

# Simultaneous QCD analysis of diffractive and inclusive DIS data

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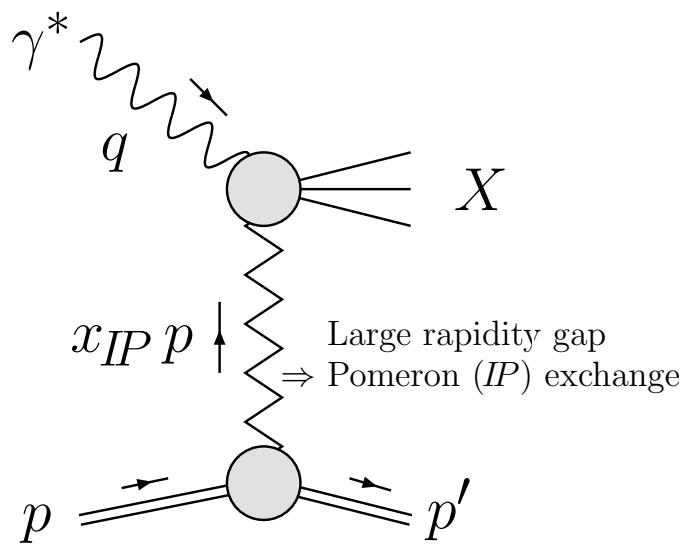
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# Diffractive DIS kinematics



- $q^2 \equiv -Q^2$
- $W^2 \equiv (q + p)^2 = -Q^2 + 2 p \cdot q$   
 $\Rightarrow x_B \equiv \frac{Q^2}{2 p \cdot q} = \frac{Q^2}{Q^2 + W^2}$   
**(fraction of proton's momentum carried by struck quark)**
- $t \equiv (p - p')^2 \approx 0, (p - p') \approx x_{IP} p$
- $M_X^2 \equiv (q + p - p')^2 = -Q^2 + x_{IP}(Q^2 + W^2)$   
 $\Rightarrow x_{IP} = \frac{Q^2 + M_X^2}{Q^2 + W^2}$   
**(fraction of proton's momentum carried by Pomeron)**
- $\beta \equiv \frac{x_B}{x_{IP}} = \frac{Q^2}{Q^2 + M_X^2}$  **(fraction of Pomeron's momentum carried by struck quark)**

# Diffractive structure function $F_2^{D(3)}$

- Diffractive cross section (integrated over  $t$ ):

$$\frac{d^3\sigma^D}{dx_{IP} d\beta dQ^2} = \frac{2\pi\alpha_{em}^2}{\beta Q^4} [1 + (1 - y)^2] \sigma_r^{D(3)}(x_{IP}, \beta, Q^2),$$

where  $y = Q^2/(x_B s)$ ,  $s = 4E_e E_p$ , and

$$\sigma_r^{D(3)} = F_2^{D(3)} - \frac{y^2}{1 + (1 - y)^2} F_L^{D(3)} \approx F_2^{D(3)}(x_{IP}, \beta, Q^2),$$

for small  $y$  and/or small  $F_L^{D(3)}/F_2^{D(3)}$

- Measurements of  $F_2^{D(3)} \Rightarrow$  **diffractive** parton distribution functions (**DPDFs**)

$$a^D(x_{IP}, \beta, Q^2) = \beta \Sigma^D(x_{IP}, \beta, Q^2) \text{ or } \beta g^D(x_{IP}, \beta, Q^2)$$

# ‘Traditional’ extraction of DPDFs

- Assume Regge factorisation [Ingelman-Schlein,1985]:

$$F_2^{D(3)}(x_{IP}, \beta, Q^2) = f_{IP}(x_{IP}) F_2^{IP}(\beta, Q^2)$$

- Pomeron flux factor from Regge phenomenology:

$$f_{IP}(x_{IP}) = \int_{t_{\text{cut}}}^{t_{\min}} dt \frac{e^{B_{IP} t}}{x_{IP}^{2\alpha_{IP}(t)-1}} \quad (\alpha_{IP}(t) = \alpha_{IP}(0) + \alpha'_{IP} t)$$

Fits to  $F_2^{D(3)}$  data give  $\alpha_{IP}(0) > 1.08$  (value from soft hadron data)  
 $\implies$  **effective** Pomeron intercept

- Evaluate Pomeron structure function  $F_2^{IP}(\beta, Q^2)$  from quark singlet  $\Sigma^{IP}(\beta, Q^2)$  and gluon  $g^{IP}(\beta, Q^2)$  Pomeron PDFs DGLAP-evolved from **arbitrary polynomial input** at scale  $Q_0^2$

# New perturbative QCD approach

- Pomeron singularity not a *pole* but a *cut* [Lipatov,1986]  
⇒ **continuous** number of components of **size  $1/\mu$** :

$$F_{2,P}^{D(3)}(x_{IP}, \beta, Q^2) = \int_{Q_0^2}^{Q^2} d\mu^2 f_{IP}(x_{IP}; \mu^2) F_2^{IP}(\beta, Q^2; \mu^2)$$

- Perturbative Pomeron represented by **two  $t$ -channel gluons** in colour singlet:

$$f_{IP=G}(x_{IP}; \mu^2) = \frac{1}{x_{IP}} \left[ \frac{\alpha_S(\mu^2)}{\mu^2} x_{IP} g(x_{IP}, \mu^2) \right]^2$$

where  $g(x_{IP}, \mu^2)$  is the (integrated) gluon distribution of the proton

# Problem: $x_{IP} g(x_{IP}, \mu^2)$ at low $\mu^2$

- $f_{IP=G}(x_{IP}; \mu^2) \propto [x_{IP} g(x_{IP}, \mu^2) / \mu^2]^2$   
 $\Rightarrow$  dominant contribution from low scales  $\mu \sim Q_0 \sim 1 \text{ GeV}$
- $F_2^{D(3)}$  data need  $x_{IP} g(x_{IP}, \mu^2) \sim x_{IP}^{-\lambda}$  with  $\lambda \simeq 0.17$

Solution:

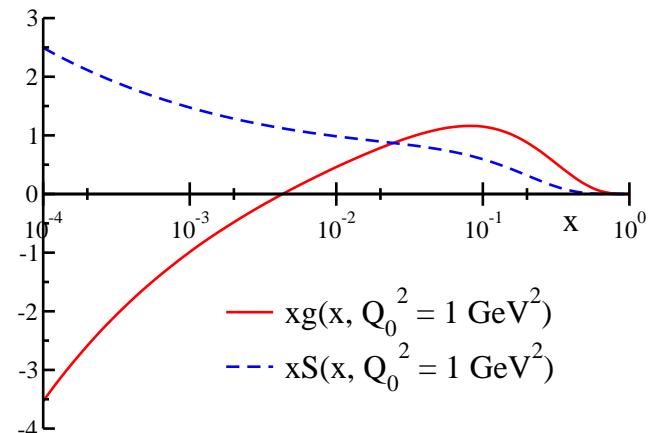
- Introduce Pomeron composed of two sea quarks in a colour singlet:

$$f_{IP=S}(x_{IP}; \mu^2) = \frac{1}{x_{IP}} \left[ \frac{\alpha_S(\mu^2)}{\mu^2} x_{IP} S(x_{IP}, \mu^2) \right]^2$$

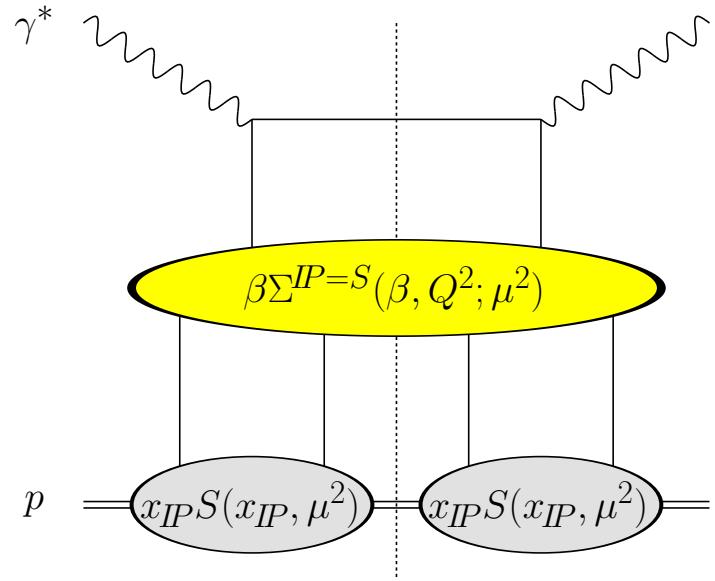
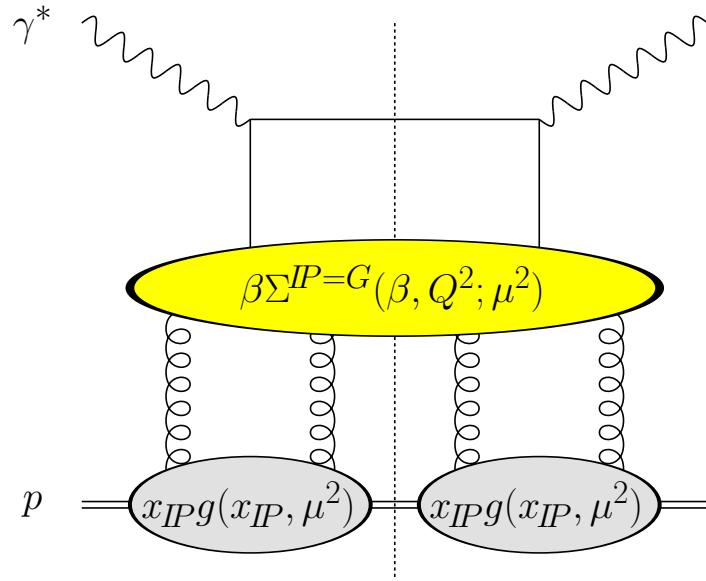
and interference term with two-gluon Pomeron ( $IP = GS$ )  
(set  $x_{IP} g(x_{IP}, \mu^2) = 0$  if  $-ve$ )

• But ...

MRST2001 NLO proton PDFs



# New perturbative QCD approach



- $F_2^{IP}(\beta, Q^2; \mu^2)$  calculated from quark singlet  $\Sigma^{IP}(\beta, Q^2; \mu^2)$  and gluon  $g^{IP}(\beta, Q^2; \mu^2)$  DGLAP-evolved from an input scale  $\mu^2$  up to  $Q^2$
- Get **input** Pomeron PDFs  $\Sigma^{IP}(\beta, \mu^2; \mu^2)$  and  $g^{IP}(\beta, \mu^2; \mu^2)$  from **lowest-order Feynman diagrams**. Calculate using light-cone wave functions of the photon [Wüsthoff, 1997]

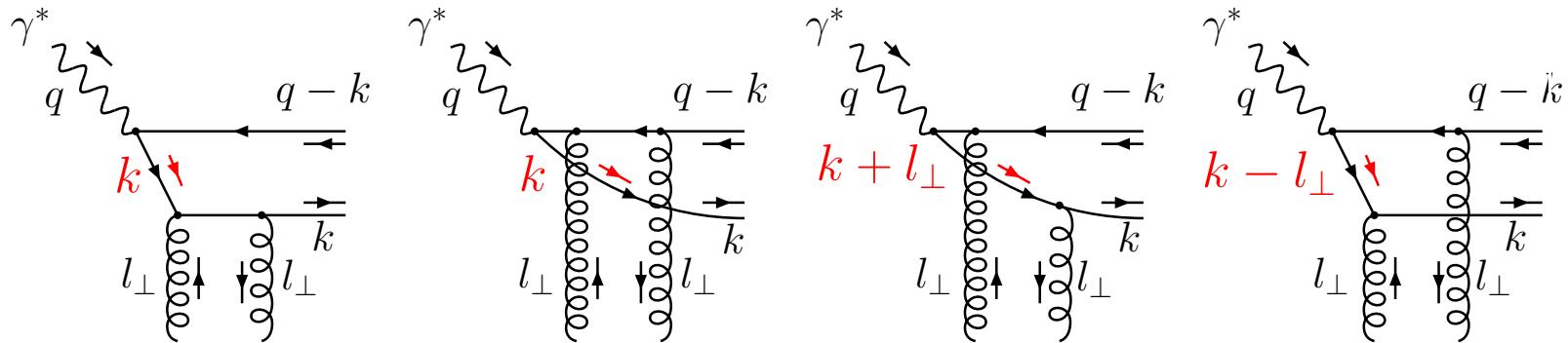
# Example of dipole calculations

Two-gluon Pomeron, transversely-polarised photon,  $\gamma^* \rightarrow q\bar{q}$ :

$$\frac{d\sigma_{q\bar{q},T}^{\gamma^* p}}{dt} \Big|_{t=0} = \frac{N_C}{16\pi} \int_0^1 d\alpha \int \frac{dk_t^2}{2\pi} \sum_f e_f^2 \alpha_{\text{em}} \frac{1}{2} \sum_{\gamma=\pm 1} \sum_{h=\pm 1} \left| \int \frac{d^2 l_t}{\pi} D\Psi_h^\gamma \frac{d\hat{\sigma}}{dl_t^2} \right|^2$$

- Obtain four different permutations by simply shifting argument of wave functions:

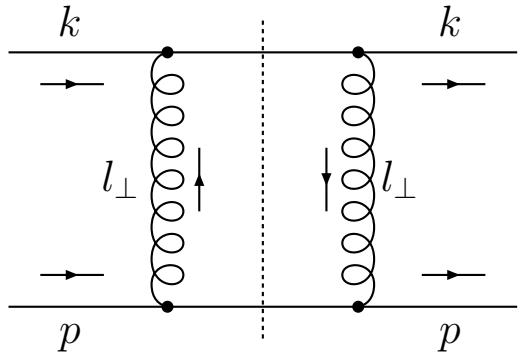
$$D\Psi(\alpha, \mathbf{k}_t, \mathbf{l}_t) \equiv 2\Psi(\alpha, \mathbf{k}_t) - \Psi(\alpha, \mathbf{k}_t + \mathbf{l}_t) - \Psi(\alpha, \mathbf{k}_t - \mathbf{l}_t)$$



# Example of dipole calculations

- Obtain dipole cross section  $\frac{d\hat{\sigma}}{dl_t^2}(q\bar{p} \rightarrow q\bar{p})$  from  $\frac{d\hat{\sigma}}{dl_t^2}(q\bar{q} \rightarrow q\bar{q})$ :

- Make replacement



$$\left. \frac{\alpha_S(l_t^2)}{2\pi} x_{IP} P_{gq}(x_{IP}) \right|_{x_{IP} \ll 1} \rightarrow f_g(x_{IP}, l_t^2, \mu^2)$$

where  $\mu^2 \equiv k_t^2/(1-\beta)$  and  $f_g(x_{IP}, l_t^2, \mu^2)$  is the *unintegrated* gluon distribution

- Work in strongly-ordered limit ( $l_t \ll k_t \ll Q$ ):

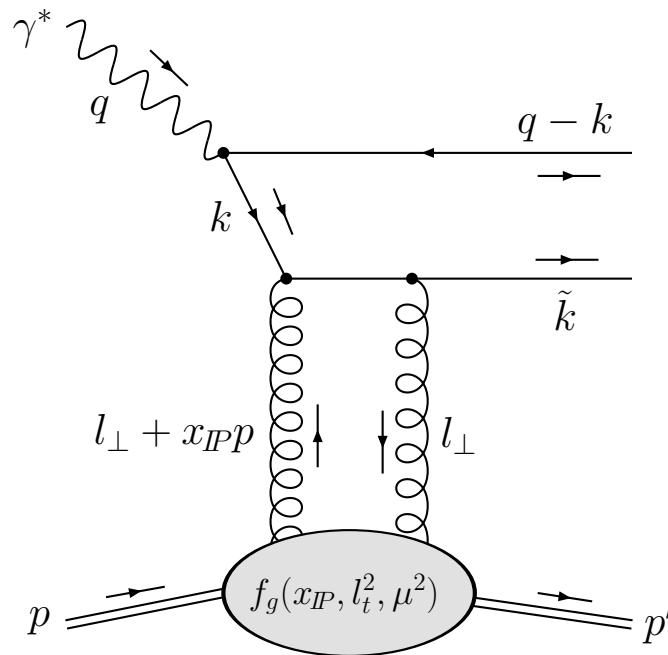
$$\int \frac{d^2 l_t}{\pi} D\Psi_h^\gamma \frac{d\hat{\sigma}}{dl_t^2} \sim \int_0^{\mu^2} dl_t^2 \frac{l_t^2}{l_t^4} f_g(x_{IP}, l_t^2, \mu^2) = x_{IP} g(x_{IP}, \mu^2)$$

$D\Psi_h^\gamma$  gives the  $\beta$  dependence of  $\Sigma^{IP=G}(\beta, \mu^2; \mu^2)$

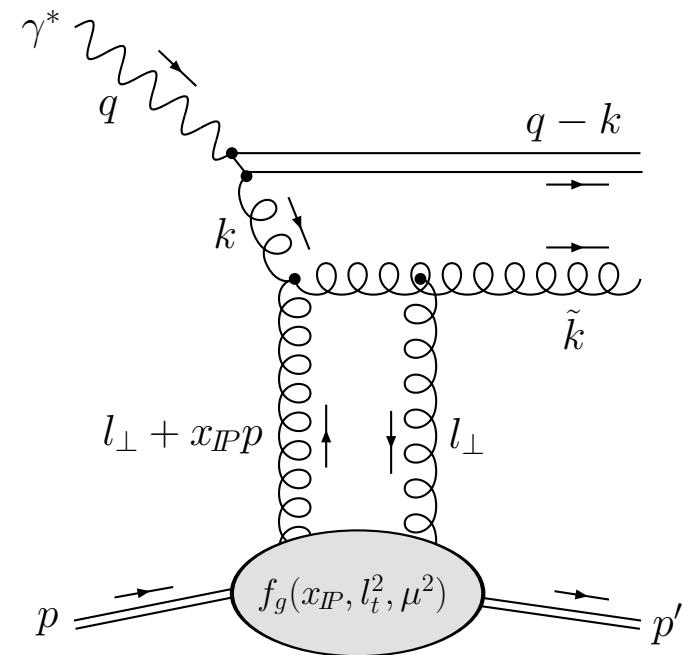
# Two-gluon Pomeron

- Work in strongly-ordered limit:  $l_t \ll k_t \ll Q$

Quark dipole



Effective gluon dipole



$$\beta \Sigma^{IP=G}(\beta, \mu^2; \mu^2) = c_{q/G} \beta^3 (1 - \beta)$$

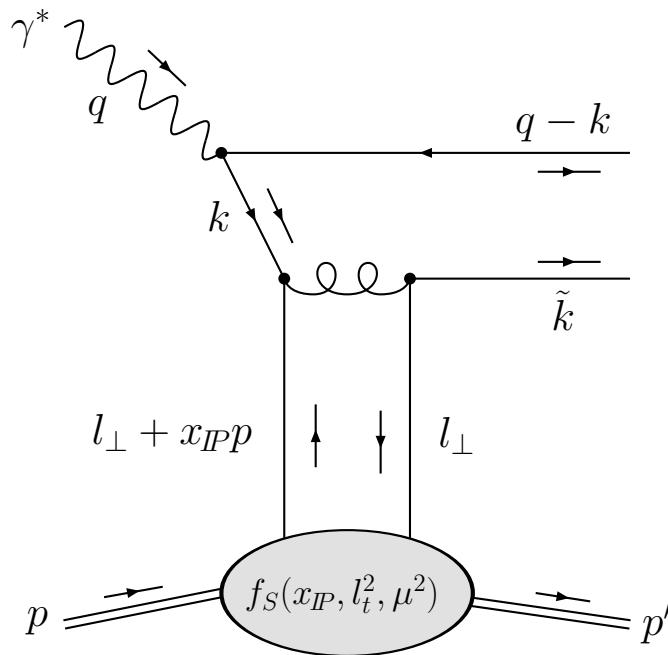
$$F_L^{IP=G}(\beta) = c_{L/G} \beta^3 (2\beta - 1)^2$$

$$\beta' g^{IP=G}(\beta', \mu^2; \mu^2) = c_{g/G} (1 + 2\beta')^2 (1 - \beta')^2$$

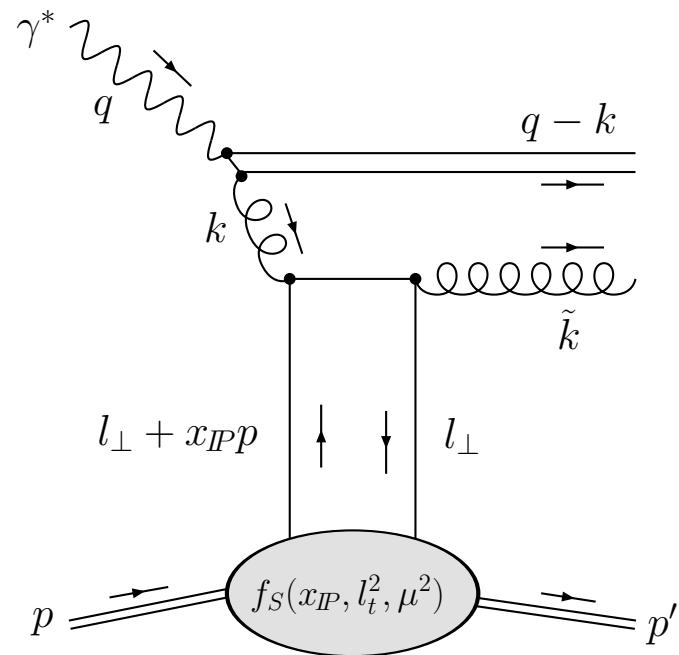
# Two-quark Pomeron

- Work in strongly-ordered limit:  $l_t \ll k_t \ll Q$

Quark dipole



Effective gluon dipole



$$\beta \Sigma^{IP=S}(\beta, \mu^2; \mu^2) = c_{q/S} \beta (1 - \beta)$$

$$F_L^{IP=S}(\beta) = c_{L/S} \beta^3$$

$$\beta' g^{IP=S}(\beta', \mu^2; \mu^2) = c_{g/S} (1 - \beta')^2$$

# Other contributions to $F_2^{D(3)}$

$$F_2^{D(3)} = F_{2,P}^{D(3)} + F_{2,NP}^{D(3)} + F_{L,P}^{D(3)} + F_{2,IR}^{D(3)}$$

- Non-perturbative contribution ( $\mu < Q_0$ ,  $\alpha_{IP}(0) = 1.08$ ):

$$F_{2,NP}^{D(3)} = f_{IP=NP}(x_{IP}) F_2^{IP=NP}(\beta, Q^2; Q_0^2)$$

$$[\beta \Sigma^{IP=NP}(\beta, Q_0^2; Q_0^2) = c_{q/NP} \beta (1 - \beta), \quad \beta' g^{IP=NP}(\beta', Q_0^2; Q_0^2) = 0]$$

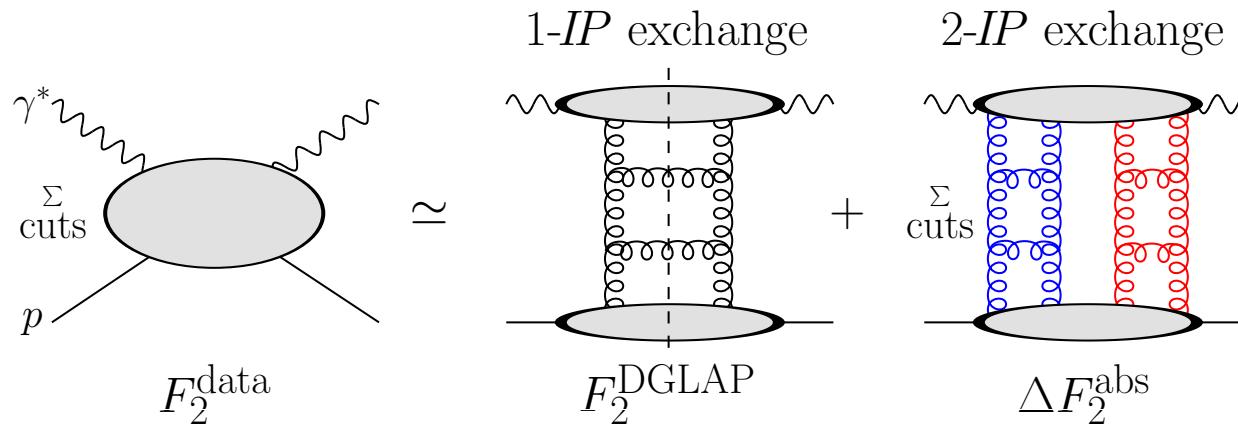
- Twist-four contribution:

$$F_{L,P}^{D(3)} = \sum_{IP=G,S,GS} \left( \int_{Q_0^2}^{Q^2} d\mu^2 \frac{\mu^2}{Q^2} f_{IP}(x_{IP}; \mu^2) \right) F_L^{IP}(\beta)$$

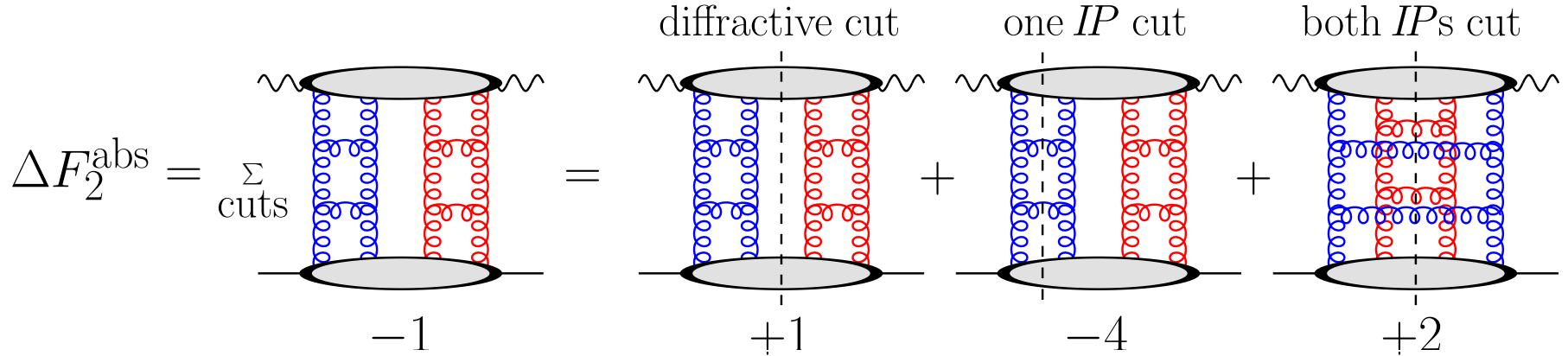
- Secondary Reggeon contribution ( $\alpha_{IR}(0) = 0.50$ ):

$$F_{2,IR}^{D(3)} = c_{IR} f_{IR}(x_{IP}) F_2^{\pi}(\beta, Q^2)$$

# Absorptive corrections to $F_2$



- **AGK cutting rules**<sup>a</sup>  $\Rightarrow$  **diffractive events** are intimately related to **absorptive corrections** to the **inclusive** structure function  $F_2$ :



<sup>a</sup> Abramovsky-Gribov-Kancheli (1973)  $\rightarrow$  QCD: Bartels-Ryskin (1997)

# Absorptive corrections to $F_2$

$$F_2^{\text{data}}(x_B, Q^2) = F_2^{\text{DGLAP}}(x_B, Q^2) + \Delta F_2^{\text{abs}}(x_B, Q^2)$$

$$\Delta F_2^{\text{abs}}(x_B, Q^2) = - \int_{Q_0^2}^{Q^2} d\mu^2 F_2^D(x_B, Q^2; \mu^2)$$

- $F_2^D(x_B, Q^2; \mu^2)$  is the contribution to  $F_2^{D(3)}$  (integrated over  $x_{IP}$ ) originating from a **perturbative** component of the Pomeron of **size**  $1/\mu$ . The  $\mu < Q_0$  contributions to the absorptive corrections are **already included** in the input parameterisations to the  $F_2$  fit
- To fit  $F_2$  using the **DGLAP** equation, first need to ‘correct’ the **data** for absorptive effects:<sup>a</sup>

$$F_2^{\text{DGLAP}} = F_2^{\text{data}} - \Delta F_2^{\text{abs}} = F_2^{\text{data}} + |\Delta F_2^{\text{abs}}|$$

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<sup>a</sup> Aside: absorptive corrections  $\sim$  non-linear effects, screening, shadowing, unitarity corrections, multiple scattering, multiple interactions, recombination, saturation effects, ...

# Simultaneous $F_2 + F_2^{D(3)}$ analysis

- Procedure:

1. Start by fitting ZEUS + H1  $F_2$  data (279 points)<sup>a</sup> with no absorptive corrections  $\sim$  MRST2001 NLO
2. Fit ZEUS + H1  $F_2^{D(3)}$  data, using  $g(x_{IP}, \mu^2)$  and  $S(x_{IP}, \mu^2)$  from previous  $F_2$  fit
3. Fit  $F_2^{\text{DGLAP}} = F_2^{\text{data}} + |\Delta F_2^{\text{abs}}|$ , with  $\Delta F_2^{\text{abs}}$  from previous  $F_2^{D(3)}$  fit
4. Go to 2.

- Only a few iterations needed for convergence

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<sup>a</sup>Cuts:  $x_B < 0.01$ ,  $2 < Q^2 < 500 \text{ GeV}^2$ ,  $W^2 > 12.5 \text{ GeV}^2$ ; match to MRST  $xg, xS$  at  $x = 0.2$

# Description of $F_2^{D(3)}$ data

- Fit three different data sets simultaneously, allowing for *different* relative normalisations due to *proton dissociation*:

Data set	Points <sup>a</sup>	Proton dissociation	Normalisation
1997 ZEUS LPS (prel.)	69	none	1
1998/99 ZEUS (prel.)	121	$M_Y < 2.3 \text{ GeV}$	$\approx 1.5$
1997 H1 (prel.)	214	$M_Y < 1.6 \text{ GeV}$	$\approx 1.2$

- Only other free parameters are *normalisations* (effective  $K$ -factors) of the input Pomeron PDFs, the twist-four contributions and the secondary Reggeon contribution:

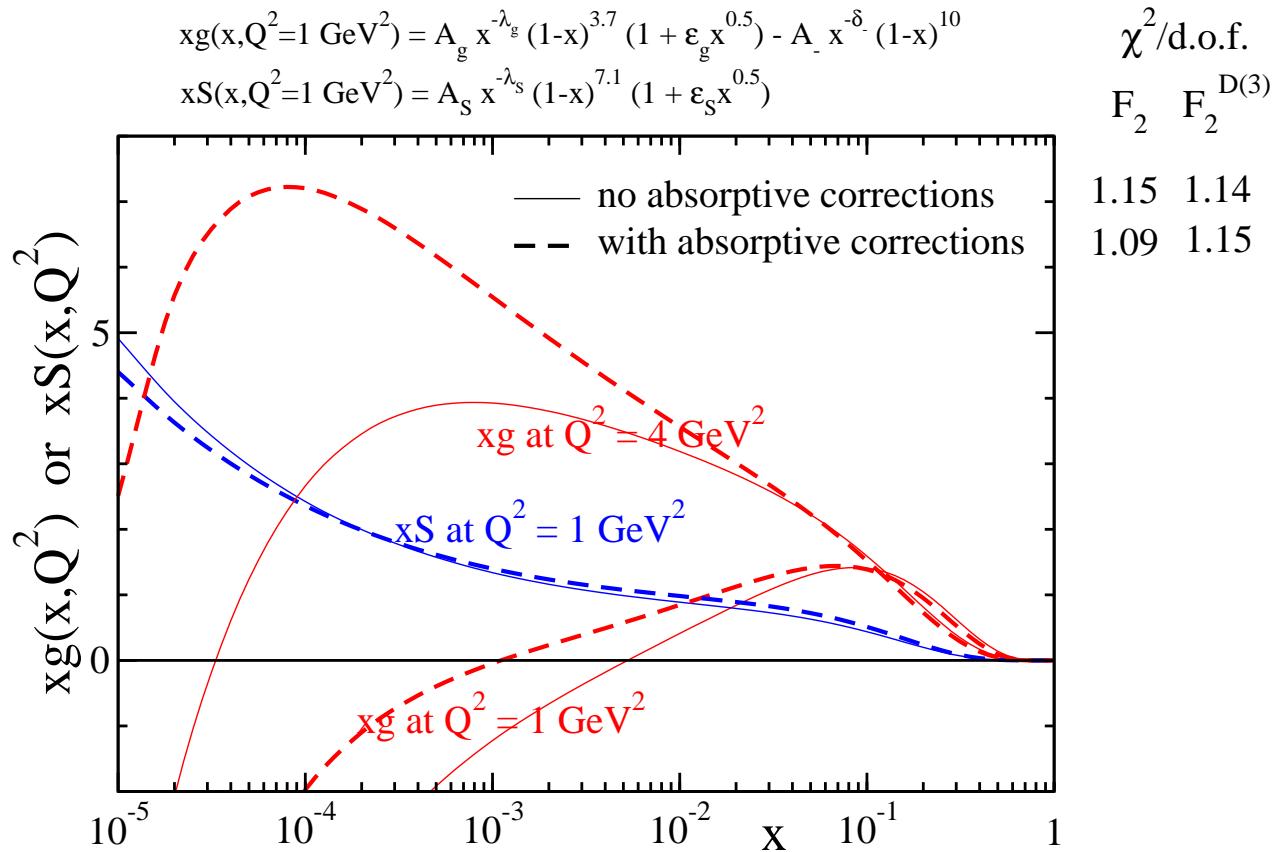
$$c_{q/G}, c_{g/G}, c_{L/G}, c_{q/S}, c_{g/S}, c_{L/S}, c_{q/NP}, c_{IR} \quad (Q_0 = 1 \text{ GeV})$$

(Fix  $c_{i/GS} = \sqrt{c_{i/G} c_{i/S}}$  for  $i = q, g, L$ )

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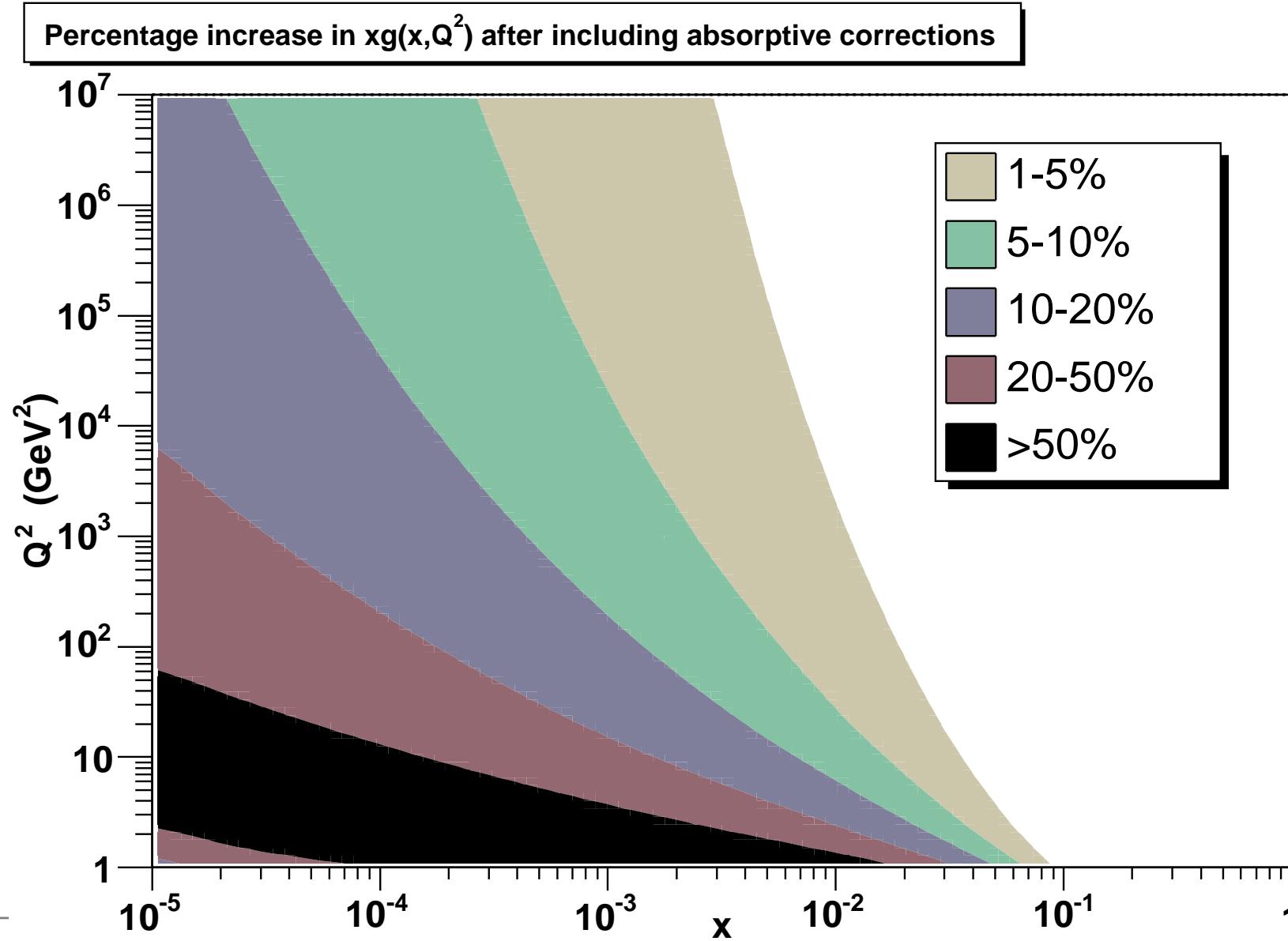
<sup>a</sup>Cuts:  $M_X > 2 \text{ GeV}$ ,  $y < 0.45$

# Gluon and sea quark PDFs

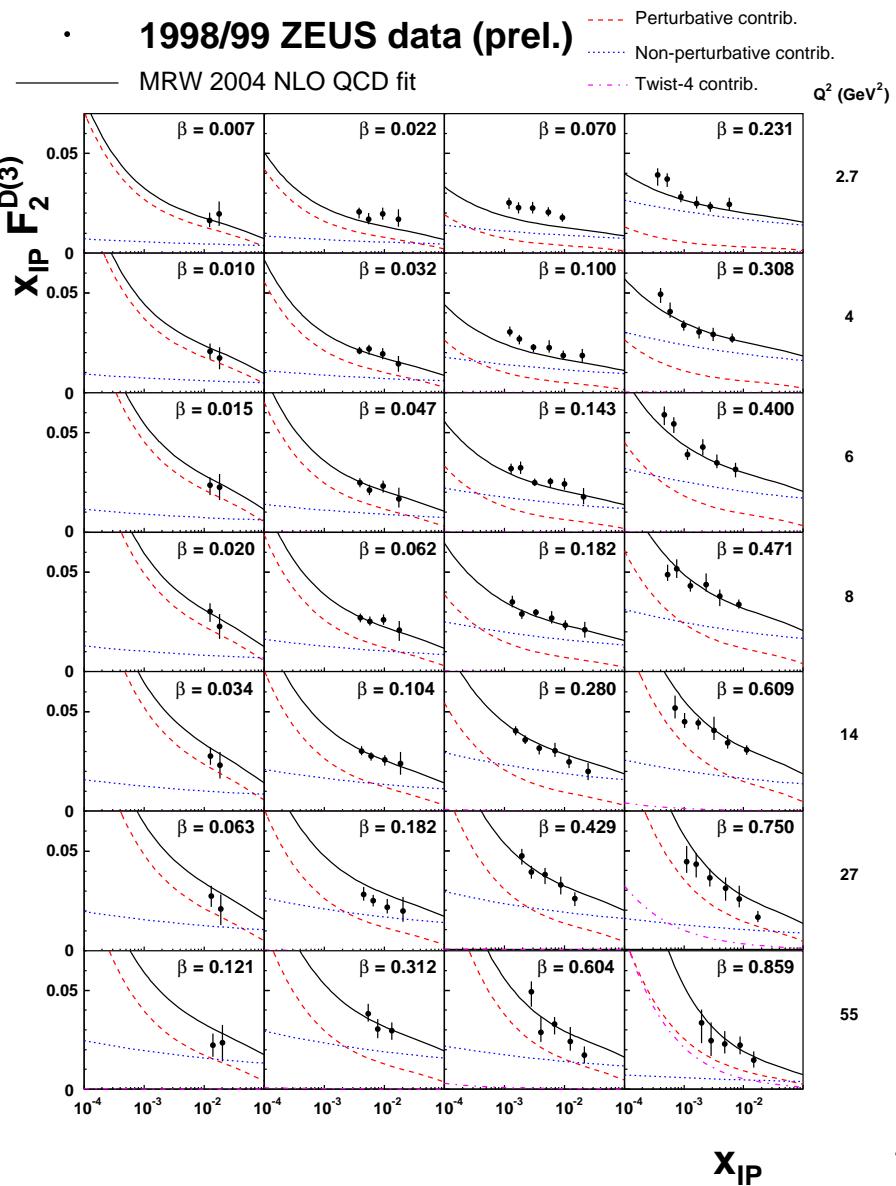
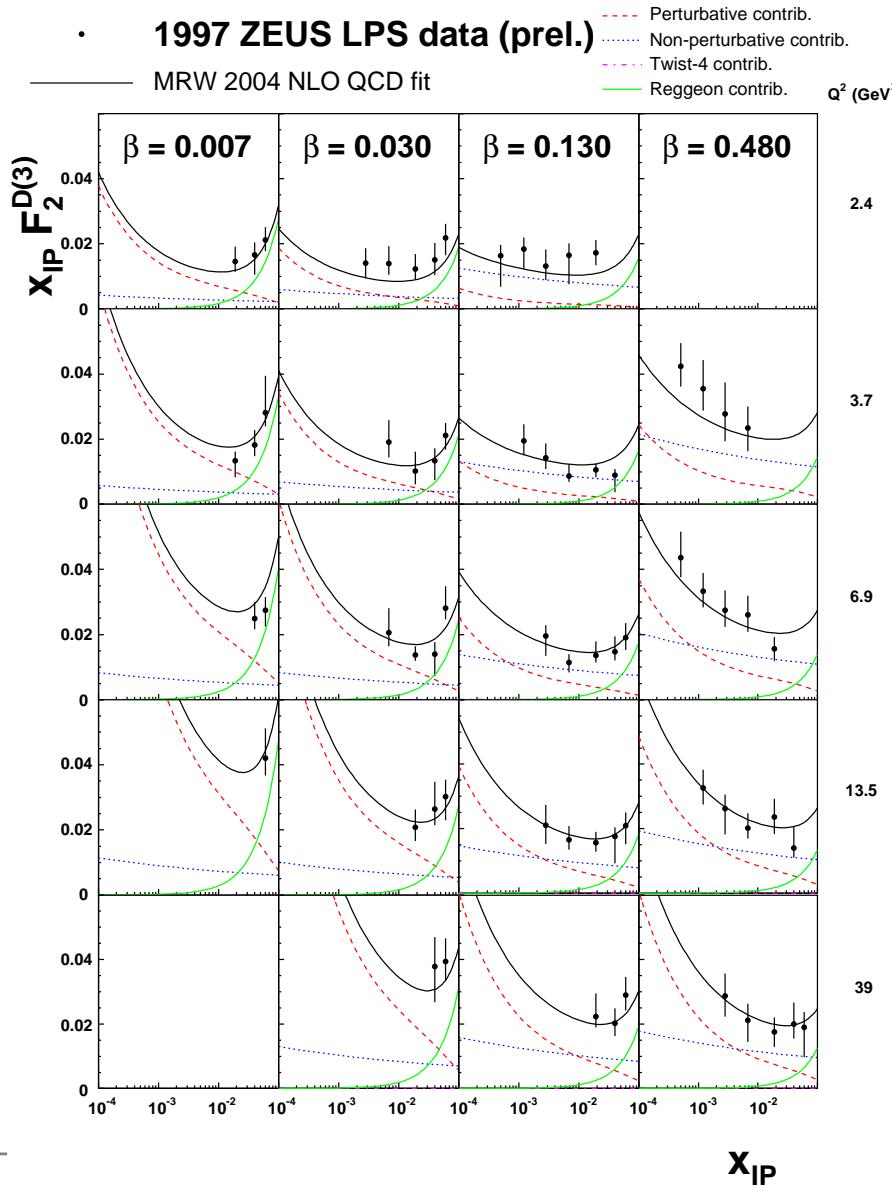


- Take +ve input gluon parameterisation ( $A_- = 0$ ):
  - no absorptive corrections  $\chi^2/\text{d.o.f.} = 1.57$  for  $F_2$ , 1.17 for  $F_2^{D(3)}$
  - with absorptive corrections  $\chi^2/\text{d.o.f.} = 1.11$  for  $F_2$ , 1.14 for  $F_2^{D(3)}$

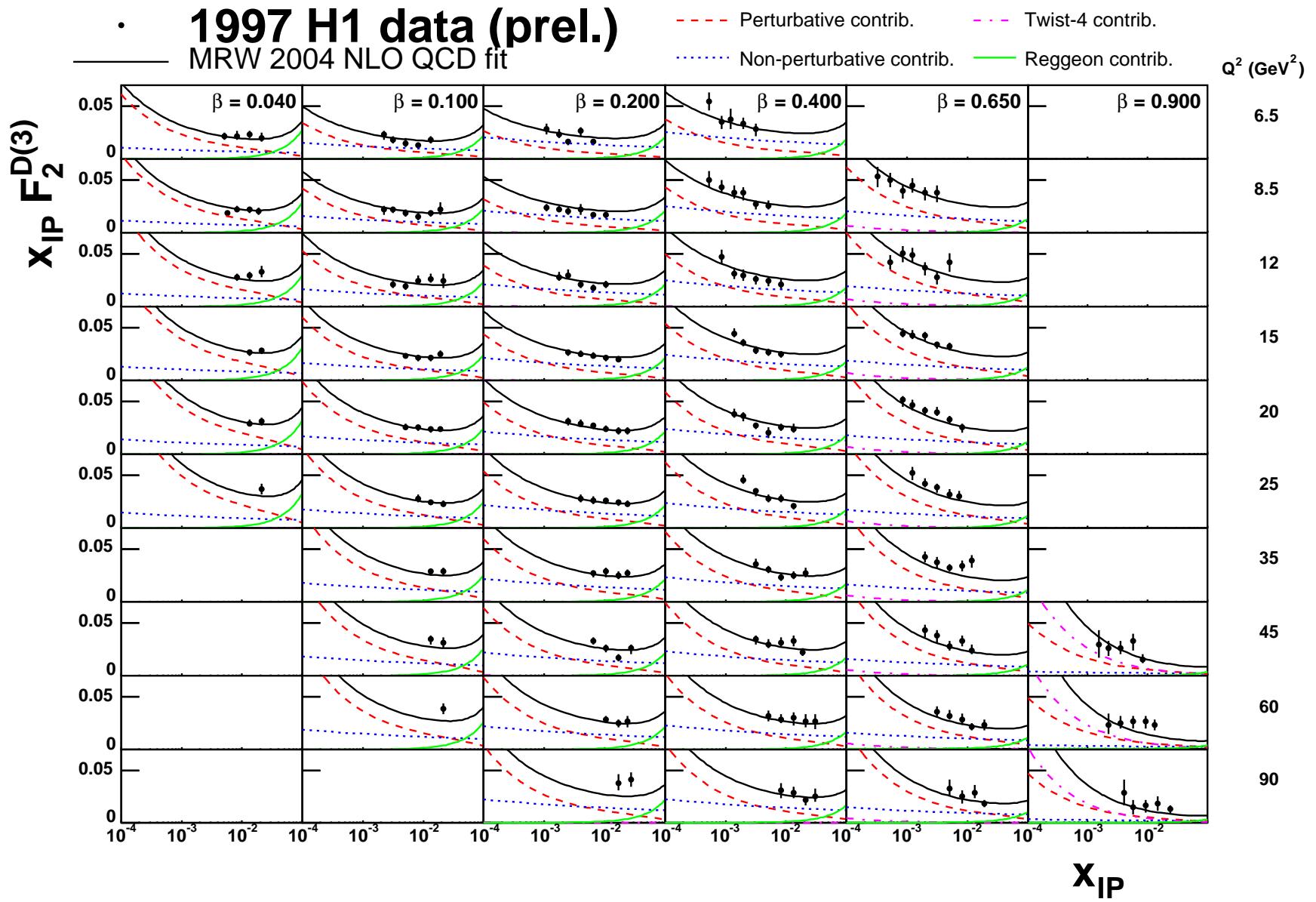
# Percentage increase in gluon distribution



# Fit to ZEUS + H1 $F_2^{D(3)}$

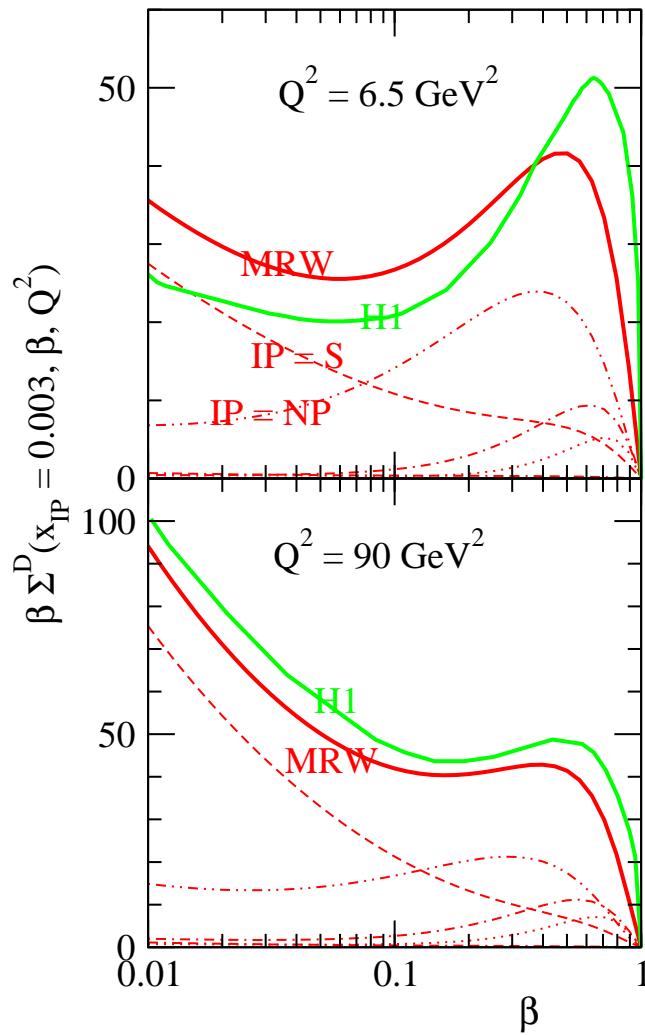


# Fit to ZEUS + H1 $F_2^{D(3)}$

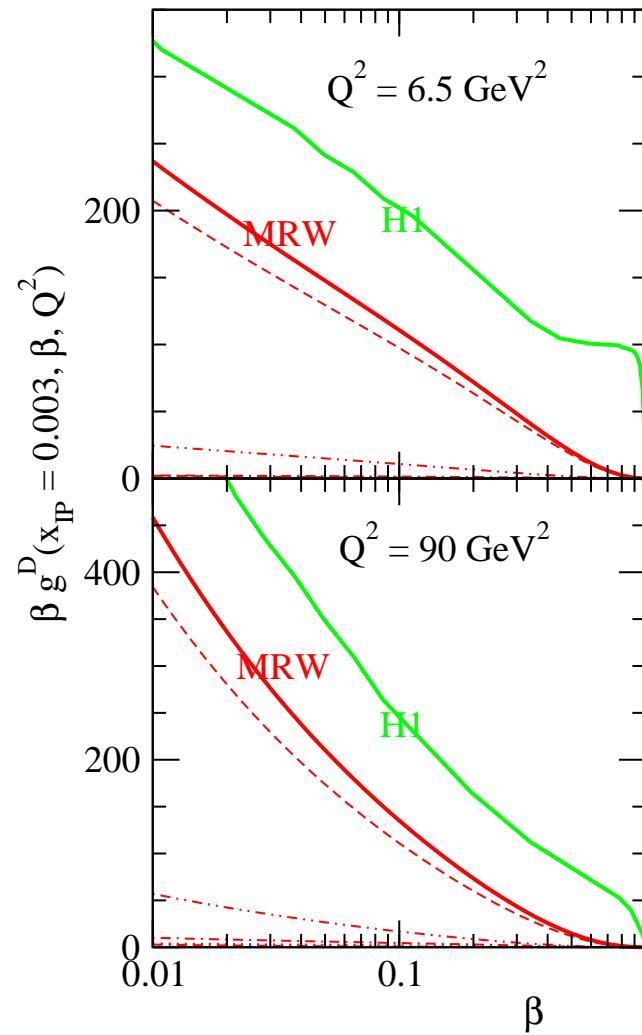


# DPDFs compared to H1 fit

Diffractive quark singlet distribution



Diffractive gluon distribution



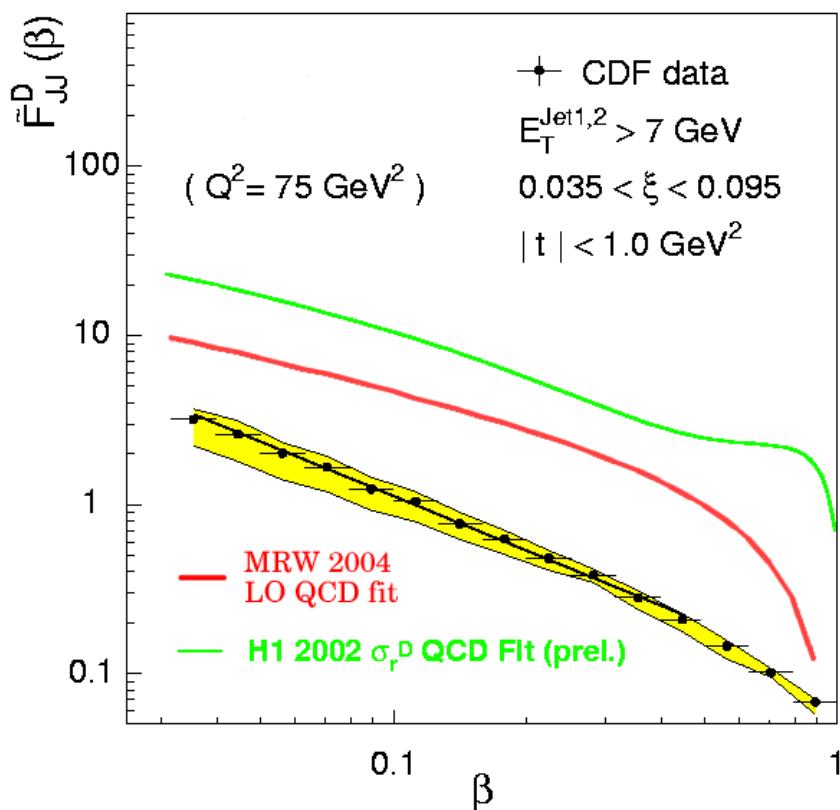
- MRW 2004  
NLO QCD fit
- IP = G component
- - IP = S component
- · IP = GS component
- - - IP = NP component
- - - - IR component
- H1 2002  
NLO QCD fit (prel.)

- H1 use a **smaller  $\alpha_S$**  and have **no twist-four contribution**

# CDF diffractive dijets

- Diffractive structure function of the antiproton:

$$\tilde{F}_{JJ}^D(\beta) = \frac{1}{\xi_{\max} - \xi_{\min}} \int_{\xi_{\min}}^{\xi_{\max}} d\xi \left[ \beta g^D(\xi, \beta, Q^2) + \frac{4}{9} \beta \Sigma^D(\xi, \beta, Q^2) \right]$$



- Results for “survival probability” of the rapidity gap do not contradict calculation by KKMR: <sup>a</sup>

$$S^2 \simeq 0.12-0.28$$

*a*

Khoze-Martin-Ryskin, Eur. Phys. J. C **18** (2000) 167;  
Kaidalov-KMR, Eur. Phys. J. C **21** (2001) 521

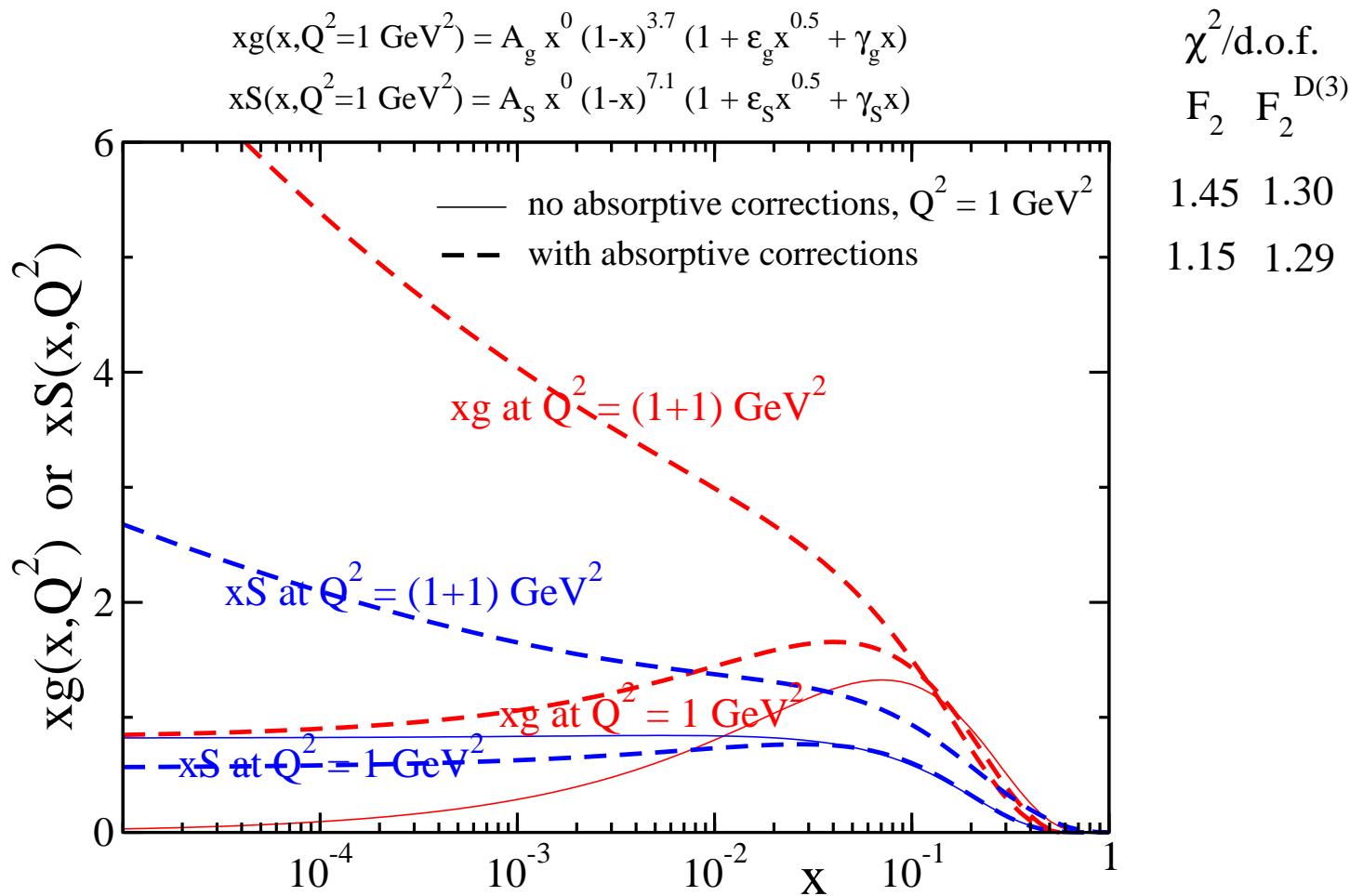
# ‘Pomeron-like’ $xS$ but ‘valence-like’ $xg$ ?

- Good news: Absorptive corrections remove the need for a negative input gluon distribution when fitting inclusive  $F_2$  data
- Bad news: Still have ‘Pomeron-like’ sea quarks but ‘valence-like’ gluons at small  $x$  and low  $Q^2$ :

$$xg \sim x^{-\lambda_g}, xS \sim x^{-\lambda_S} \quad \text{with} \quad \lambda_g < 0 \text{ and } \lambda_S > 0$$

- Reminder:
  - Regge theory  $\Rightarrow \lambda_g = \lambda_S$
  - Resummed NLL BFKL  $\Rightarrow \lambda_g = \lambda_S \simeq 0.3$
  - Soft hadron data  $\Rightarrow \lambda \simeq 0.08$
- Must be some large non-perturbative effect causing the observed behaviour. One possibility: mimic unknown power corrections by shifting scale in  $F_2$  and  $F_2^{D(3)}$  fits by  $\approx 1 \text{ GeV}^2$ . Fix  $\lambda_g = \lambda_S = 0$

# Shift scale by 1 GeV<sup>2</sup> ?



- Satisfactory description of  $F_2$  and  $F_2^{D(3)}$  data with ‘flat’ asymptotic behaviour ( $x \rightarrow 0$ ) of input  $xg, xS$

# Conclusions

- **New perturbative QCD description of  $F_2^{D(3)}$** 
  - Pomeron singularity not a *pole* but a *cut*  
⇒ Integral over Pomeron scale  $\mu$
  - Input Pomeron PDFs from lowest-order QCD diagrams
  - Two-quark Pomeron in addition to two-gluon Pomeron
- **Absorptive corrections to  $F_2$  from AGK cutting rules**
  - Good news: remove need for negative gluon input
  - Dilemma: still have ‘Pomeron-like’ sea quarks but  
‘valence-like’ gluons at small  $x$  and low  $Q^2$ 
    1. Non-perturbative Pomeron doesn’t couple to gluons,  
secondary Reggeon couples more to gluons than sea quarks ?
    2. Unknown non-perturbative power corrections slow down  
DGLAP evolution at low  $Q^2$  ?