

Future Colliders

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Lectures aims

- High energy physics
 - Particle physics reasons for pursuing higher energies
 - Relationship between hadron and lepton colliders
- High energy acceleration
 - Luminosity
 - Limits on energy, luminosity, particle production
 - How these limits relate to existing and proposed colliding facilities

Physics of colliders

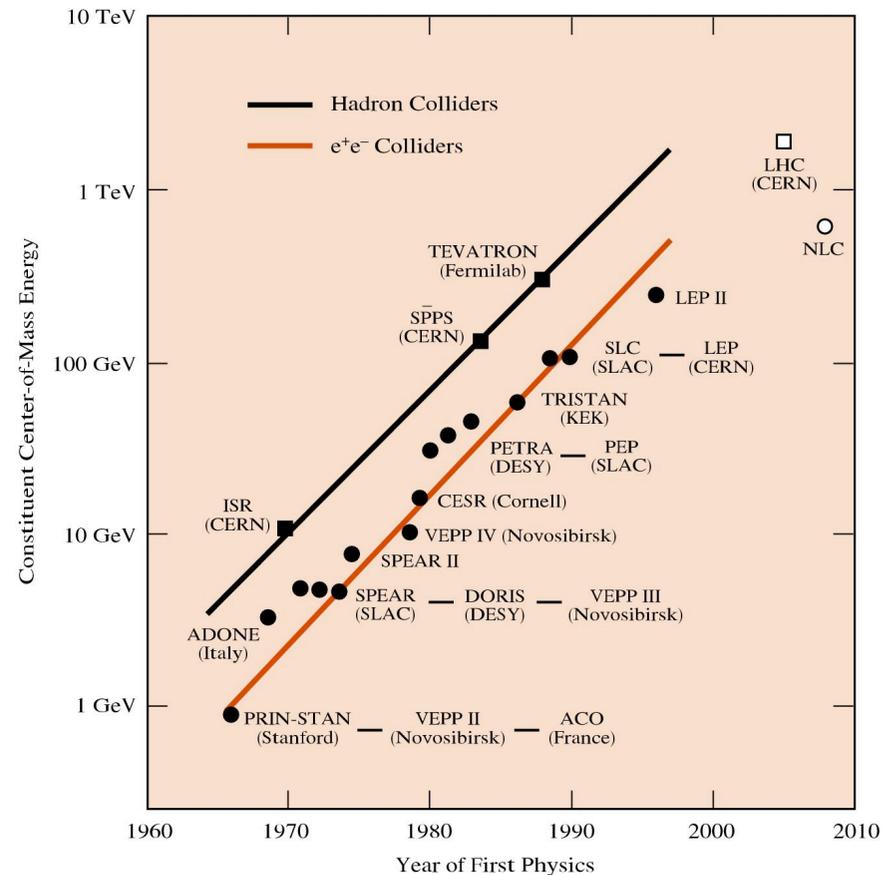
- Particle accelerators immensely powerful tools for understanding the standard model
- Long history of colliding beam experiments
- Review history and future possibilities are examined in this lecture
- Quick review of the particle physics (there is no point building a future facility if there is no physics)
- Technical challenges, limitations
- More sociological and financial challenges

Why accelerators?

- Prepare collisions using accelerator system
- Definite knowledge of particle species, energy and luminosity
- Other considerations
 - Polarisation
 - Lifetime
 - Radiation

Accelerator development

- Long history of high energy acceleration
- Proton-(anti-)Proton
- Electron-Positron
- Electron-hadron
- Exponential increase in beam energy (Moore's law)



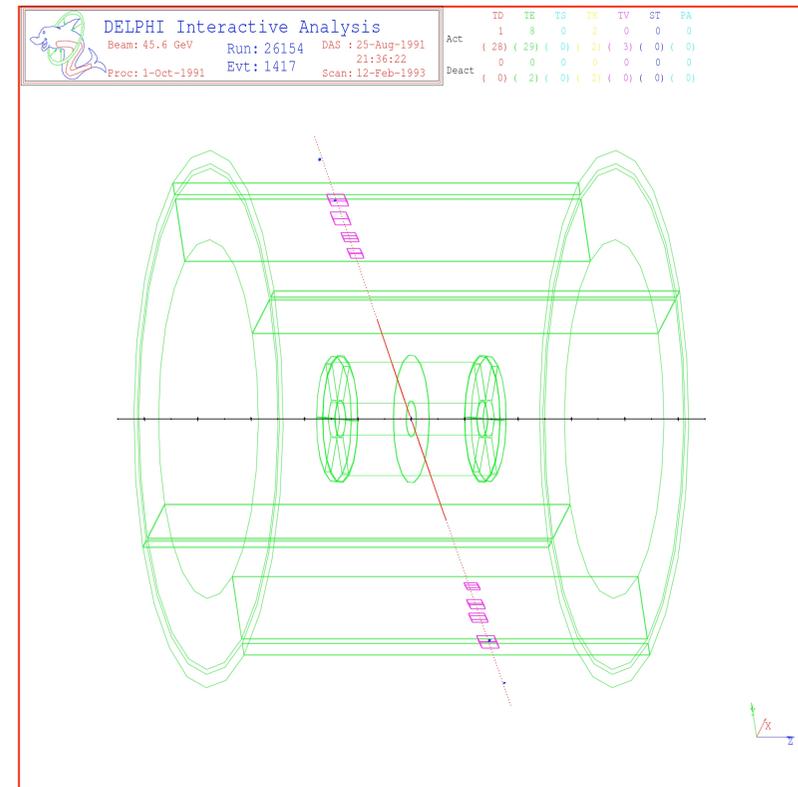
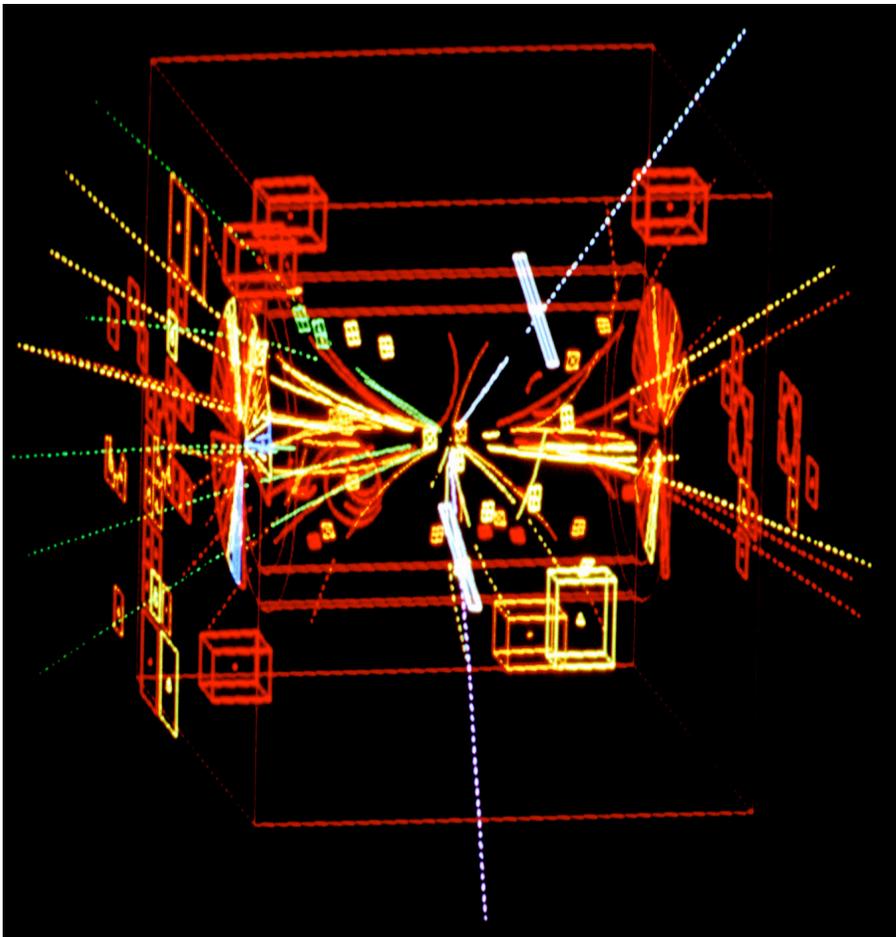
Hadron vs. Lepton colliders

- High energy acceleration has given some of the most powerful insights into constituents of matter and their interactions
 - Strong nuclear force
 - Discovery of gluons at PETRA
 - Electroweak vector bosons
 - Discovery at UA1/2
 - Precision measurement at LEP
 - Top quark and Higgs?

Z^0 discovery and measurement

$$p\bar{p} \rightarrow Z^0 + X$$

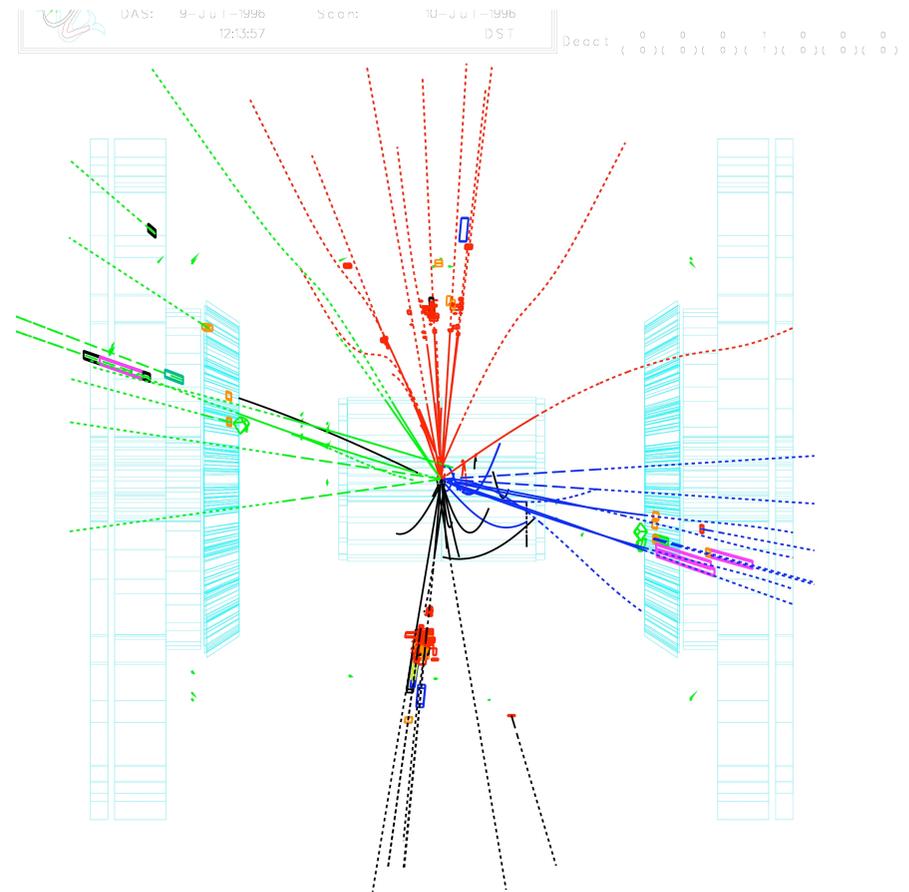
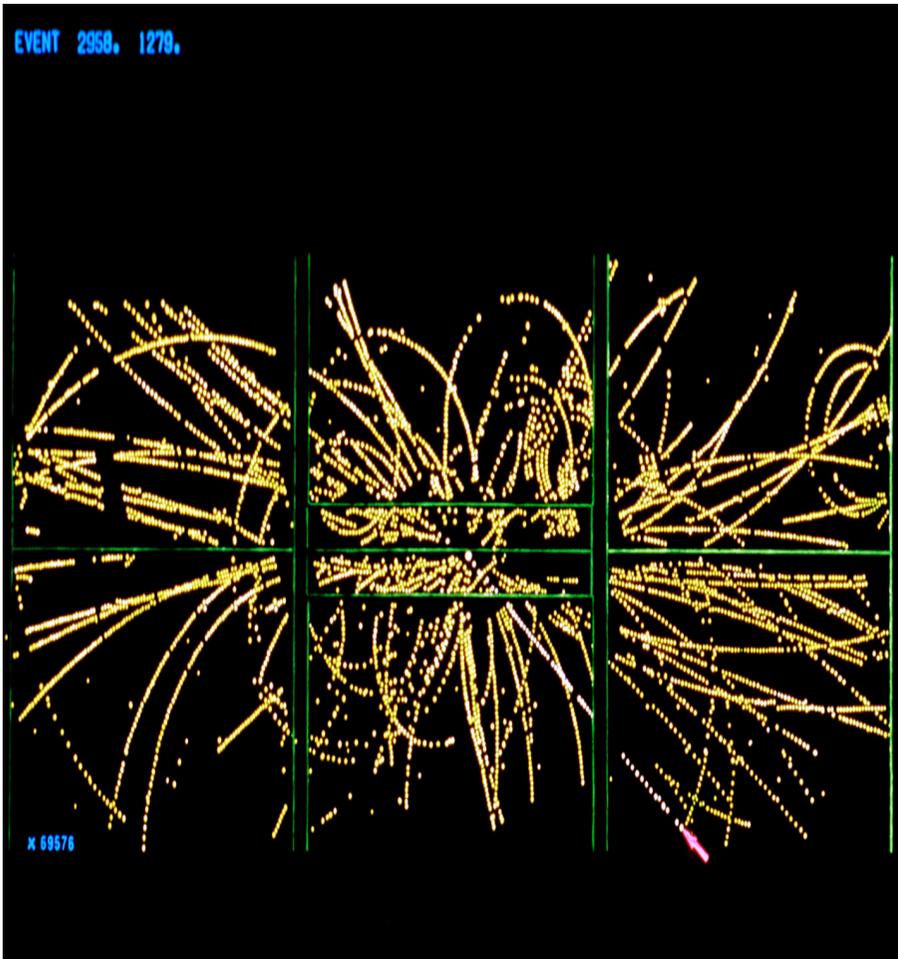
$$e^+e^- \rightarrow Z^*/\gamma \rightarrow \mu^+\mu^-$$



W discovery and measurement

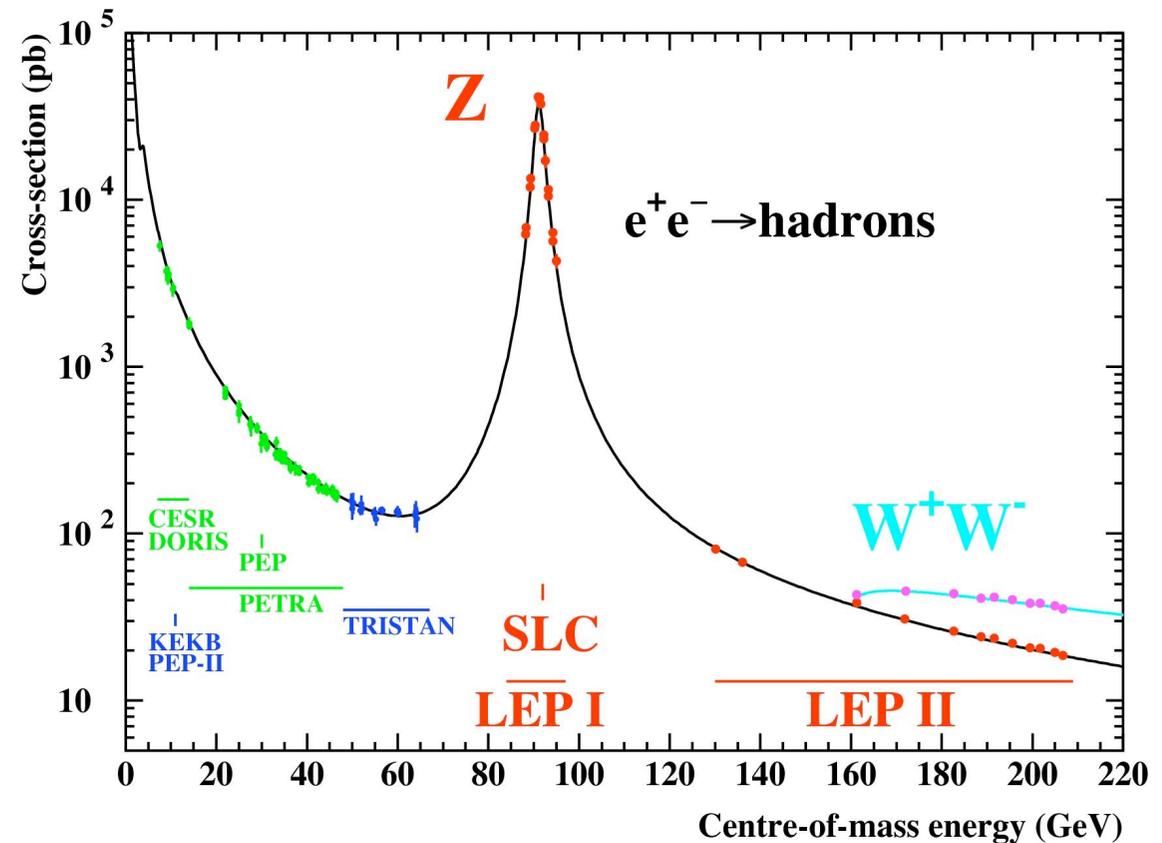
$$p\bar{p} \rightarrow W^{\pm} + X$$

$$e^{+}e^{-} \rightarrow W^{+}W^{-} \rightarrow q_1q_2 + q_3q_4$$



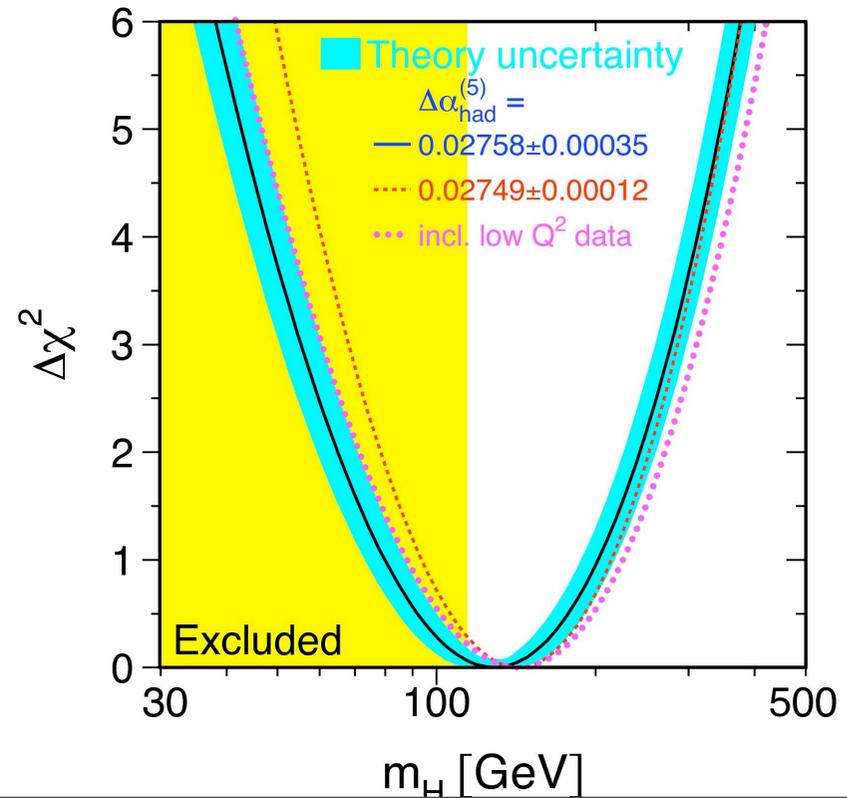
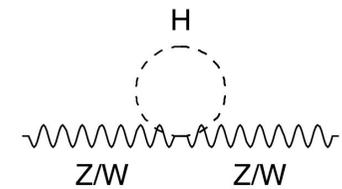
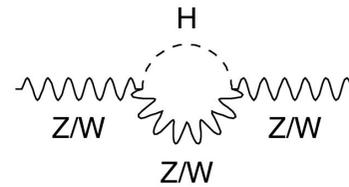
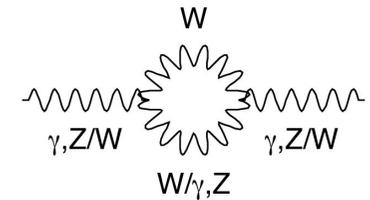
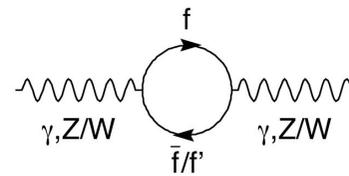
Recent history

- Pre-LEP
 - Hardronic R-ratio
 - Gluonic jets
- LEP I
 - Z-line shape
- LEP II
 - W threshold



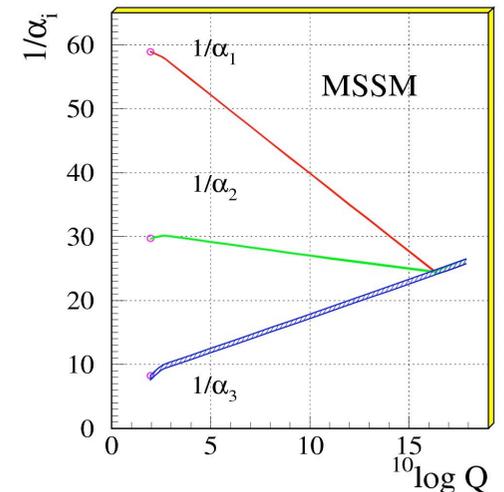
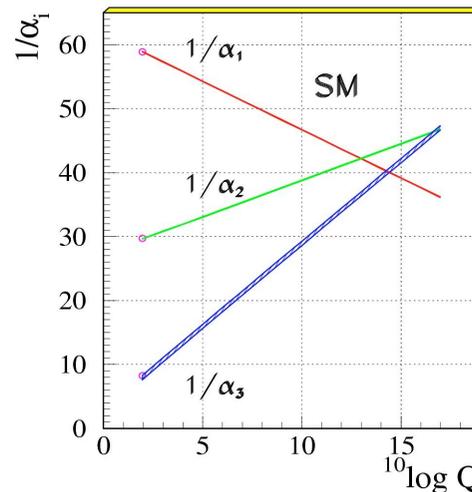
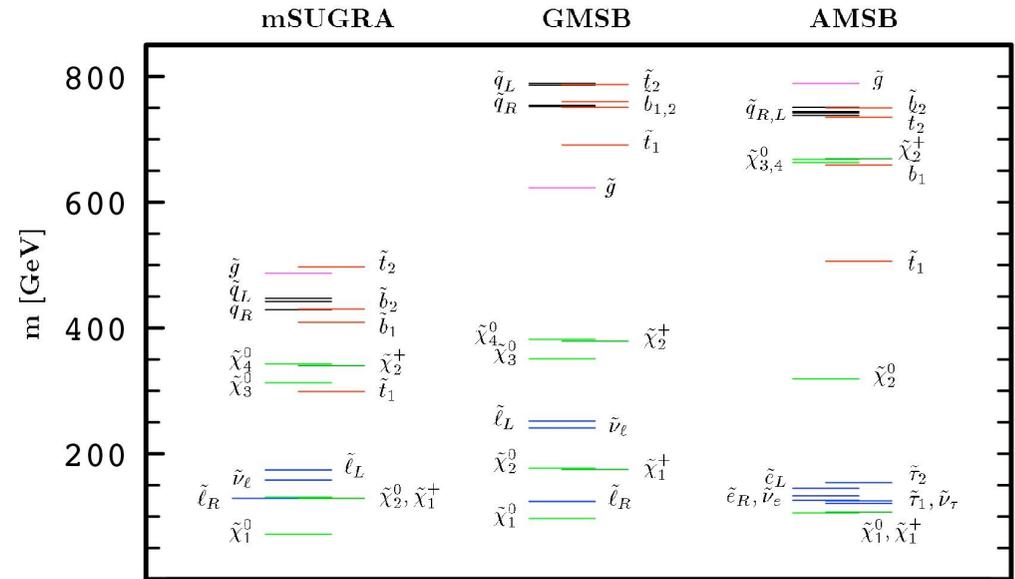
Electro-weak observables

- Higgs not yet observed
- Precision measurements of the electroweak physics contains a great deal of information
- Loop corrections to observables
- Precision electron-positron collisions



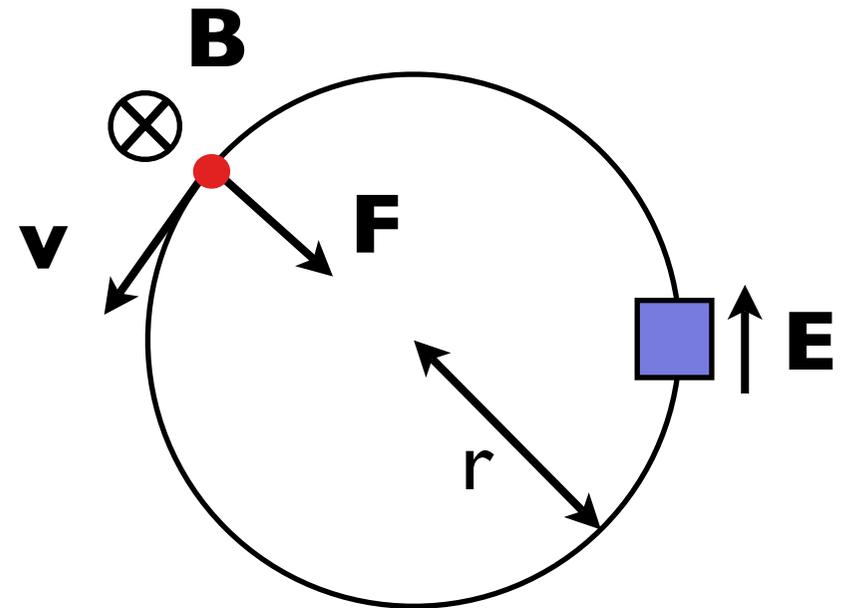
Energy frontier

- Why push to higher and higher energies?
- Standard model is incomplete even with the discovery of Higgs
- Supersymmetry?
- More exotic models
 - Large extra dimensions
 - etc etc...



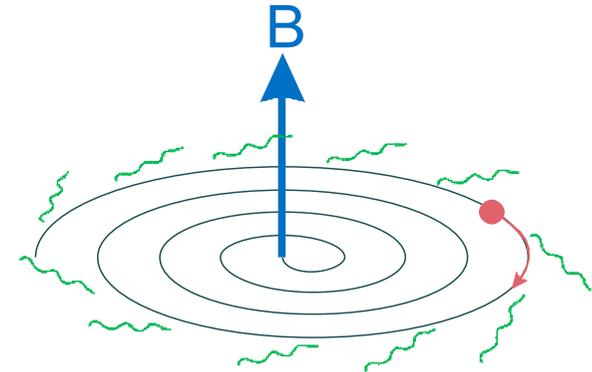
Synchrotrons

- Work horse of modern particle physics
- Efficient
- Multiple interaction points
- Accelerating systems used of each revolution of the accelerator
- Requires magnetic bending



Limits on synchrotrons

- Why not just build a bigger LEP?
- Power loss due to synchrotron radiation
- Energy must be replaced by accelerator
- Higher energies also require higher luminosities



$$P = \frac{1}{4\pi\epsilon_0} \frac{e^2 v^4}{c^3 \rho^2} \gamma^4$$

Electron machine

$$W = 8.85 \times 10^{-5} E^4 / \rho$$

MeV/turn

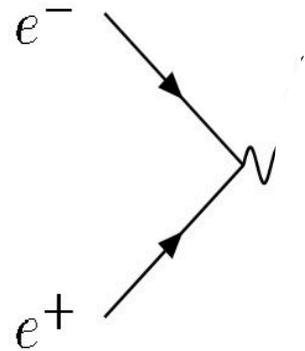
GeV

km

Cross sections (I)

- Standard model course
 - Define the initial state and calculate matrix element then cross section
- More problematic for hadron colliders where the colliding beams are composite objects
- Parton density functions

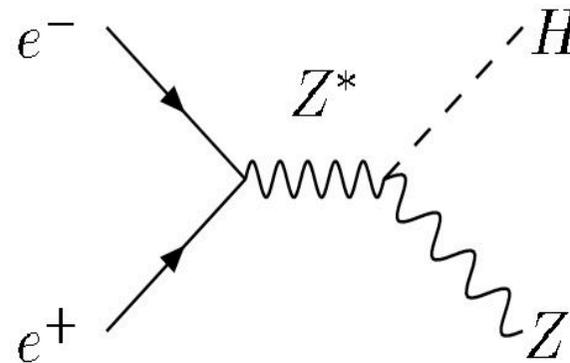
Initial state
Species, energy, helicity



Cross sections (I)

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Initial state
Species, energy, helicity



Cross sections (II)

- Consider SM cross sections
- In order to probe scales where we need higher energies
- Higher energies require correspondingly higher luminosity

Cross section

$$\sigma \sim \lambda^2$$

Wavelength

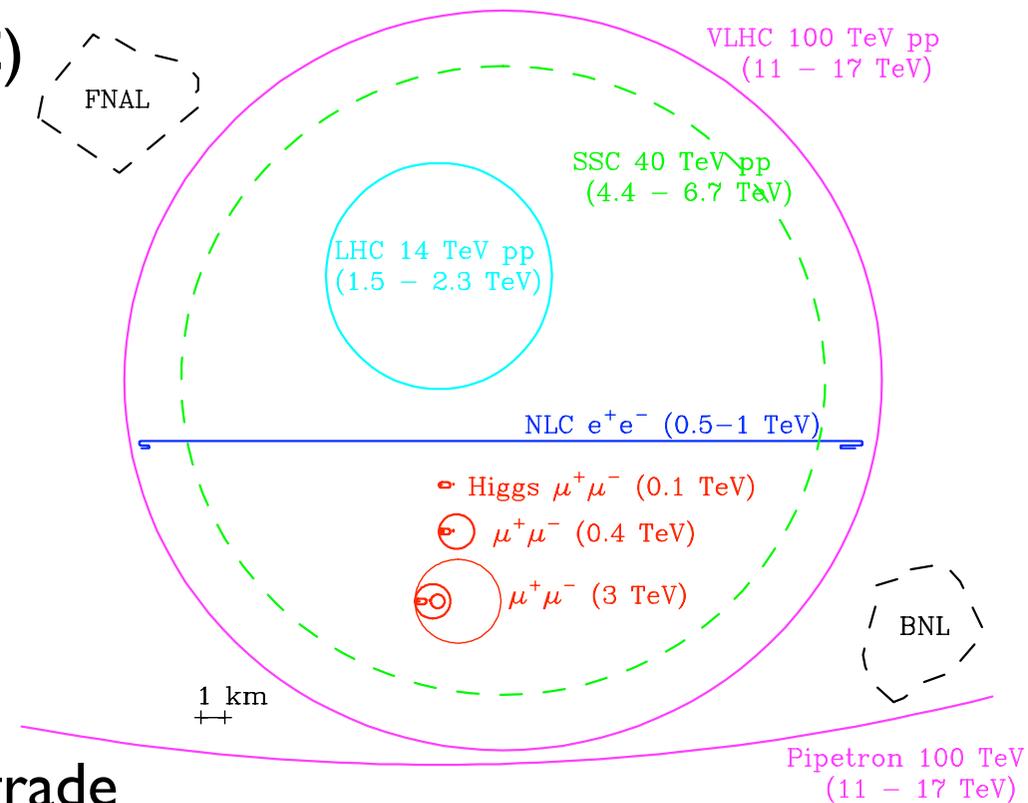
$$E \sim \frac{h}{\lambda}$$

Point-like cross section must scale as

$$\sigma \sim \frac{1}{E^2}$$

Planned facilities

- Linear Collider
 - International Linear Collider (ILC)
 - Compact Linear Collider (CLIC)
- Muon accelerators
 - Muon colliders
 - Neutrino factories
- Hadron colliders
 - Large Hadron collider and its upgrade
 - Very Large Hadron Collider (VLHC)



Designing a machine

- Particle species
 - Electrons/positrons
 - Protons/anti-protons
 - Muons/anti-muons
- Beam energy
- Luminosity
- How does one produce anti-particles?
- Once produced how do you keep them?
- Once you have collided what do you do with the spent beams (ILC), Dumps
- Accelerator and detector protection (LHC)

Luminosity equations

- What luminosity is required for measurement?
- Require some knowledge of the cross section
- Integrated luminosity depends on many factors
 - Beam lifetimes

Assuming head on collisions and equal beam sizes

$$\mathcal{L} = f \frac{N_1 N_2}{4\pi\sigma_x\sigma_y}$$

Rewriting in terms of emittance and beta functions

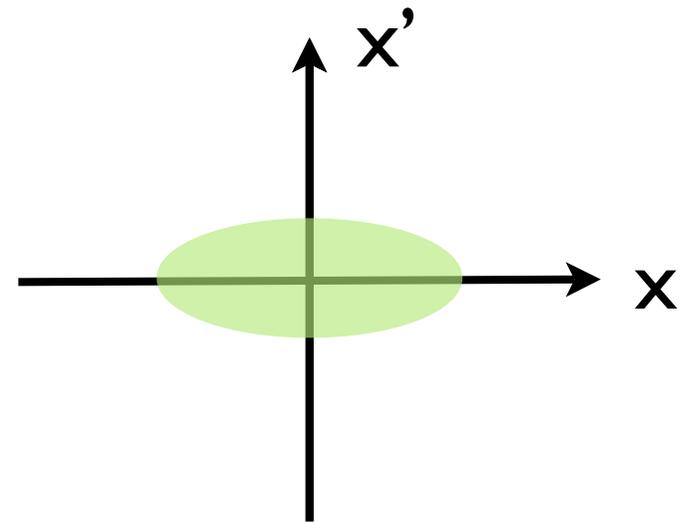
$$\mathcal{L} = f \frac{N_1 N_2}{4\sqrt{\epsilon_x\beta_x^*\epsilon_y\beta_y^*}}$$

Accelerator aside : Emittance

- Accelerator physics in three slides!
- Emittance is a measure of the spatial properties of a particle beam
- Essentially the product of the spatial width with the angular width
- Normalised emittance invariant

position angle

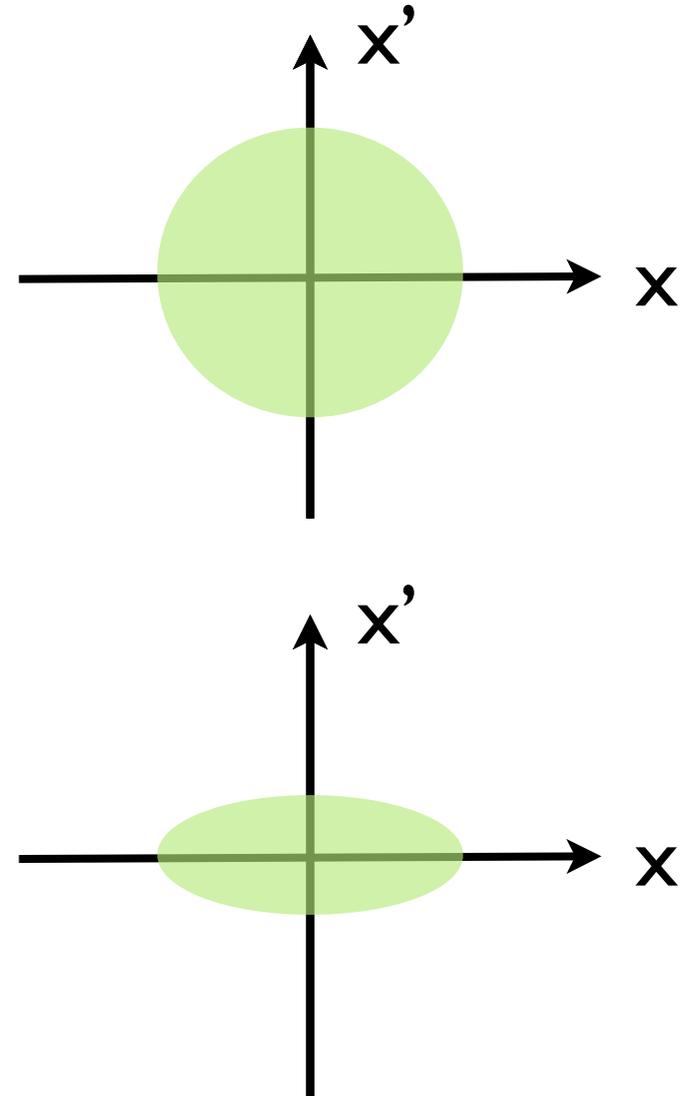
$$\epsilon^2 = \langle x^2 \rangle \langle x'^2 \rangle - \langle xx' \rangle^2$$



$$\epsilon_N \equiv \epsilon \times \left(\gamma \frac{v}{v} \right)$$

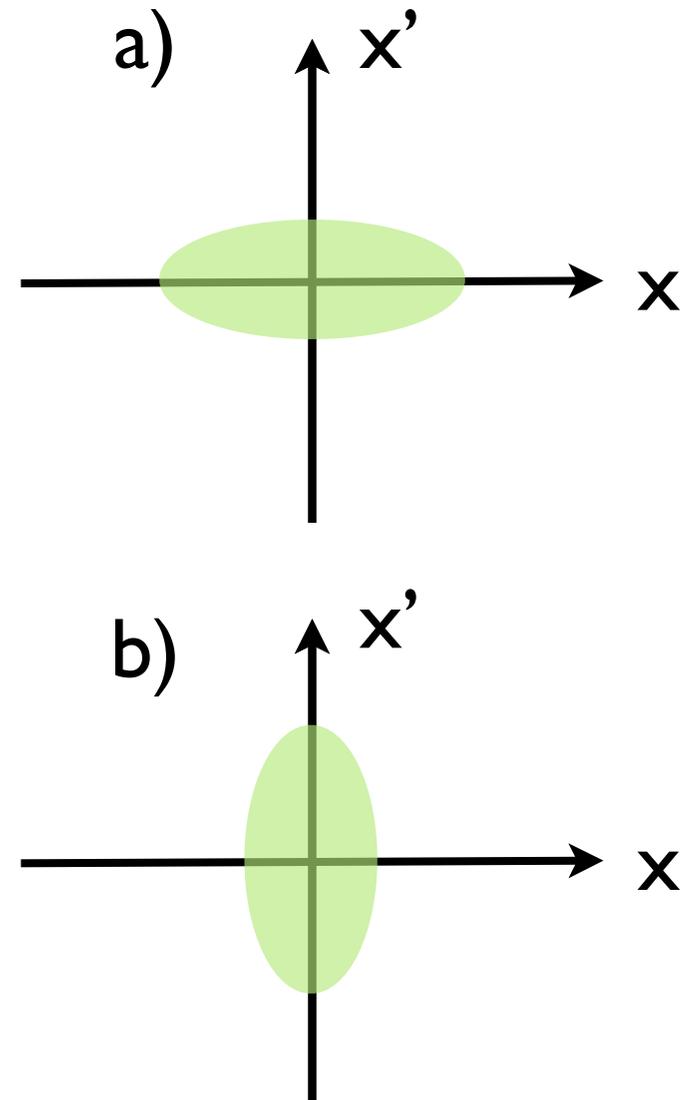
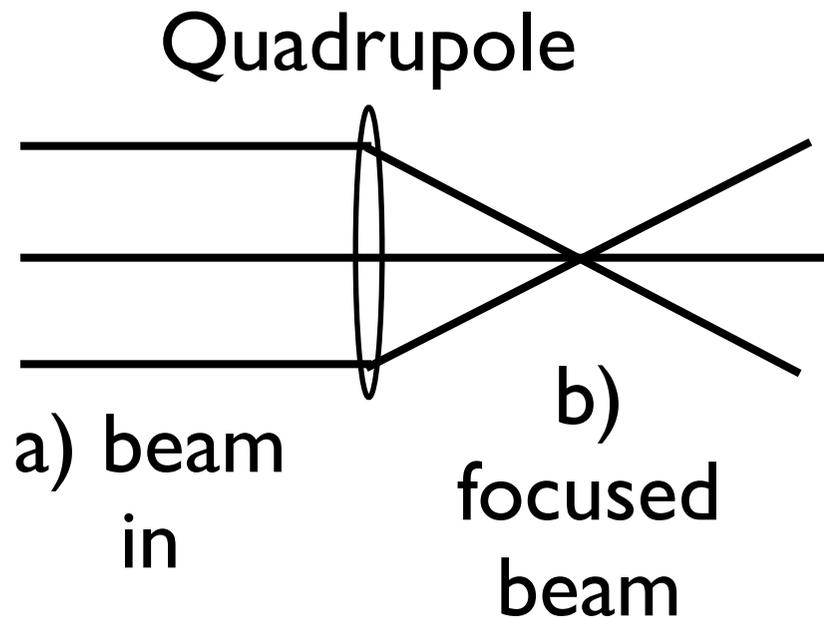
Acceleration

- Accelerating cavities are used to increase the energy of the beam
- The transverse momentum of the particles is not changed but it is increased in the direction of motion
- x' is reduced



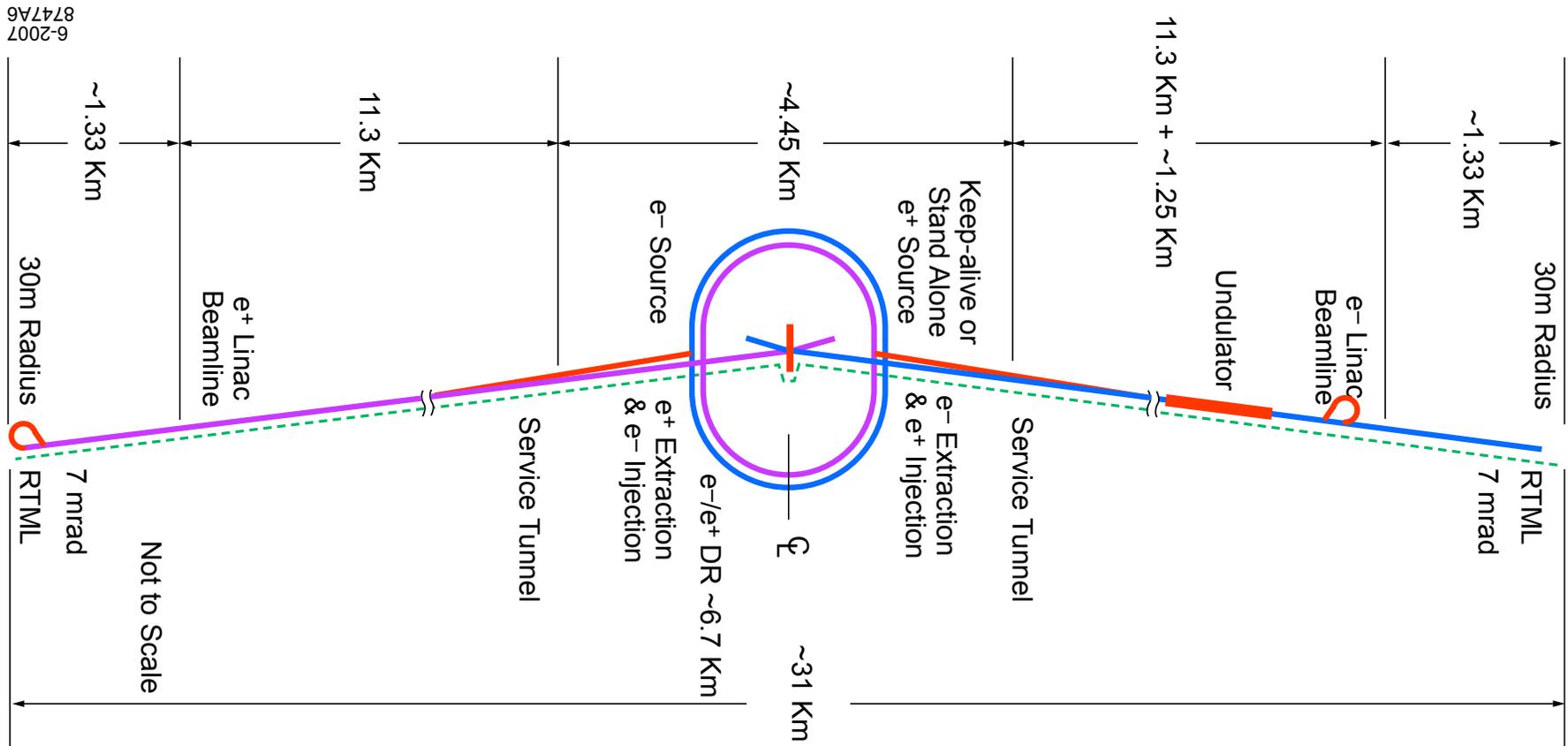
Focusing

- Quadrupole magnets act as lenses
- Focusing in one axis and defocusing in the other



International linear collider ILC

- ILC designed to be a high luminosity e^+e^- collider initially up to 500 GeV then upgradable to 1 TeV
- Major systems all driven by the requirement for luminosity



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International Linear Collider

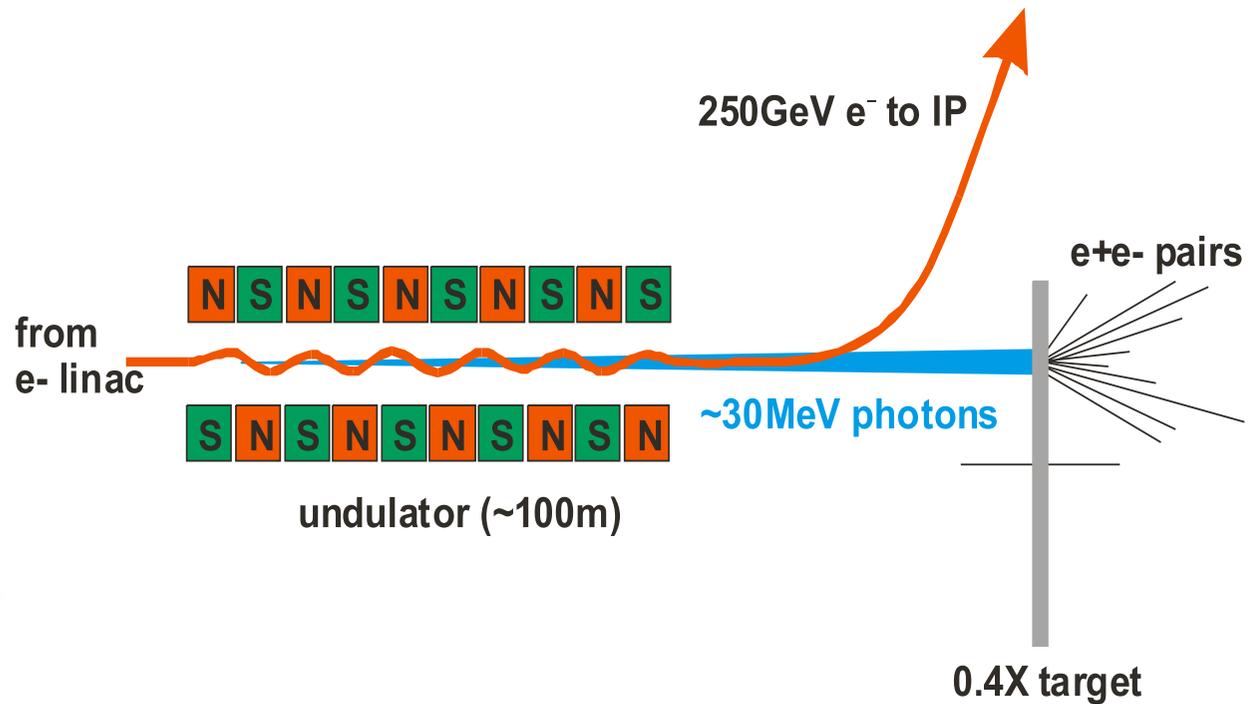
- LEP final energy ~200 GeV
- Note the vertical beam size required
- Not continuous bunches but bunch trains of 2820 bunches at 5 Hz
- Low emittance beams required
- High beam powers

Parameter	Value
Beam energy	250 to 500 GeV
Bunch density	$2 \times 10^{10} e^-$
Number of bunches	2820
Bunch spacing	300 ns
Repetition frequency	5 Hz
Beam size y (x)	3.5 (554) nm
Luminosity	$2.82 \cdot 10^{38} m^{-2}s^{-1}$

Positron production

$$\mathcal{L} = f \frac{N_1 N_2}{4 \sqrt{\epsilon_x \beta_x^* \epsilon_y \beta_y^*}}$$

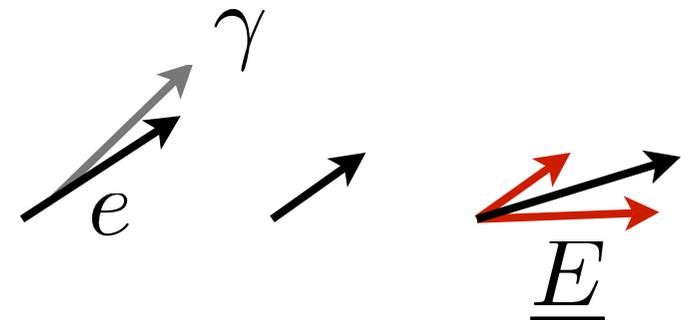
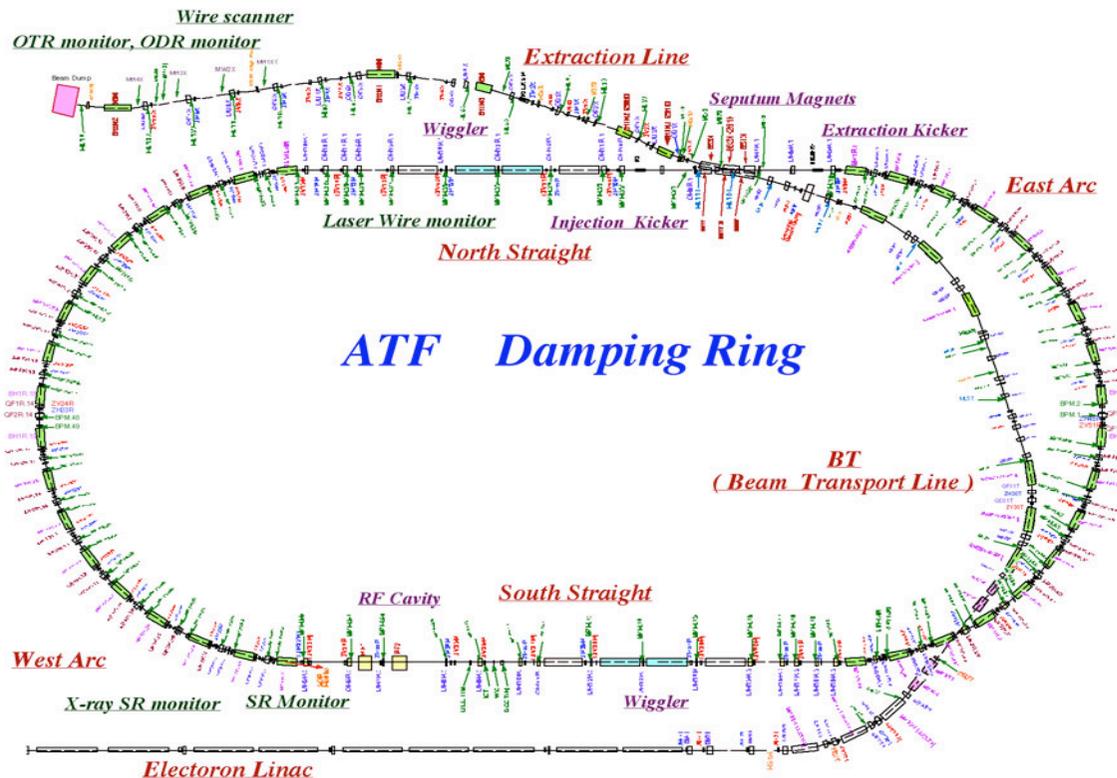
- Positron production at the ILC will use the high energy electron beam
- Pass electron beam through undulator
- 30 MeV photons
- Thin target generate electron positron pairs



Damping of the electron beam

$$\mathcal{L} = f \frac{N_1 N_2}{4 \sqrt{\epsilon_x \beta_x^* \epsilon_y \beta_y^*}}$$

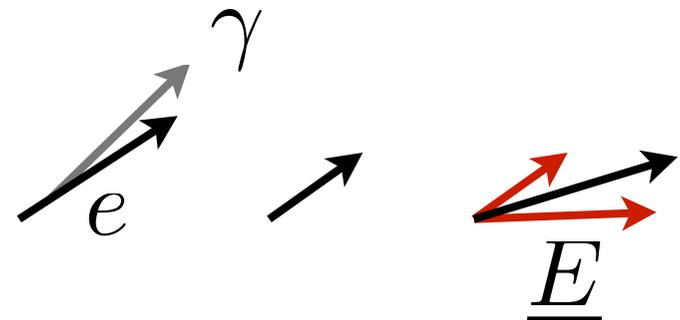
- Ring in which beam is stored for 20 to 200 ms
- To reduce the beam emittance
- Radiation energy loss
- Longitudinal momentum replaced by accelerator



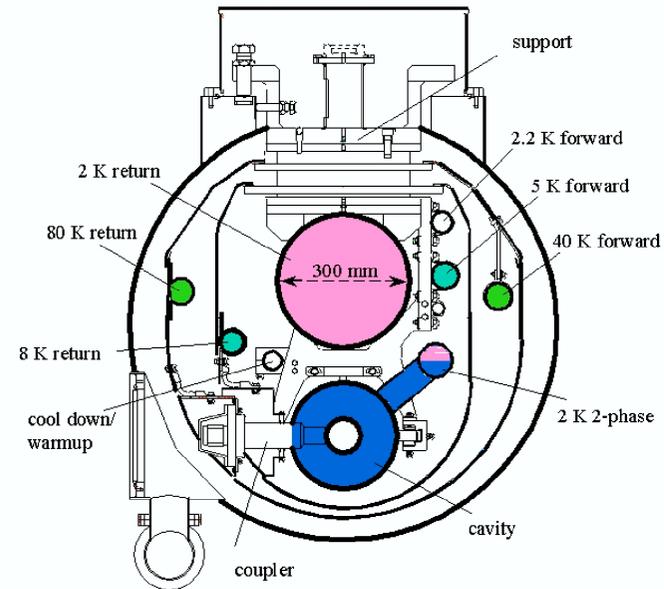
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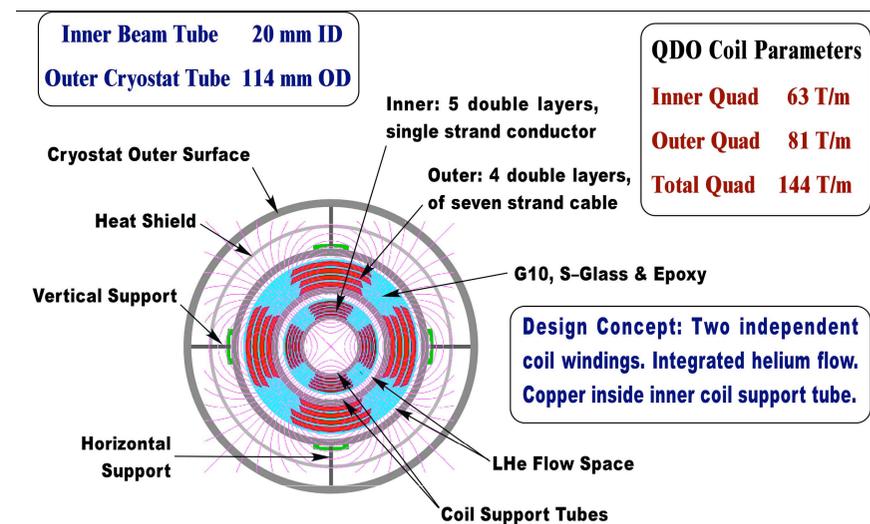
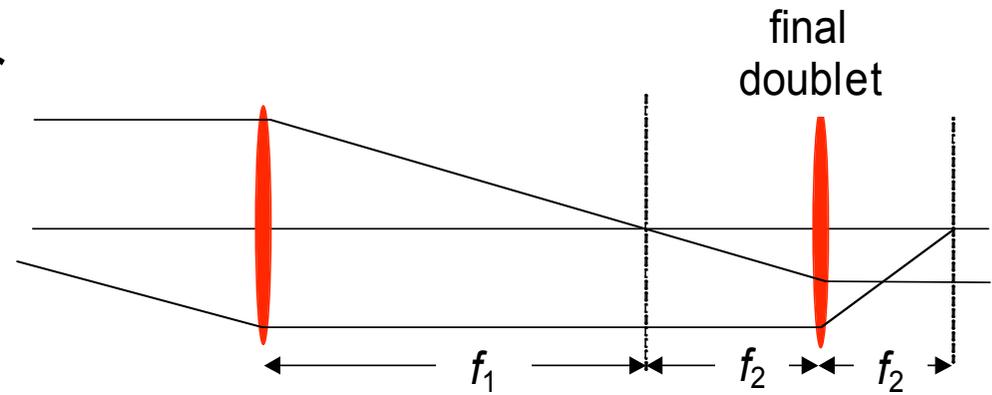
ILC acceleration



- Pure Niobium cavities
 - 1.2 GHz radio frequency
 - Super conducting at LHe temperatures
 - Require ~ 35 MeV/m accelerating gradient

Final focus system

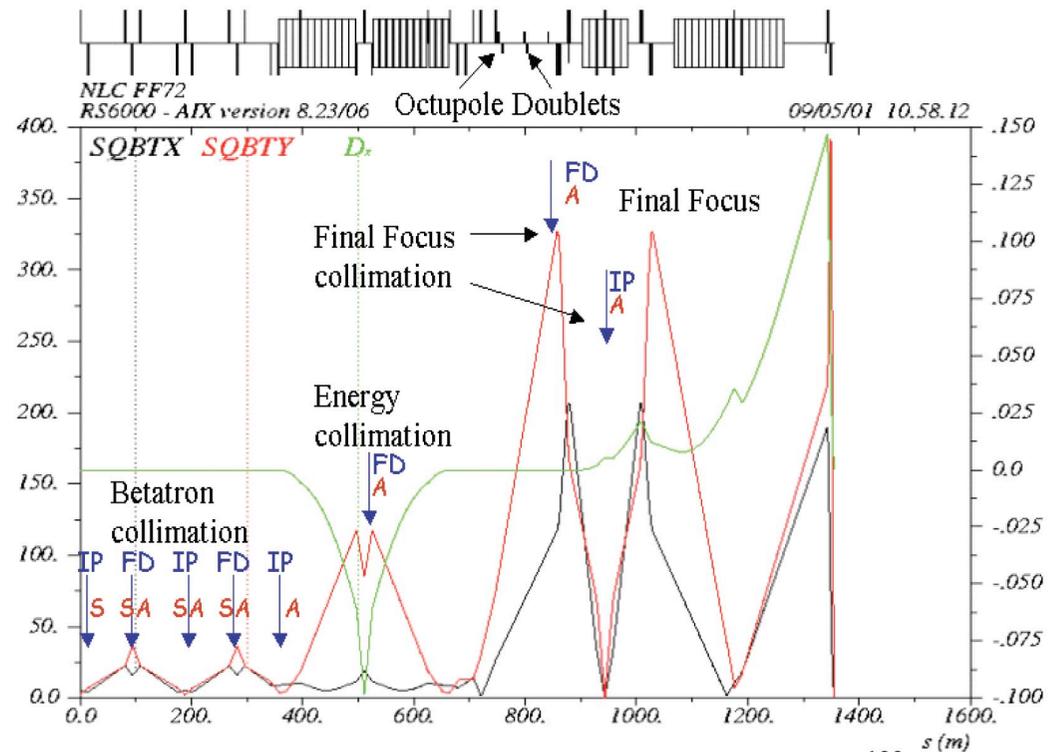
- Use telescope to demagnify beam by factor ~ 300
- $M = f_1/f_2 = f_1/L^*$
- Set $L^* = 2$ m then $f_1 = 600$ m
- Require large magnetic field for final magnet
- Small L^* , magnets inside detector



Beam delivery system

- Beam diagnostics
- Emittance (transverse and longitudinal)
- Energy
- Collimation
- Final focus
- Corrections
- Chromatic/geometric

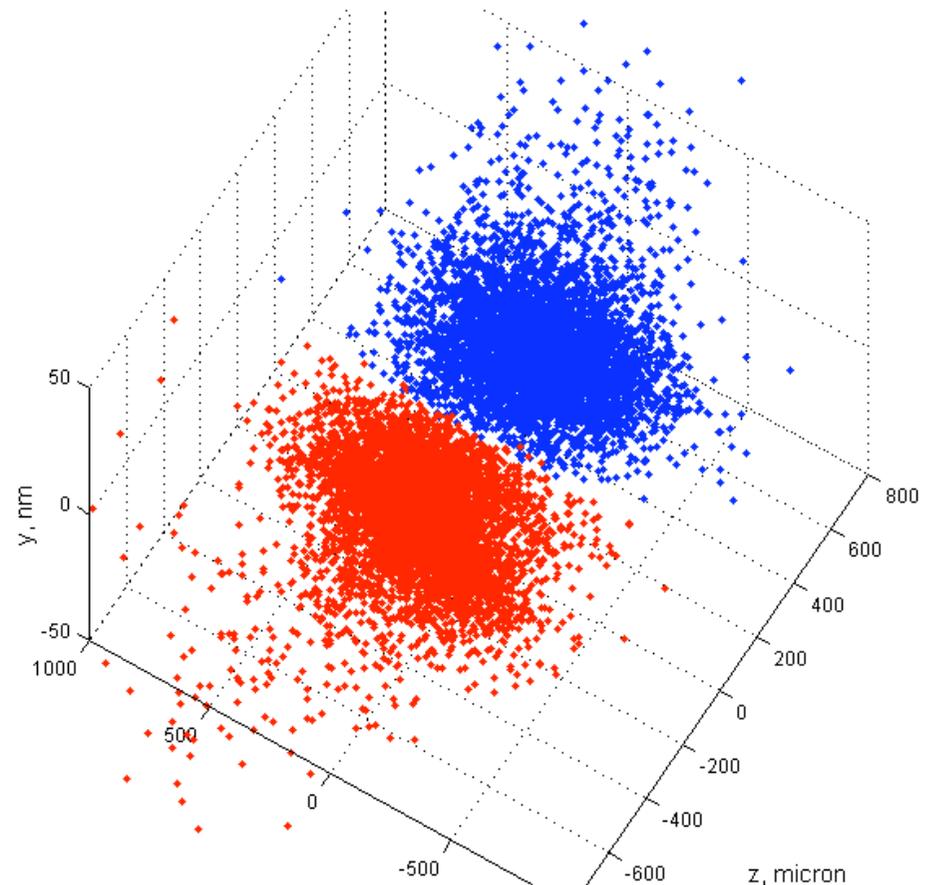
$$\mathcal{L} = f \frac{N_1 N_2}{4 \sqrt{\epsilon_x \beta_x^* \epsilon_y \beta_y^*}}$$



Beam-beam interaction

- 5 nm beam size causes some serious problems
 - Strong mutual bunch focusing
 - Radiation from strong opposing bunch fields (beamstrahlung)
 - Pair production, interaction of the radiation with field (pairs)

$$\mathcal{L} = N_b f \frac{N_1 N_2}{4\pi\sigma_x\sigma_y} H_D$$



Luminosity equations

- Can rewrite luminosity equation in many different ways
- Consider the total beam power
- What is the total beam power given ILC parameters?

Recall equation for
luminosity

$$\mathcal{L} = N_b f \frac{N_1 N_2}{4\pi\sigma_x\sigma_y} H_D$$

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Recall equation for luminosity

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$$\begin{aligned} P_{beam} &= f E N_b N_1 \\ &= \eta P_{grid} \end{aligned}$$

Luminosity equations

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Recall equation for luminosity

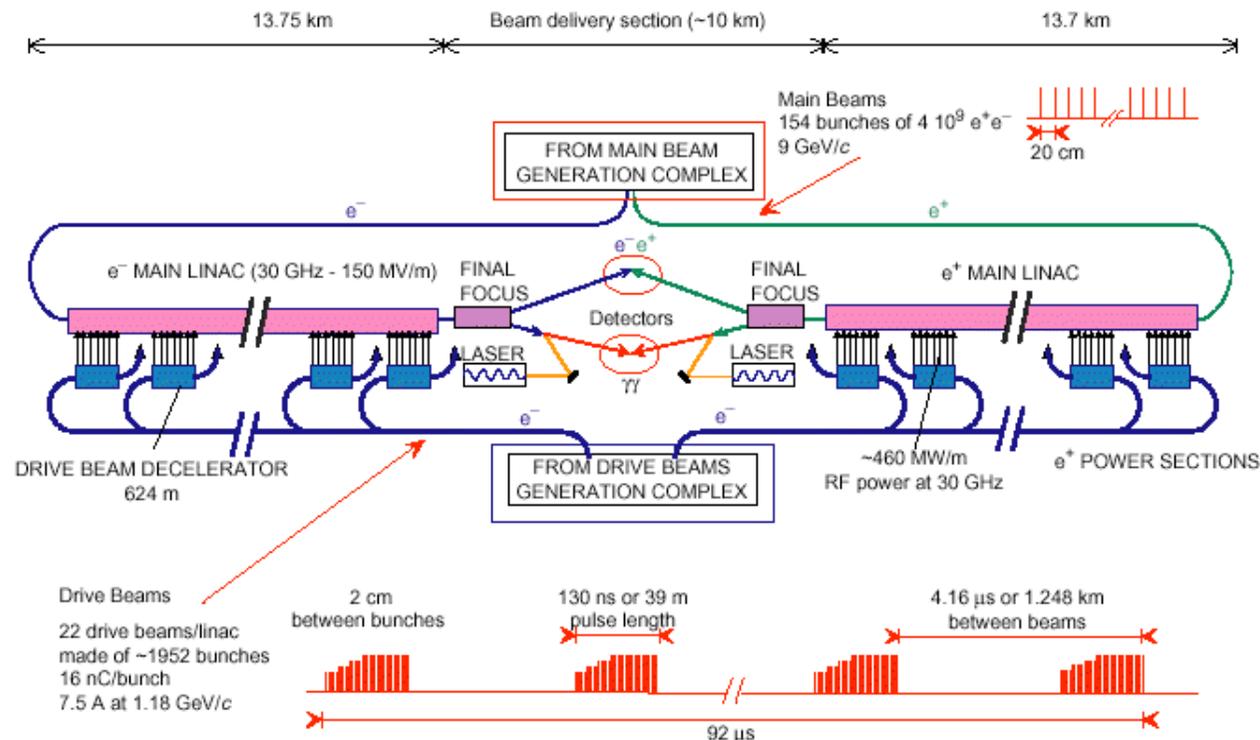
$$\mathcal{L} = N_b f \frac{N_1 N_2}{4\pi\sigma_x\sigma_y} H_D$$

$$\begin{aligned} P_{beam} &= f E N_b N_1 \\ &= \eta P_{grid} \end{aligned}$$

$$\mathcal{L} = \frac{N}{4\pi\sigma_x\sigma_y} H_D \frac{\eta P_{grid}}{E_{CM}}$$

Compact Linear Collider (CLIC)

- Further into the future and higher energies 2-5 TeV
- Power conversion efficiency
- Use high current low energy beam (drive beam) to generate RF power for probe beam



Linear collider

- Linear collider is a challenging machine
- Large momentum developed internationally to see the machine built
- Cost is a important issue \$\$\$
- Damping rings, accelerator and beam delivery system all push current technologies to the limits
 - 20 km of superconductor fed with high power radio-frequency power, with MW of beam power traveling down the middle.
 - Precision Higgs and top physics.
- Low mass supersymmetry

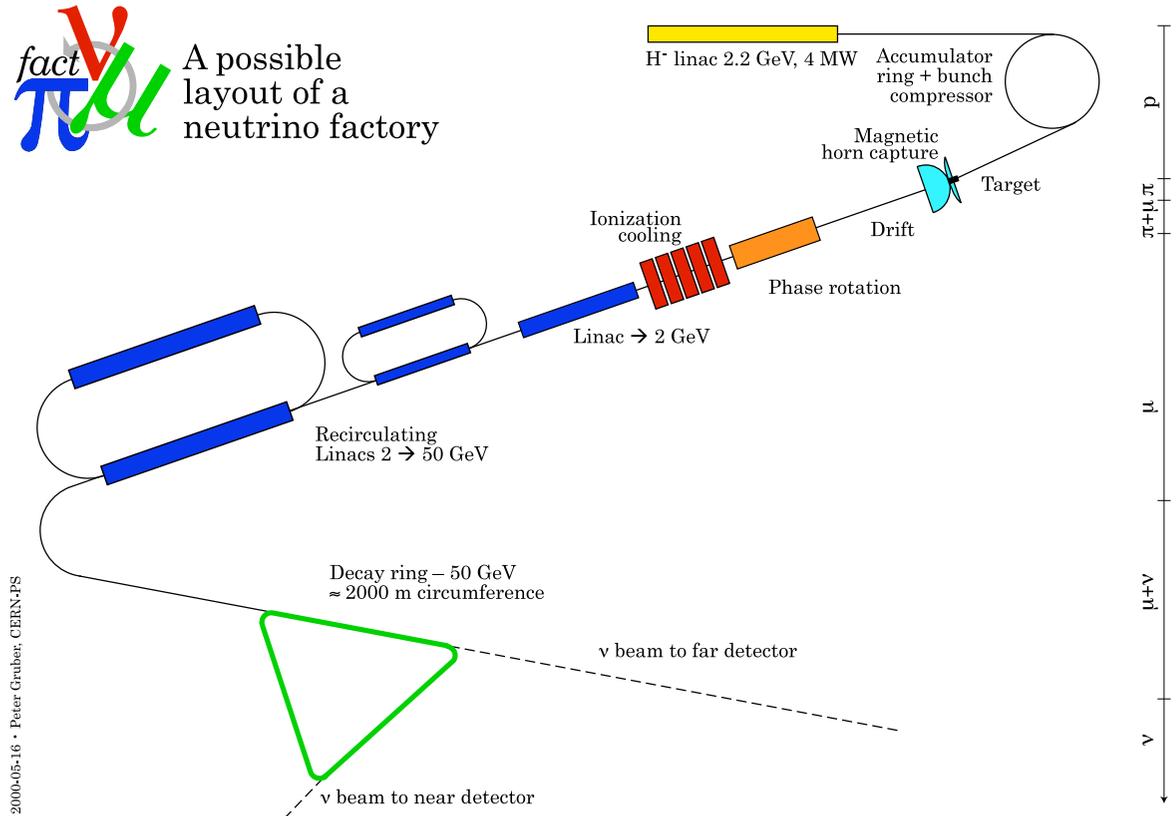
Muon storage and acceleration

- Muon significantly more massive than electron

$$m_{\mu} \approx 207m_e$$

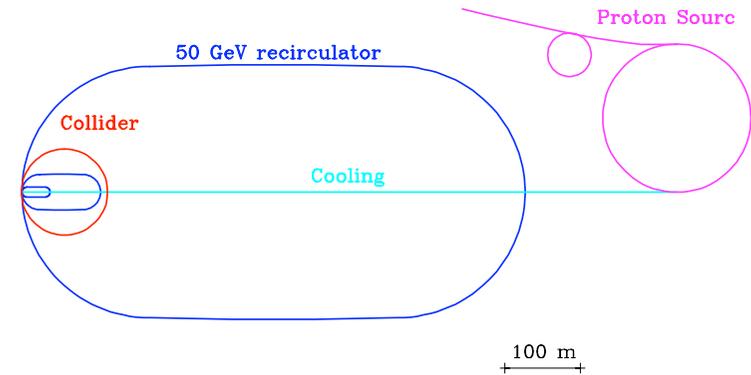
$$P = \frac{1}{4\pi\epsilon_0} \frac{e^2 v^4}{c^3 \rho^2} \gamma^4$$

- SR losses low
- Production and capture difficult
- Cooling (lowering emittance)
- Quick acceleration before decay

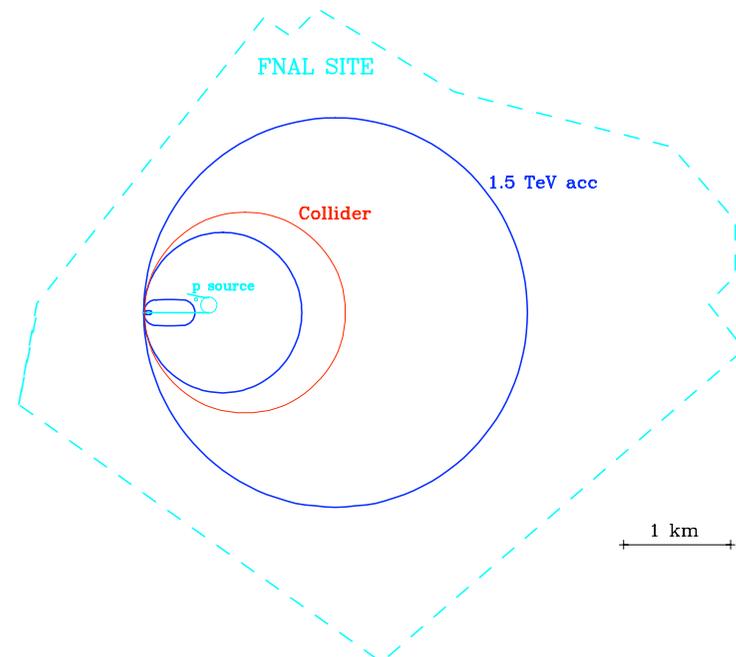


Muon collider

- Muon collider is highly challenging
- Possible to achieve required luminosity
- First stage is neutrino factory technology
- Main accelerator is not so challenging



Plan of a 0.1 TeV COM muon collider.

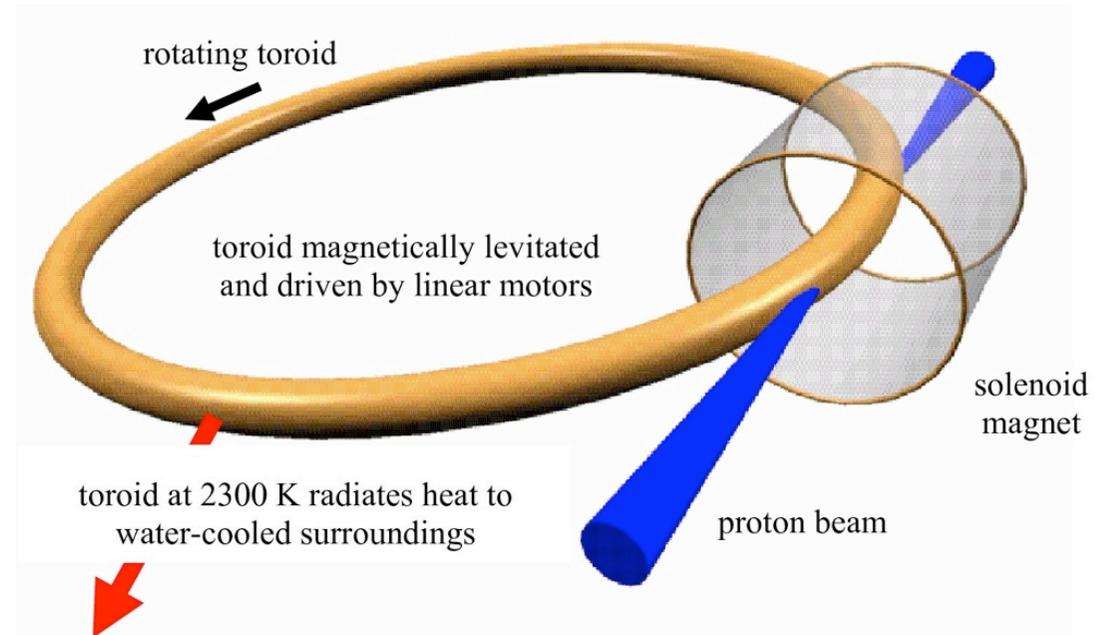


Plan of a 3 TeV COM muon collider shown on the Fermi National Laboratory site as an example.

Muon production

- Muons created from pion decay
- Pions from proton-solid target collisions
- Problems are numerous
 - Heat dissipation
 - Radiation damage
 - Thermal stress, shock and fatigue

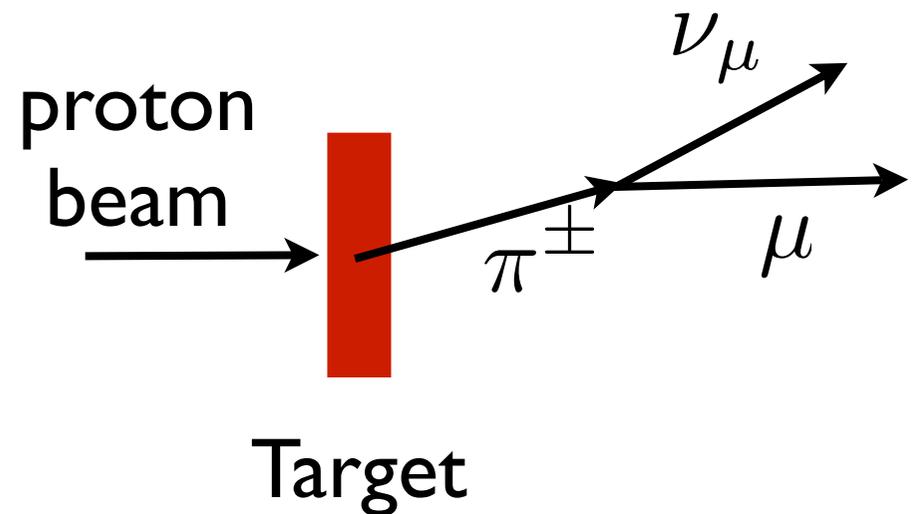
$$\mathcal{L} = f \frac{N_1 N_2}{4 \sqrt{\epsilon_x \beta_x^* \epsilon_y \beta_y^*}}$$



One target idea rotating metal ring

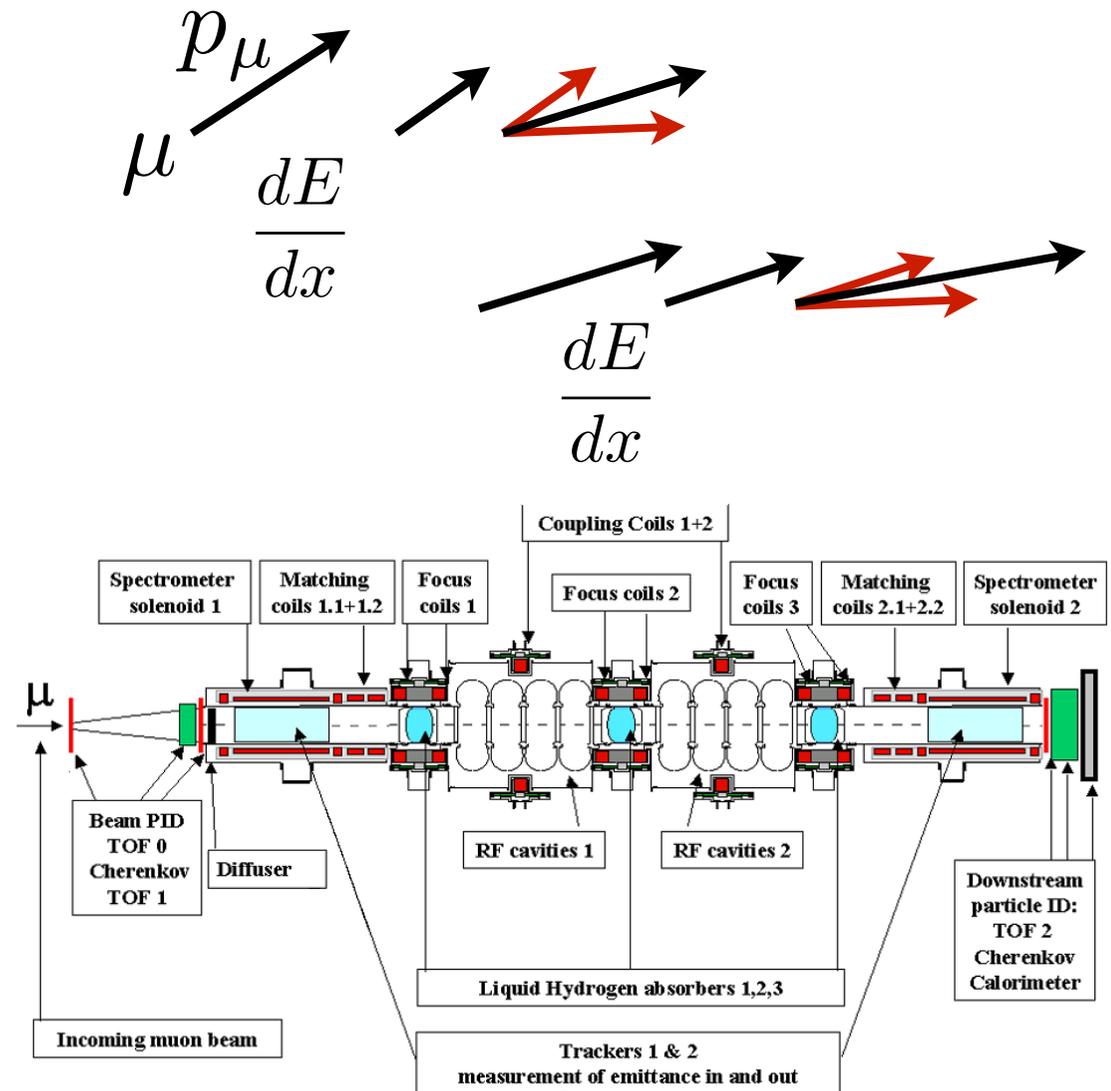
Muon production

- Generate charged pions from proton interaction with target
- Allow pions to decay into muons
- Angular and momentum distribution of pions and decay products



Ionization cooling

- Reduction of emittance
- Radiation cooling impossible
- Reduce momentum of muons, accelerate in one direction
- Energy loss in material
- Low mass target - Liquid hydrogen

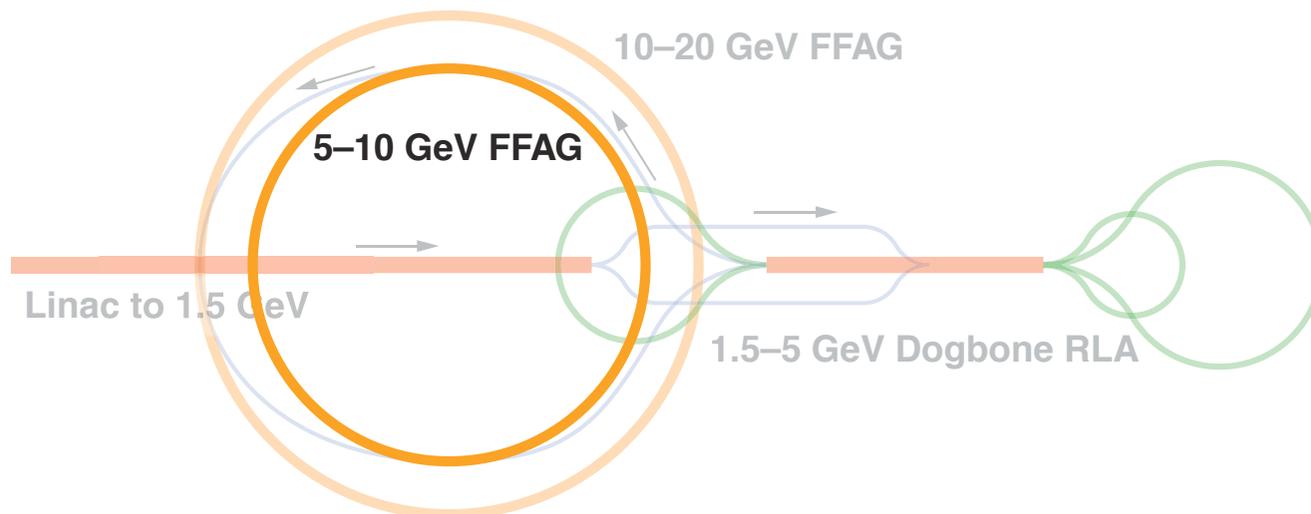


Muon acceleration

- Muon lifetime
 - Proper lifetime 2.2 micro-seconds
 - Time dilation to stop decay in laboratory frame

$$t = \gamma \tau$$

- Quickly accelerate to prevent decay, 10s of turns in each accelerator



Muon collider

- A muon collider is a very challenging accelerator to design and build
- Neutrino factory might be a more realistic, whilst doing effective R&D towards a collider
- As with the ILC low emittance and beta functions are required to obtain the luminosity
- Problems are mainly at the front end, high power proton driver, proton target, capture of muons, cooling and acceleration
- Still a long way off decades
 - Neutrino factory might be sooner ~decade

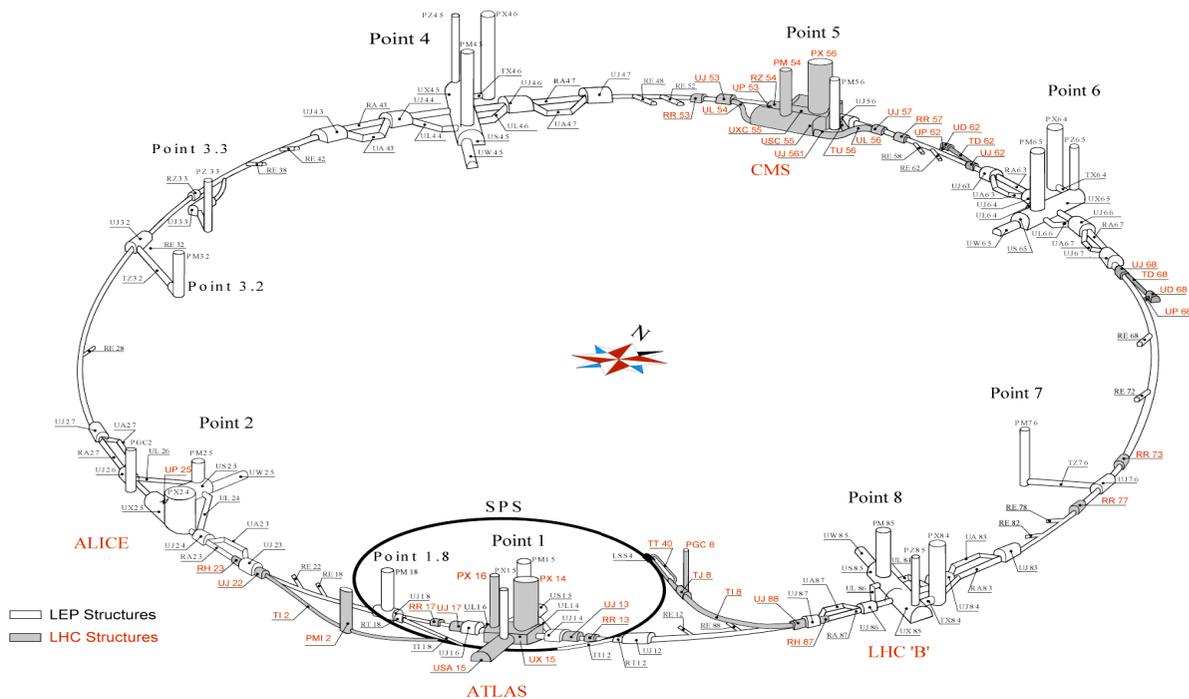
Large hadron collider



- LHC is the premier facility for the next decade
- Proton-**proton** synchrotron
- 14 TeV COM collision energy
- 27 km tunnel
- Luminosity upgrade potential?

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		Injection	Collision
Beam Data			
Proton energy	[GeV]	450	7000
Relativistic gamma		479.6	7461
Number of particles per bunch		1.15×10^{11}	
Number of bunches		2808	
Longitudinal emittance (4σ)	[eVs]	1.0	2.5 ^a
Transverse normalized emittance	[$\mu\text{m rad}$]	3.5 ^b	3.75
Circulating beam current	[A]	0.582	
Stored energy per beam	[MJ]	23.3	362
Peak Luminosity Related Data			
RMS bunch length ^c	cm	11.24	7.55
RMS beam size at the IP1 and IP5 ^d	μm	375.2	16.7
RMS beam size at the IP2 and IP8 ^e	μm	279.6	70.9
Geometric luminosity reduction factor F ^f		-	0.836
Peak luminosity in IP1 and IP5	[$\text{cm}^{-2}\text{sec}^{-1}$]	-	1.0×10^{34}
Peak luminosity per bunch crossing in IP1 and IP5	[$\text{cm}^{-2}\text{sec}^{-1}$]	-	3.56×10^{30}

LHC Upgrade

$$L = \frac{N_b^2 n_b f_{rev} \gamma_r}{4\pi \epsilon_n \beta^*} F$$

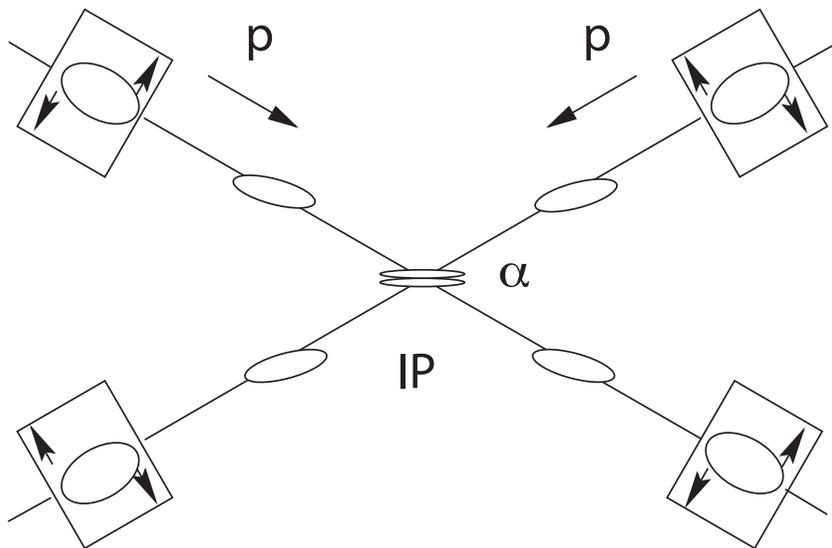
$$F = 1 / \sqrt{1 + \left(\frac{\theta_c \sigma_z}{2\sigma^*} \right)^2}$$

- Reduce beta functions at the IP
- Emittance?
- There is a crossing angle
 - Reduces total luminosity
 - Crab beam crossing

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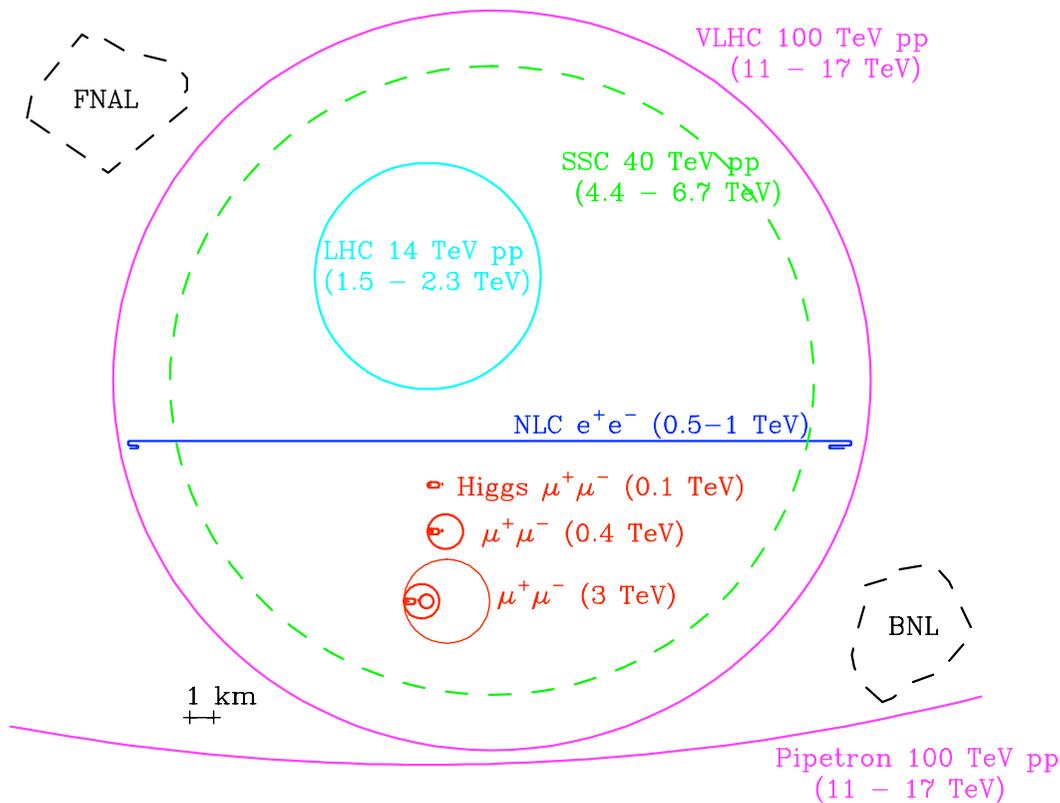
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Very Large Hadron Colliders

- Larger radius LHC
- Significant SR from proton beam
- Civil engineering
- Cheaper tunneling required
- Heating (quenching) of dipole magnets



Very Large Hadron Colliders

Table 1.1. The high-level parameters of both stages of the VLHC.

	Stage 1	Stage 2
Total Circumference (km)	233	233
Center-of-Mass Energy (TeV)	40	175
Number of interaction regions	2	2
Peak luminosity ($\text{cm}^{-2}\text{s}^{-1}$)	1×10^{34}	2.0×10^{34}
Luminosity lifetime (hrs)	24	8
Injection energy (TeV)	0.9	10.0
Dipole field at collision energy (T)	2	9.8
Average arc bend radius (km)	35.0	35.0
Initial number of protons per bunch	2.6×10^{10}	7.5×10^9
Bunch spacing (ns)	18.8	18.8
β^* at collision (m)	0.3	0.71
Free space in the interaction region (m)	± 20	± 30
Inelastic cross section (mb)	100	130
Interactions per bunch crossing at L_{peak}	21	54
Synchrotron radiation power per meter (W/m/beam)	0.03	4.7
Average power use (MW) for collider ring	25	100
Total installed power (MW) for collider ring	35	250

US-VLHC study group

- First phase start at 15 to 40 TeV
- Injection from Tevatron at 900 GeV
- Second phase 85 TeV injection from phase I
- Up to 200 TeV machine
- Proton SR damping
- Can the world afford

Summary

- Discussed new facilities
 - Linear collider (CLIC)
 - Muon factories and colliders
 - Large hadron collider and possible upgrades
 - Very large hadron collider
- Increasing difficult to build these facilities
 - Cost
 - Technical challenges
 - Time scales decades (fortunately you are young)

Resources for further study

- <http://www.linearcollider.org/cms/>
- <http://clic-study.web.cern.ch/clic%2Dstudy/>
- <http://www.cap.bnl.gov/mumu/>
- <http://lhc.web.cern.ch/lhc/>
- <http://vlhc.org/>
- <http://pdg.lbl.gov/>