} > 20 \text{ GeV}, |\eta_j| \leq 5,$$

$$R_{jj} > 0.6$$



# Higgs Plus Dijets

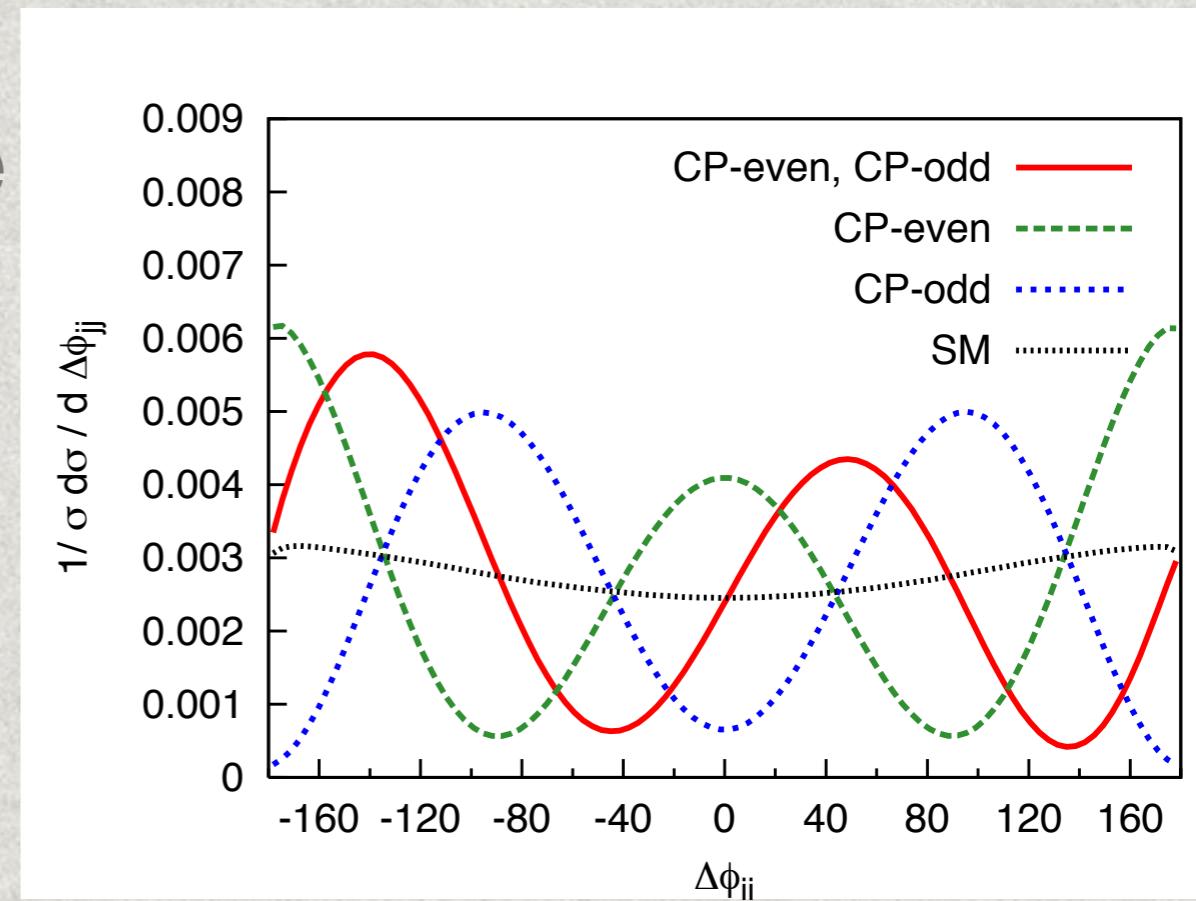
Typical “VBF” cuts:

$$p_{T,j} > 25 \text{ GeV}, |\eta_j| \leq 5, |\Delta\eta_{jj}| > 2.8, m_{jj} > 400 \text{ GeV}$$

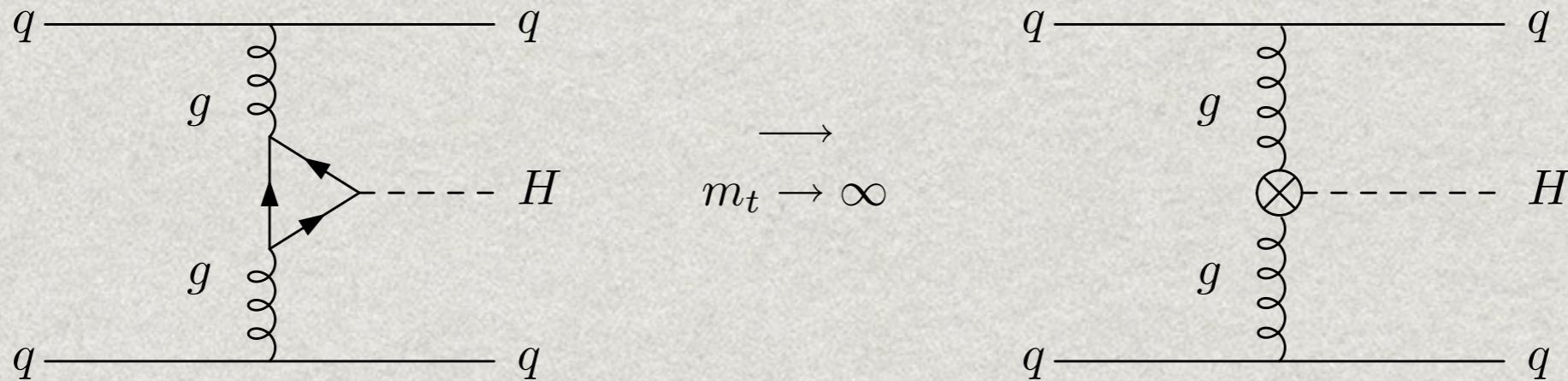
Puts us right into the difficult region!

Want to use azimuthal angle between jets to study CP structure of the vertex:

HE limit tells you how to extend to n jets



# Higgs Plus Jets



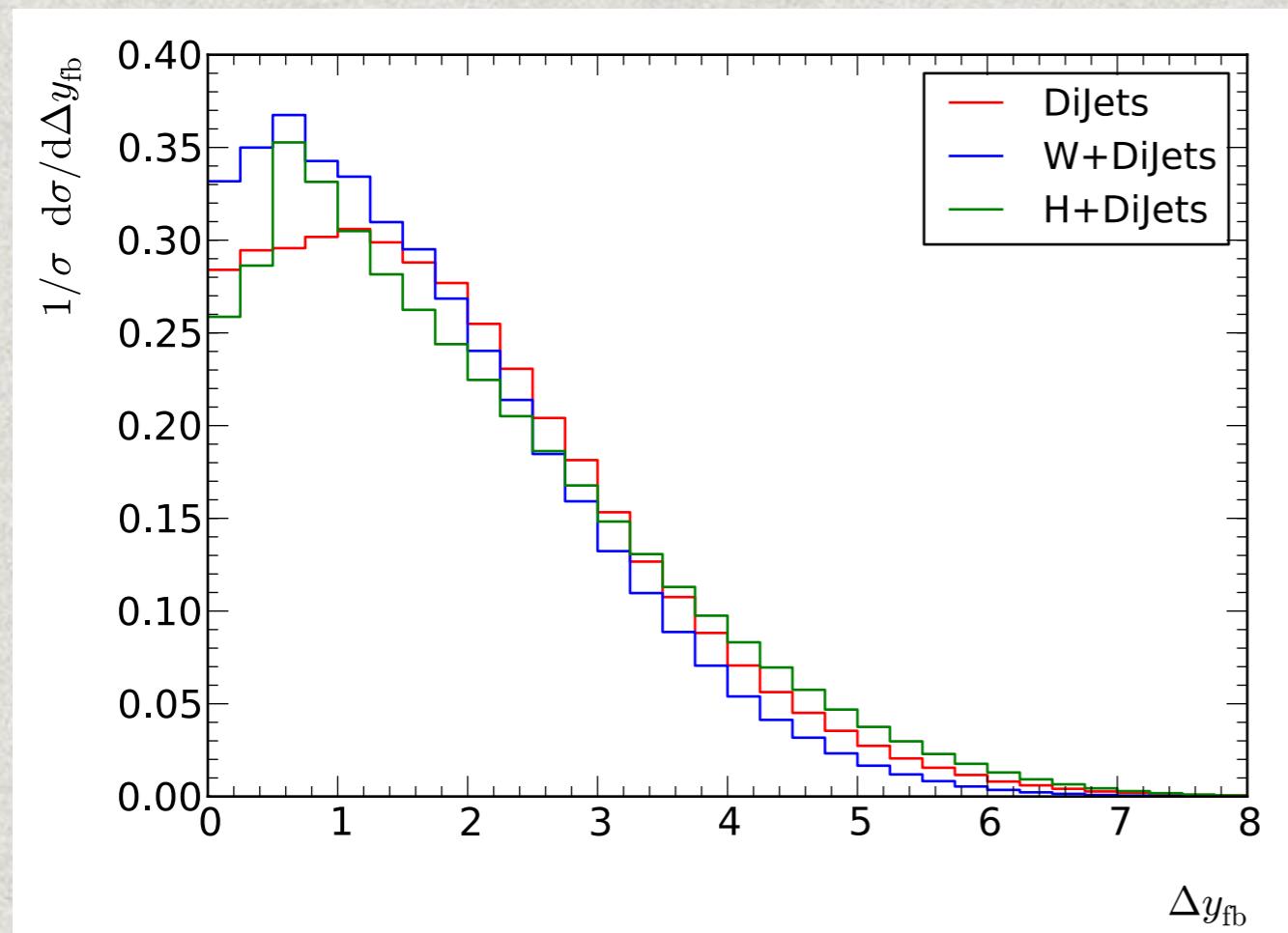
In heavy top-mass limit:  $V_{Hgg}(p^\mu, q^\nu) = \frac{i\alpha_s}{3\pi v} (p \cdot q g^{\mu\nu} - p^\nu q^\mu)$

- \* Different CP structure so can contaminate study.
- \* Interesting to study in own right
- \* Gluons expected to radiate more  
∴ use a “jet veto” between tagged jets to separate

# Multi-Jet Descriptions

To extract couplings cleanly, need to separate Weak Boson Fusion and Gluon-Gluon Fusion (ideally both!)

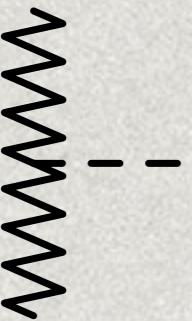
From now on, will focus on Gluon-Gluon Fusion.



Jet radiation patterns universal across processes.

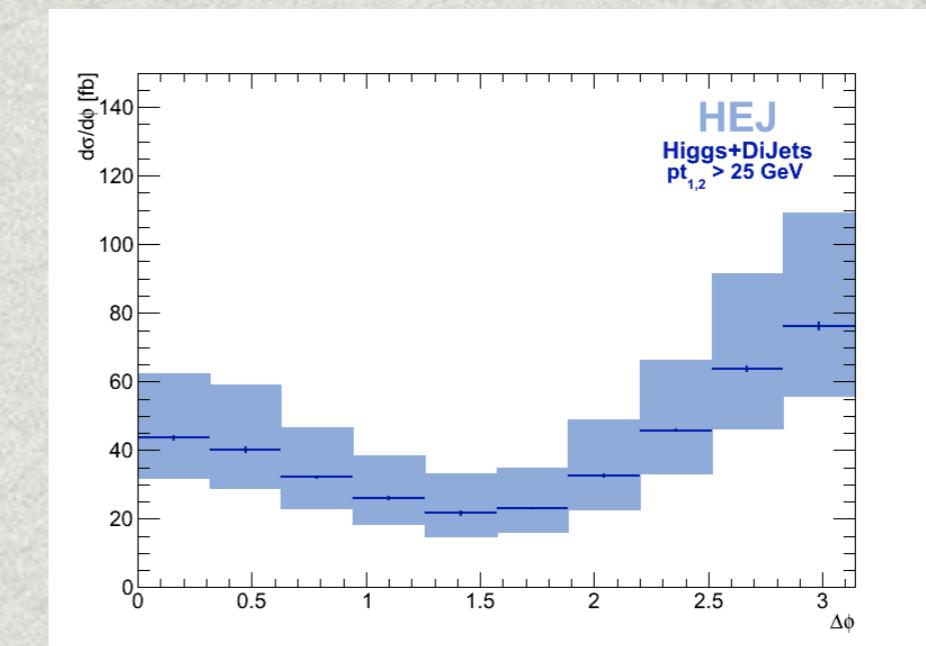
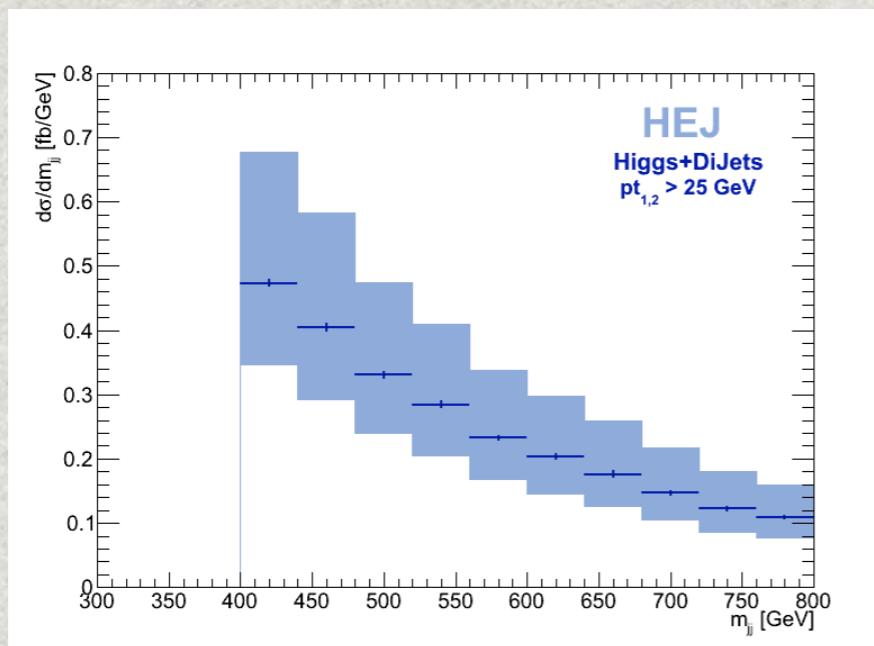
Use existing data to test descriptions.

# Higgs in HEJ



$$\frac{j^\mu j_\mu}{\hat{t}} \rightarrow \frac{j^\mu j^\nu}{q_1^2 q_2^2} (g_{\mu\nu} q_1 \cdot q_2 - q_{1\nu} q_{2\mu})$$

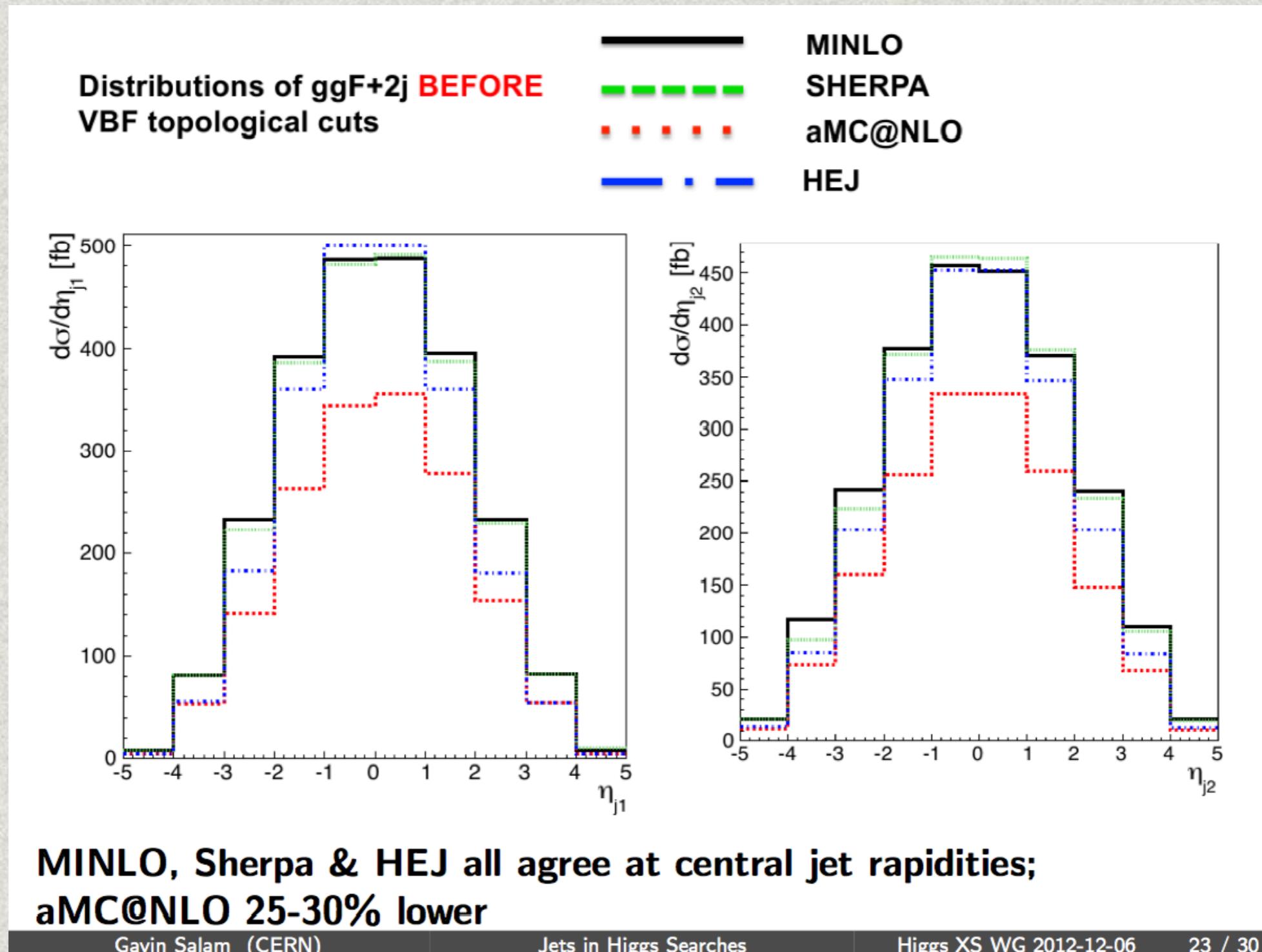
Insert this in the gluon chain according to rapidity



Now also includes one un-ordered gluon emission

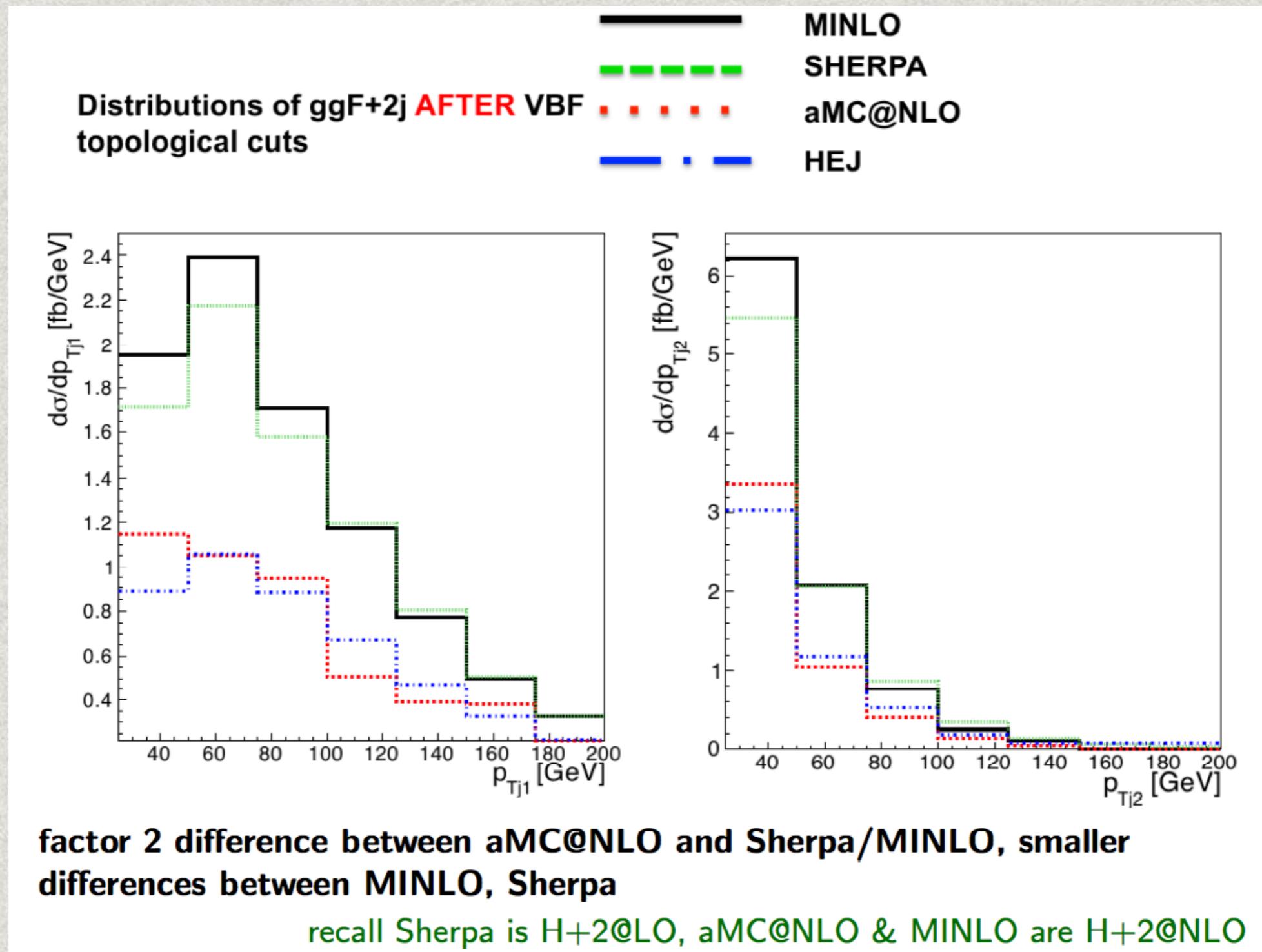
# Higgs XS WG Studies

Gavin Salam's Dec 2012 Talk:

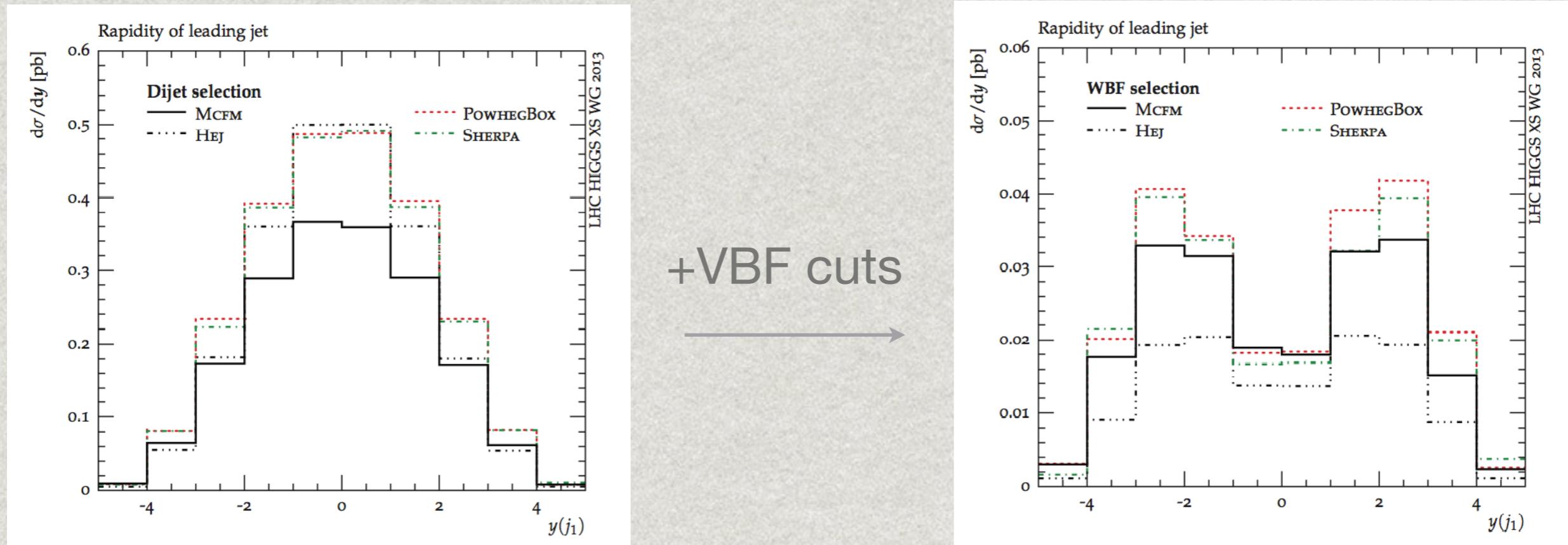


# Higgs XS WG Studies

Gavin Salam's Dec Talk:



# Higgs XS WG YR3 2013



- \* Difference in shape expected
- \* Impact on cross section:  
About 10% for MCFM, POWHEG & SHERPA; 6% for HEJ
- \* 2 effects: if well-separated jets, will typically emit a (harder) jet in between; otherwise Regge-suppression

See update in this year's LH proc

# Summary

- \* Hard QCD radiation feature of LHC collisions
- \* Data has clearly shown effects beyond pure NLO
- \* Flexible MC description from HEJ  
Built from HE properties of amplitudes
- \* Lots of interesting physics in jet data with important applications to Higgs+Jets studies

<http://cern.ch/hej>