Brunel University Queen Mary, University of London Royal Holloway, University of London University College London

## Intercollegiate post-graduate course in High Energy Physics

## Paper 2: Current HEP Projects

Friday, 6 February 2009

Time allowed for Examination: 3 hours

### Answer **ALL** questions

Books and notes may be consulted

The paper is split into the following sections each carrying 15 marks:

- 1. Neutrino physics
- 2. CP violation
- 3. Hadron Colliders
- 4. LHC physics
- 5. QCD phenomenology
- 6. Introduction to machine physics

Please answer different sections in different answer books as they will be marked by different people.

#### Section 1: Neutrino physics

#### Question 1

The Opera experiment has recently presented its first results from a short period of data-taking on the CERN to Gran Sasso neutrino beamline: out of 38 observed neutrino interactions, 29 have been classified as  $\nu_{\mu}$  CC events and 9 as NC events; no  $\nu_{\tau}$  CC event was observed. The detector target mass for this period corresponded to 0.5 kton.

(a) Briefly describe the purpose of experiment and its sensitivity.

(b) Draw the Feynman diagram of the  $\nu_{\tau}$  events that are searched for. What is the characteristic signature of this kind of interaction in the Opera detector target?

(c) Given the expected numbers of: 2900  $\nu_{\mu}$  CC/kton/year and 2  $\nu_{\tau}$  CC/kton/year (for  $\Delta m^2 = 2.5 \times 10^{-3}$  at maximal mixing), which values of  $\Delta m^2$  can be excluded by the first Opera results? (**HINT**: use the expected number of events to infer a ratio of cross-sections times detection efficiencies)

[7 marks]

#### Question 2

(a) Explain how CP violation (CPV) can arise in the lepton sector. How many neutrino families are needed for CPV to manifest in neutrino oscillations? Which parameter(s) of the MNS matrix should be different from zero for its observation? Could an experiment observe a CPV effect if all neutrinos had identical mass? Justify all your answers.

(b) What are the experimental evidences that there are at least three different mass eigenstates?

(c) Describe briefly one of the experiments under construction which can measure or improve the limit on the mixing angle  $\theta_{13}$  (detectors, beam/baseline main parameters, sensitivity). Which CPV effect can it look for (if any)?

[8 marks][Total Marks = 15]

#### Section 2: CP violation

#### Question 1

Describe the significance of Kobayashi and Maskawa's work that led to them being awarded half of the 2008 Nobel Prize for physics. Also note how this differs from the quark-mixing model proposed by Cabibbo.

[5 marks]

#### Question 2

What are the Sakharov conditions, and what is their physical consequence?

[3 marks]

#### Question 3

The decay  $B^0 \to J/\psi K^0$  can be used to measure  $\sin 2\beta$ . Draw the tree Feynman diagram for this decay. Which diagram does this decay pick up a factor of  $V_{\rm td}$  from in order for it to be sensitive to  $\sin(2\beta)$ ? (**HINT:** The quark content of  $J/\psi$  is  $c\overline{c}$ ). Note CKM matrix elements on vertices where appropriate.

> [7 marks][Total Marks = 15]

#### Section 3: Hadron Colliders

#### Question 1

# Draw the two Feynman diagrams which illustrate why precision measurements of the W boson and top-quark mass can be used to place a limit on the Higgs mass. What is the present experimental lower bound on the Higgs mass? What is the approximate upper limit (at 95% CL) implied by the W, top-quark mass and other precision electroweak measurements?

[4 marks]

#### Question 2

Draw the rapidity distribution of Z bosons produced at the Tevatron. Explain why the distribution has the shape it does. Explain how the distribution is expected to change at the LHC (at nominal beam energy) for the same integrated luminosity and approximately what is the maximum rapidity at which Z bosons can be produced at the LHC?

[7 marks]

#### Question 3

Considering the production of a Higgs boson ( $m_H = 120 \text{ GeV}$ ) in association with a Z boson at the Tevatron. Show that the energy of the Higgs ( $E_H$ ) is given by:

$$E_H = \frac{x^2 s + m_H^2 - m_Z^2}{2x\sqrt{s}},$$

where  $m_Z$  is the mass of the Z boson,  $m_H$  is the mass of the Higgs boson,  $\sqrt{s}$  is the Tevatron's centre of mass energy and both the interacting partons carry the same momentum fraction, x, of the proton and anti-proton's 4-momenta.

> [4 marks][Total Marks = 15]

#### Section 4: LHC Physics

#### Question 1

## Define *R*-parity $(R_p)$ . Which values does $R_p$ take for Standard Model and for SUSY particles, respectively? Discuss some of the consequences of $R_p$ conservation at the LHC, including how $R_p$ conserving SUSY models support the existence of a good Dark Matter candidate.

[4 marks]

#### Question 2

Draw a lowest order Feynman diagram for gluino pair production at the LHC.

[3 marks]

#### Question 3

What is a typical inclusive SUSY selection (both leptonic and non-leptonic) for  $R_p$ conserving SUSY decays at the LHC? Explain. (Consider the case where the sparticle
mass ordering is such that  $m_{\tilde{g}} > m_{\tilde{\chi}} > m_{\tilde{\chi}_2} > m_{\tilde{l}}$ ).

[5 marks]

#### Question 4

With the help of a Feynman diagram, discuss how real graviton emission in ADD models with extra spatial dimensions could "fake" a SUSY signature in the final state.

[3 marks][Total Marks = 15]

#### Section 5: QCD phenomenology

#### Question 1

Consider  $e^-e^+$  annihilation in the centre-of-mass frame with total energy  $\sqrt{s}$ . We produce a quark, antiquark and gluon with four-momenta  $p_1, p_2$  and  $p_3$  respectively. Defining  $x_i = 2E_i/\sqrt{s}$  (where *E* represents energy), using energy and momentum conservation show that

$$(1 - x_1) = 1/2x_2x_3(1 - \cos\theta_{\bar{q}g})$$

where  $\theta_{\bar{q}g}$  is the angle between the antiquark and gluon.

[4 marks]

The three jet cross-section diverges as  $x_1 \rightarrow 1$ . By reference to the above equation describe the cuts required to avoid this happening. Discuss how this matches our idea of the requirements for measuring a three jet event in practice.

[4 marks]

#### Question 2

The structure function  $F_2$  for neutral current scattering is given by

$$F_2(x) = x \sum_{i} e_i^2(q_i(x) + \bar{q}_i(x)),$$

where  $e_i$  is the electric charge weighting. Show that the integral

$$\int_0^1 dx \, (F_2^p(x) - F_2^n(x))/x,$$

where p represents proton and n neutron, is equal to 1/3 if  $\bar{u} = \bar{d}$ , and calculate the correction term if this is not the case. (Assume isospin symmetry, i.e. in going from proton to neutron swap up and down quarks and antiquarks).

[4 marks]

The experimental measurement is  $0.23 \pm 0.03$ . Suggest another experiment which would give more information on  $\bar{u}, \bar{d}$  differences.

[3 marks][Total Marks = 15]

#### Section 6: Introduction to machine physics

Parameter	Value	Unit
Proton energy $(E_p)$	7000	GeV
Relativistic $\gamma$	7461	
Number of particles per bunch $(N_b)$	$1.15 \times 10^{11}$	
Number of bunches $(n)$	2808	
Normalised transverse emittance	3.75	$\mu { m m} { m rad}$
Beta function $(\beta)$	0.55	m
Bunch length $(\sigma_z)$	7.55	cm
RMS bunch size $(\sigma_x = \sigma_y = \sigma^*)$	16.7	$\mu { m m}$
Crossing angle $(\theta_c)$	285	$\mu$ rad

The parameters for the LHC at the ATLAS interaction point are

Some general LHC parameters are

Parameter	Value	Unit
Ring circumference	26658.9	m
Revolution frequency	11.245	kHz

#### Question 1

Calculate the peak luminosity of the LHC in  $\rm cm^{-2}s^{-1}$  with and without a crossing angle.

#### Question 2

Calculate the total beam power in a full storage of the LHC and briefly discuss why this might cause difficulties.

[3 marks]

[3 marks]

[5 marks]

#### Question 3

Discuss the factors which limit the luminosity of the LHC.

#### Question 4

Discuss how the LHC luminosity and energy could be upgraded, whilst keeping the same circumference ring, with as much reference as possible to your answers to previous questions.

[4 marks][Total Marks = 15]